

Lecture-1

Date: 05.08.2014

- Motivation
- Why this course?
- Differentiating factor between low and high frequency circuits
- Transmission Line (Intro.)

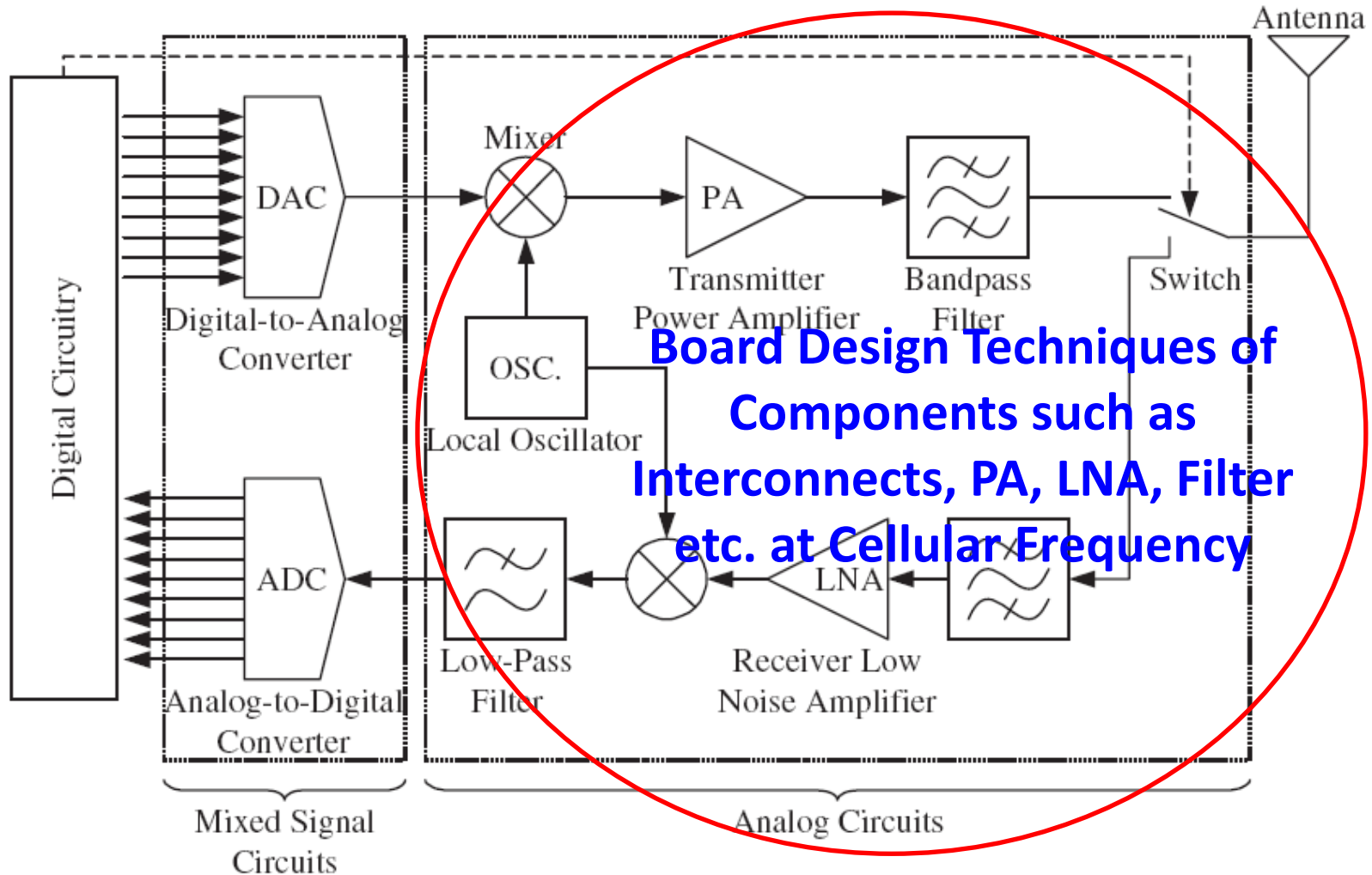
Motivation

- **Importance of RF Circuit Design**
 - Wireless/Wirebased Communication Circuits → multi-band and multi-standard transceivers
 - Global Positioning System (GPS)
 - Increased clock speeds in ASICs/SoCs

- **Why this course**
 - Lumped no more applicable!
 - Solution? → **distributed!!!**

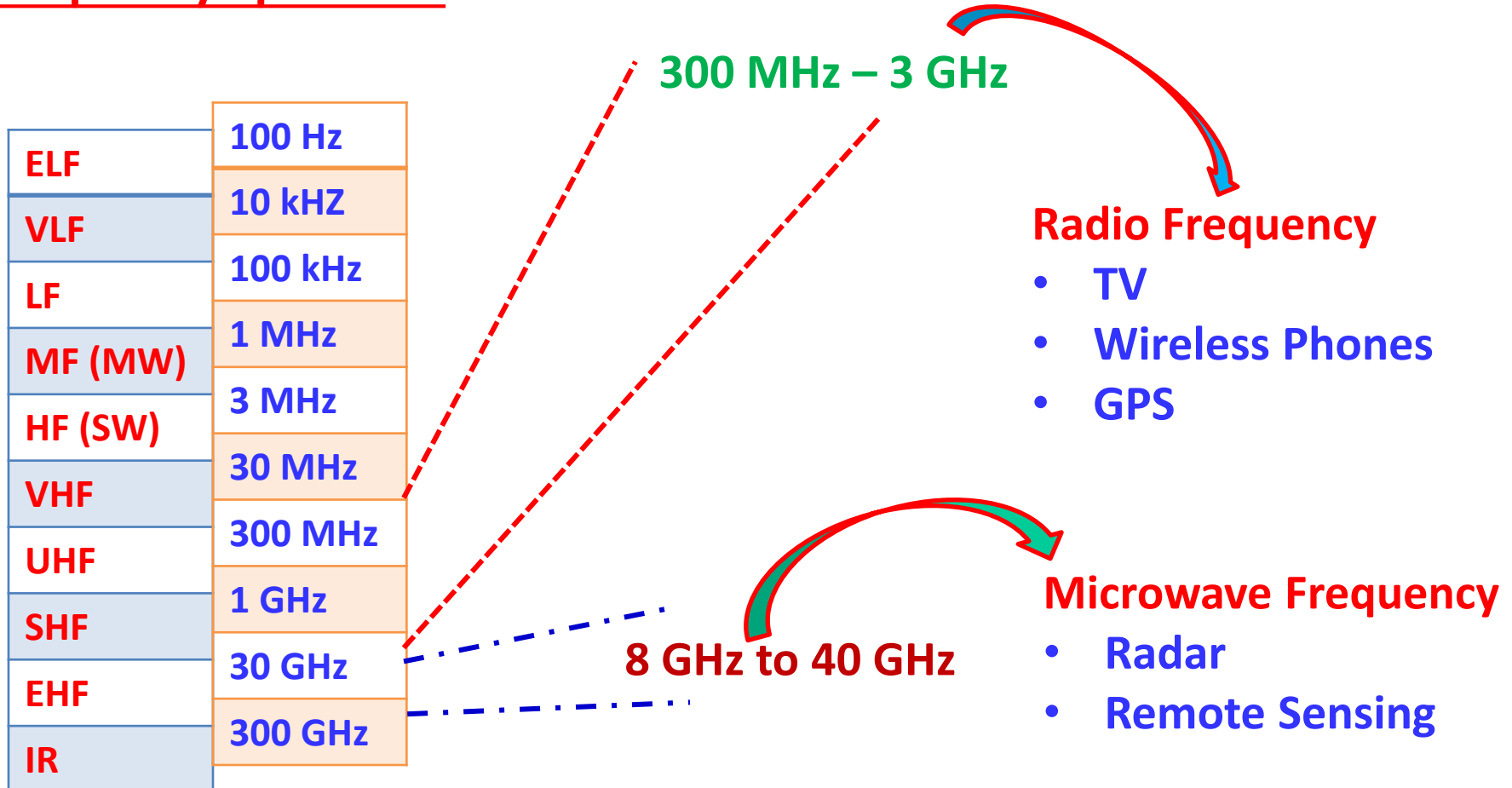
Motivation (contd.)

Design Focus in this Course



Motivation (contd.)

Frequency Spectrum



Why this course?

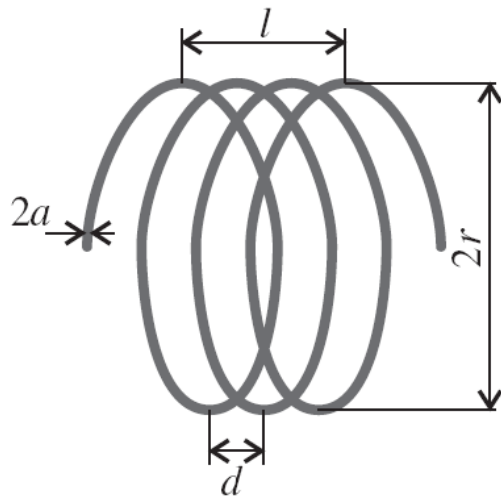
- Lumped components (wires, resistors, capacitors, inductors, connectors etc.) behave differently at low and high frequencies.
- Why?
 - current and voltage vary spatially over the component size
 - Leads to the concept of distributed components!

The KCL and KVL are no more applicable

Why this course?

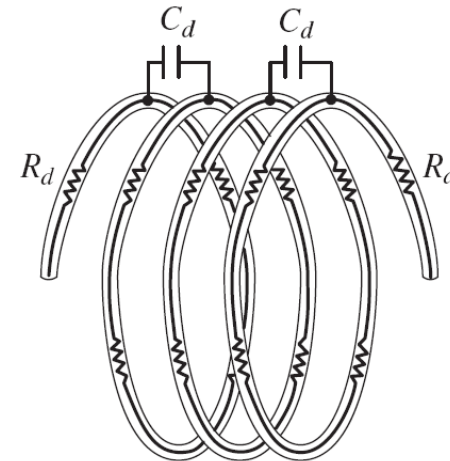
- What do we mean by distributed?
 - Example – Inductor

Low Frequency (Lumped)



$$Z = R + j\omega L$$

High Frequency (Distributed)



$$Z = ?$$

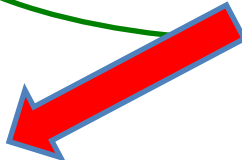
RF Behavior of Passive Components

- Why do inductors, capacitors, and resistors behave differently at Radio Frequency?
- What is skin effect?
- Equivalent Circuit Model?

RF Behavior of Passive Components (contd.)

For conventional AC circuit analysis:

- R is considered frequency independent
- Ideal Inductor (L) possesses an impedance ($X_L = j\omega L$)
- Ideal capacitor (C) possesses an impedance ($X_C = 1/j\omega C$)



Capacitor behaves as open circuit at DC and low frequency whereas an Inductor behaves as short circuit at DC and low frequencies

RF Behavior of Resistors

At low frequency:

- Resistances, inductances, and capacitances are formed by wires, coils, and plates etc.
- Even a single wire or a copper line on a PCB possesses resistance and inductance.
- this cylindrical copper conductor has a DC resistance:

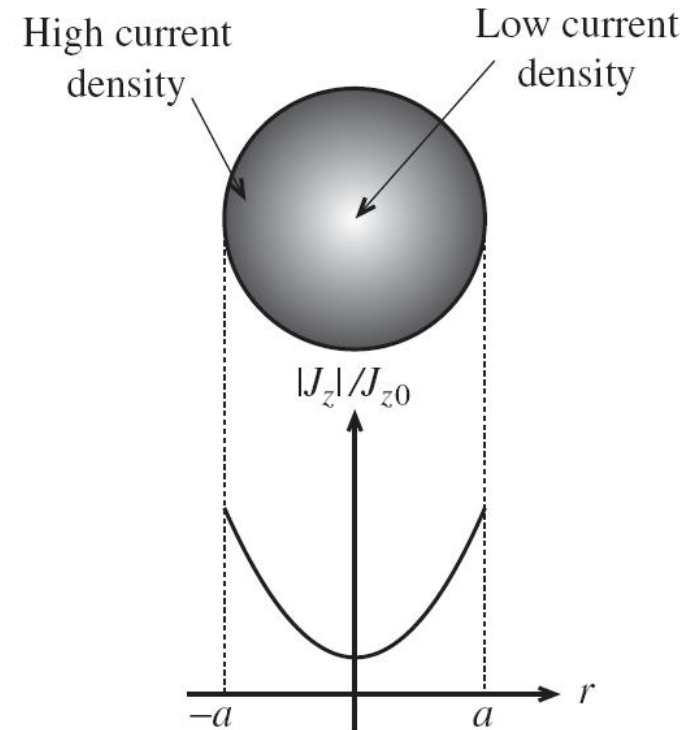


$$R_{DC} = \frac{l}{\pi a^2 \sigma_{cond}}$$

← **Length of cylinder**
↑ **Radius of cylinder** ← **conductivity**

RF Behavior of Resistors (contd.)

- At DC, current flows uniformly distributed over the entire conductor cross-sectional area.
- At AC, the alternating charge carrier flow establishes a magnetic field that induces an electric field (Faraday's Law) whose associated current density opposes the initial current flow → this effect is very strong at the center ($r=0$) where the impedance is substantially increased → as a result the current flow resides at the outer periphery with the increasing frequency.



DC Current Density:

$$J_{z0} = \frac{I}{\pi a^2}$$



Skin Effect

RF Behavior of Resistors (contd.)

- The current density at AC is given by:

$$J_z = \frac{pI}{2\pi a j \sqrt{r}} \exp\left(- (1+j) \frac{a-r}{\delta}\right)$$

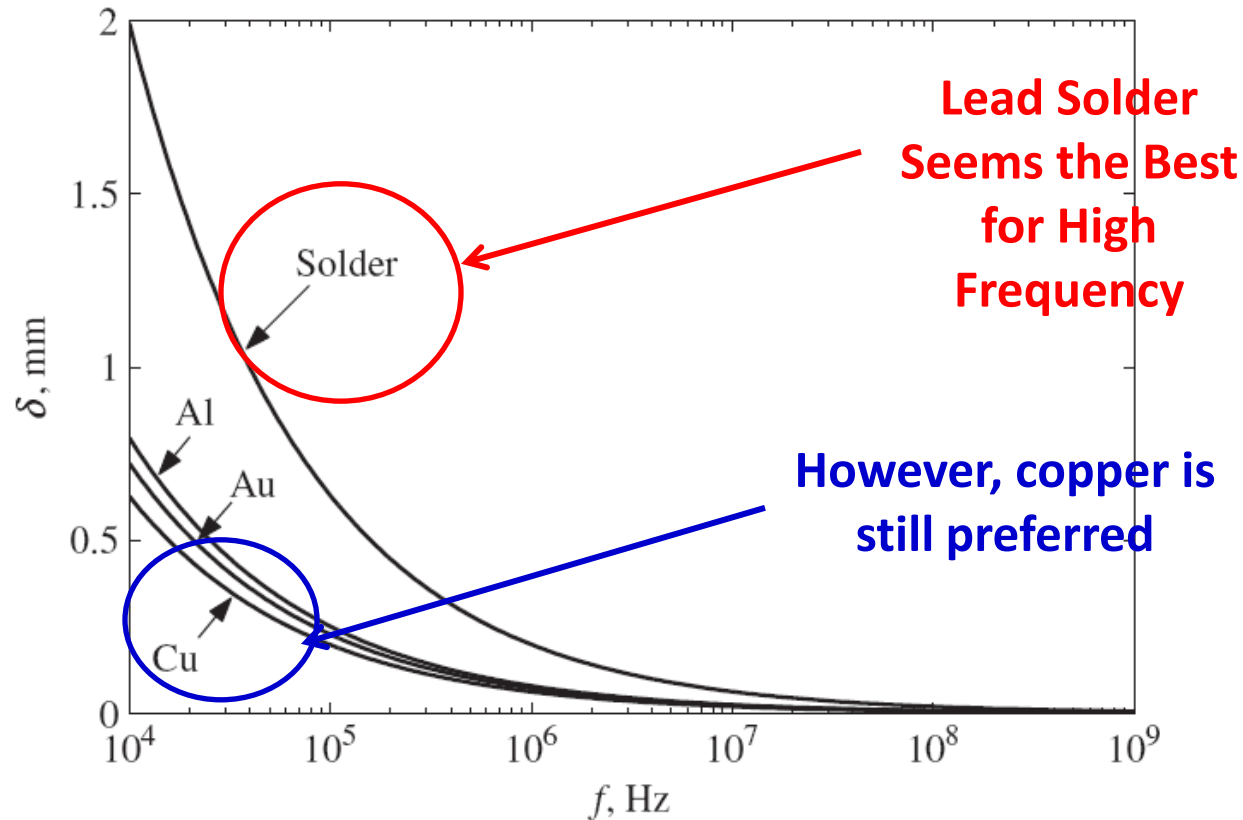
$$p^2 = -j\omega\mu\sigma_{cond}$$

$$\delta = \frac{1}{\sqrt{\pi f \mu \sigma_{cond}}}$$

Skin Depth

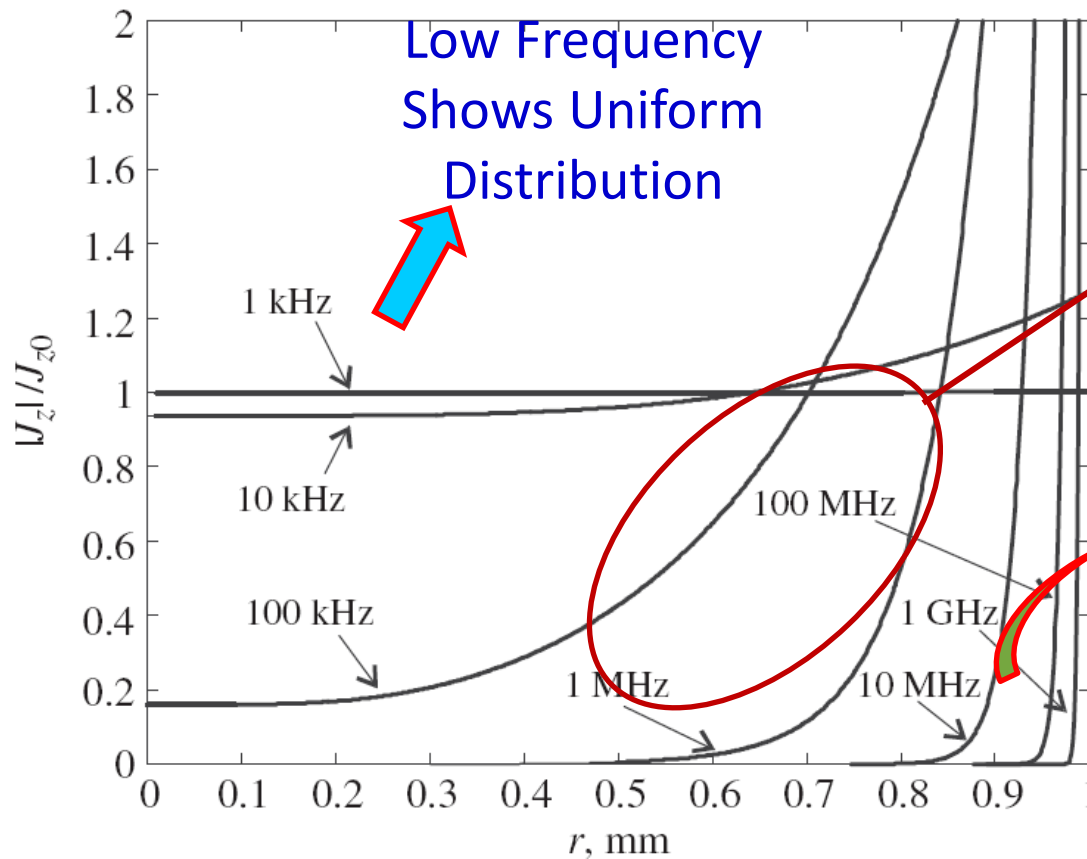
- J_z drops with decrease in r (proximity to the center)
- δ decreases with increase in frequency (skin depth from periphery reduces with increased frequency) → means the path for current conduction remains nearer to the periphery (skin effect) → means, current density towards center decreases with increase in frequency and increase in conductivity

RF Behavior of Resistors (contd.)



RF Behavior of Resistors (contd.)

Frequency sweep: For a fixed wire radius of $a = 1\text{mm}$, the plot $|J_z|/|J_{z0}|$ as a function of depth r :



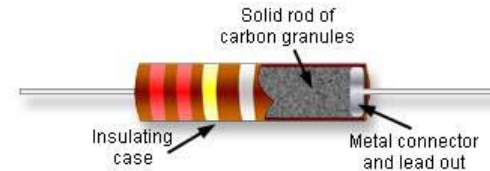
Medium to High
Frequency Pushes
the Current to the
Periphery

RF Sees Current
Restricted to
Surface

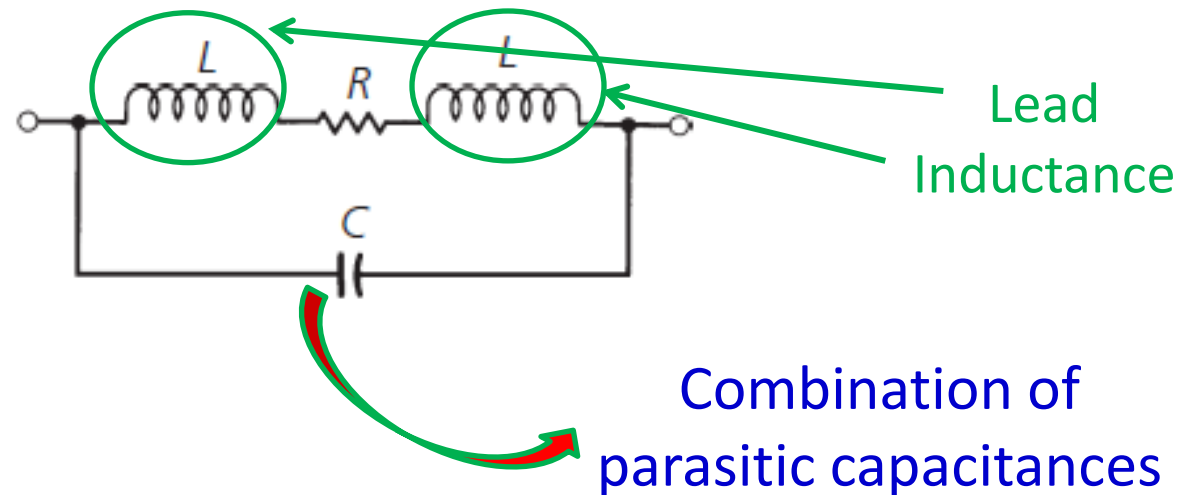
Resistors at High Frequencies

1. Carbon-composition resistors:

- Consists of densely packed dielectric particulates or carbon granules.
- **Between each pair of carbon granules is very small parasitic capacitor.**
- These parasitics, in aggregate, are significant → **primarily responsible for notoriously poor performance at high frequencies.**

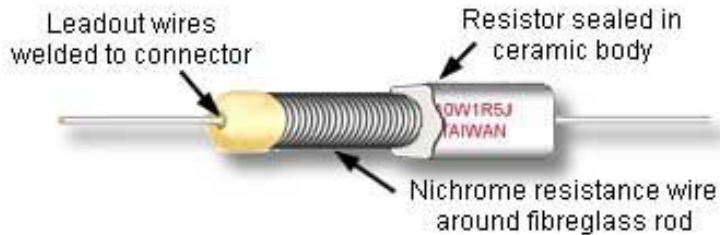


Equivalent Ckt Model:



Resistors at High Frequencies (contd.)

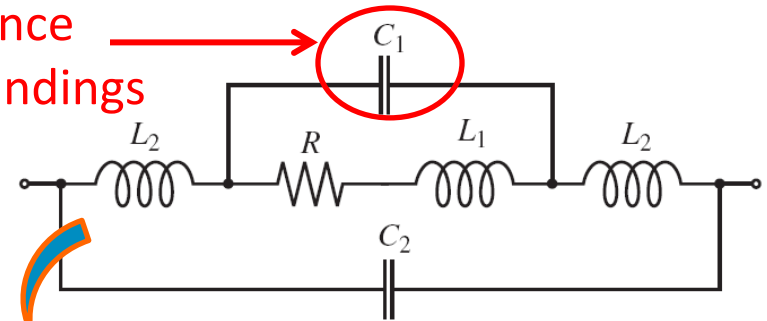
2. Wire-wound Resistors:



- Exhibit widely varying impedances over various frequencies.
- The inductor L is much larger here as compared to carbon-composition resistor.
- These resistors look like inductors \rightarrow impedances will increase with increase in frequency.
- At some frequency F_r , the inductance will resonate with shunt capacitance \rightarrow leads to decrease in impedance.

Equivalent Ckt Model:

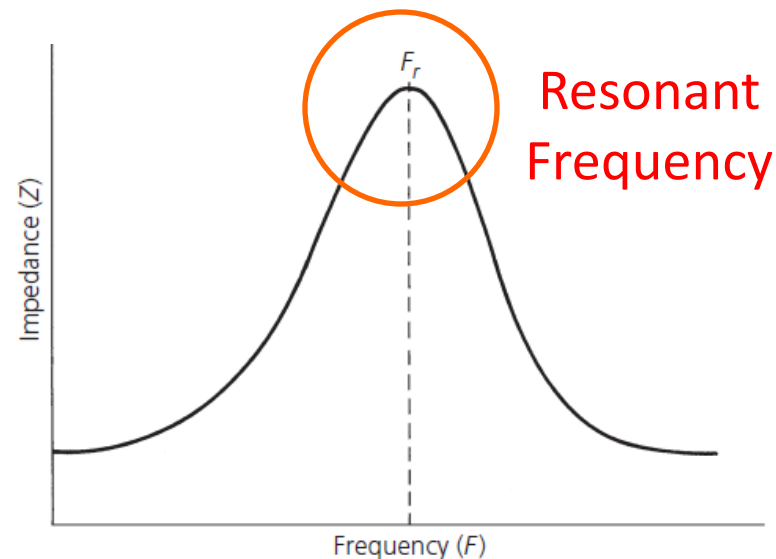
Capacitance
between Windings



L_2 : lead inductance

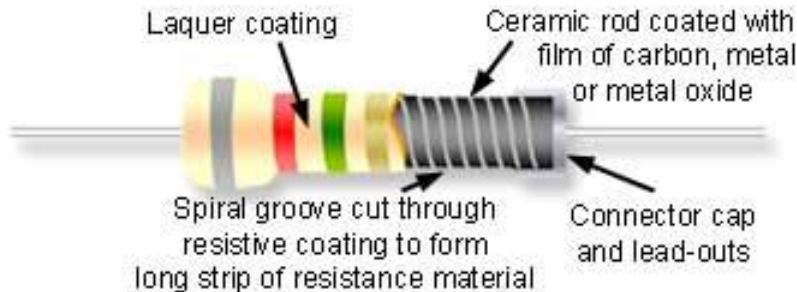
L_1 : inductance of resistive wires

C_2 : Interlead Capacitance

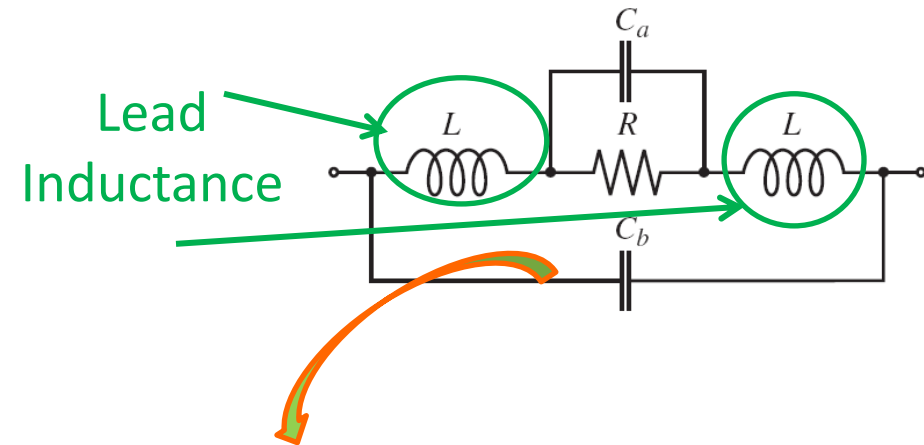


Resistors at High Frequencies (contd.)

3. Metal-film Resistors:



Equivalent Ckt Model:



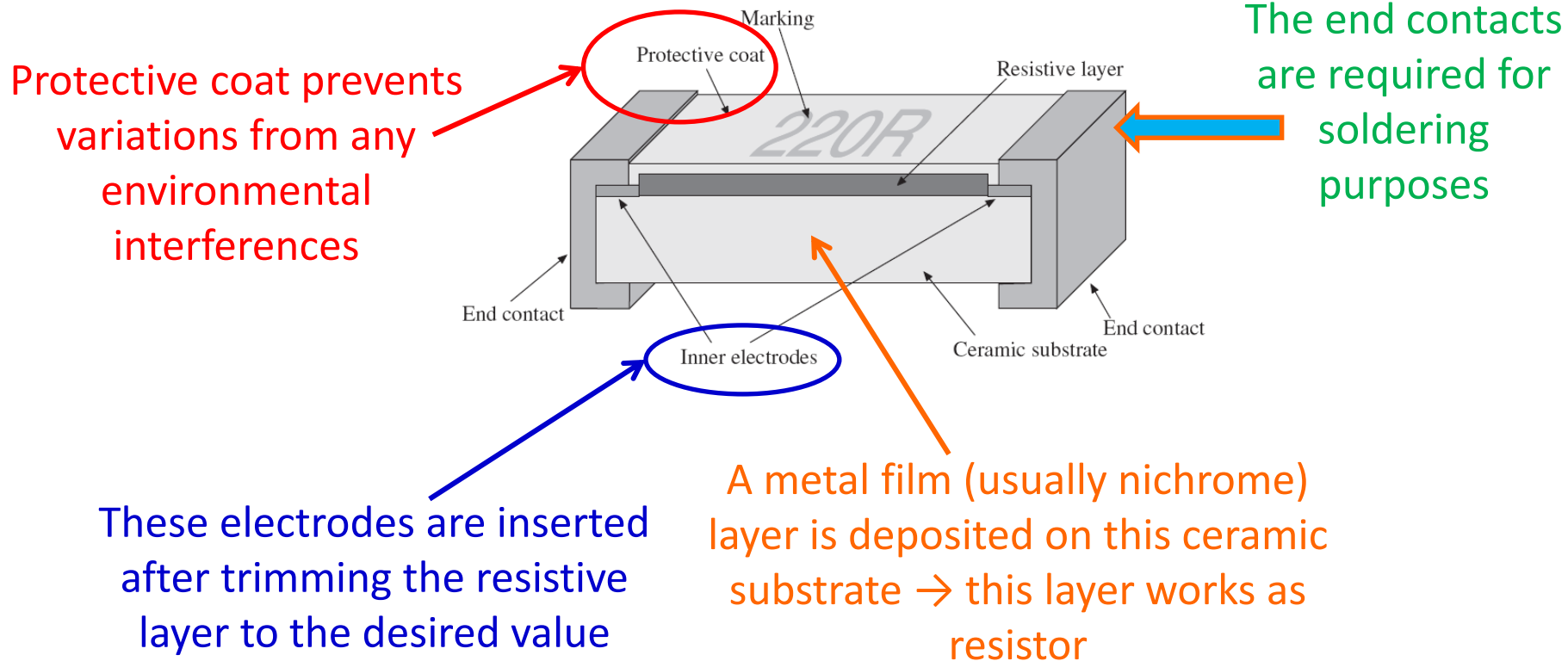
C_a models charge separation effects and C_b models interlead capacitance

- Seems to exhibit very good characteristics over frequency.
- Values of L and C are much smaller as compared to wire-wound and carbon-composition resistors.
- It works well up to 10 MHz → useful up to 100 MHz

Resistors at High Frequencies (contd.)

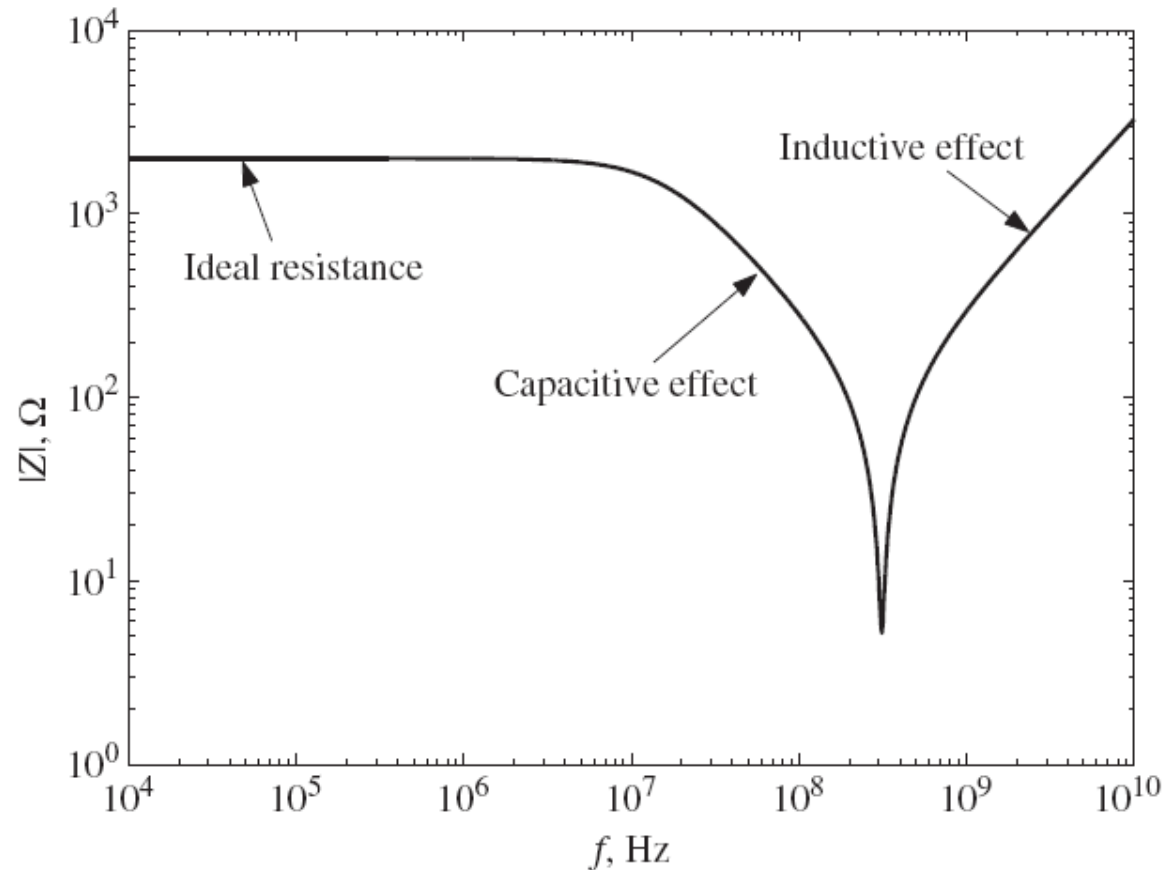
3. Thin-film Chip Resistors:

- The idea is to eliminate or reduce the stray capacitances associated with the resistors
- Good enough up to 2 GHz.



Resistors at High Frequencies (contd.)

What is the reason for following behavior of a 2000 Ω thin-film resistor?



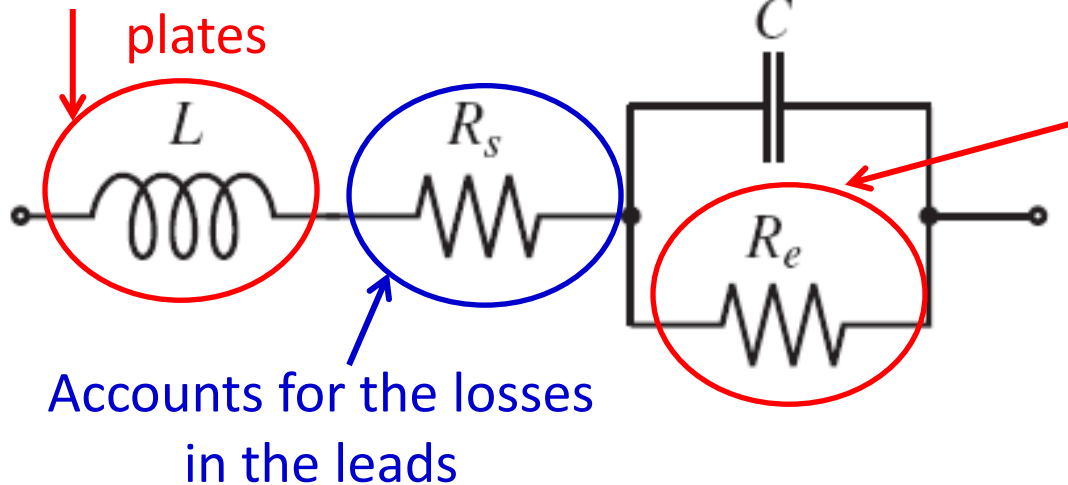
HW # 0

Demonstrate using either ADS or MATLAB

Capacitors at High Frequencies

Equivalent Circuit Representation of a Capacitor → for a parallel-plate

Inductance of the leads and
plates



Represents
Insulation
Resistance

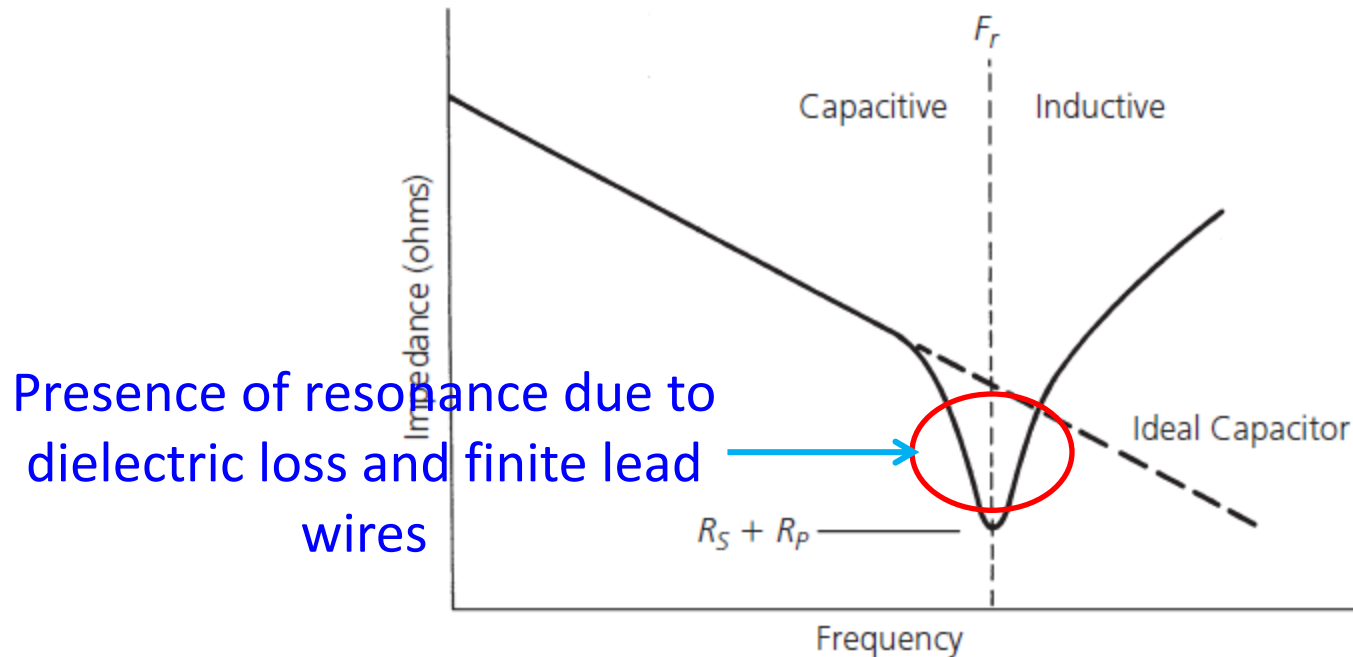
Accounts for the losses
in the leads

$$C = \frac{\epsilon A}{d} = \epsilon_0 \epsilon_r \frac{A}{d}$$

At high frequency, the dielectric become lossy i.e.,
there is conduction current through it

Then impedance of capacitor becomes
a parallel combination of C and
conductance G_e

Capacitors at High Frequencies (contd.)

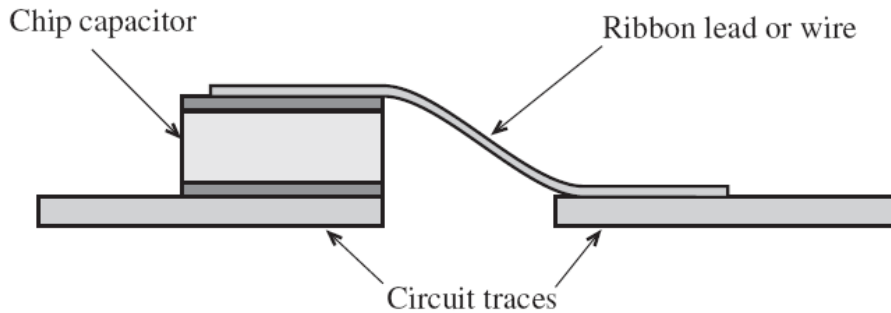


Presence of resonance due to dielectric loss and finite lead wires

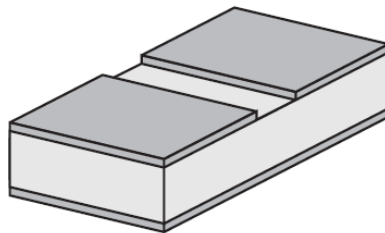
- Above F_r , the capacitor behaves as an inductor.
- In general, larger-value capacitors tend to exhibit more internal inductance than smaller-value capacitors.
- Therefore, it may happen that a $0.1\mu F$ may not be as good as a $300pF$ capacitor in a bypass application at $250 MHz$.
- The issue is due to significance of lead inductances at higher frequencies.

Capacitors at High Frequencies (contd.)

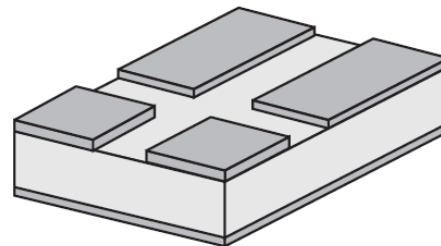
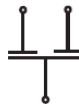
Chip Capacitors



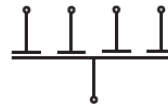
**Cross-section of a
single-plate capacitor
connected to the
board**



Dual capacitor

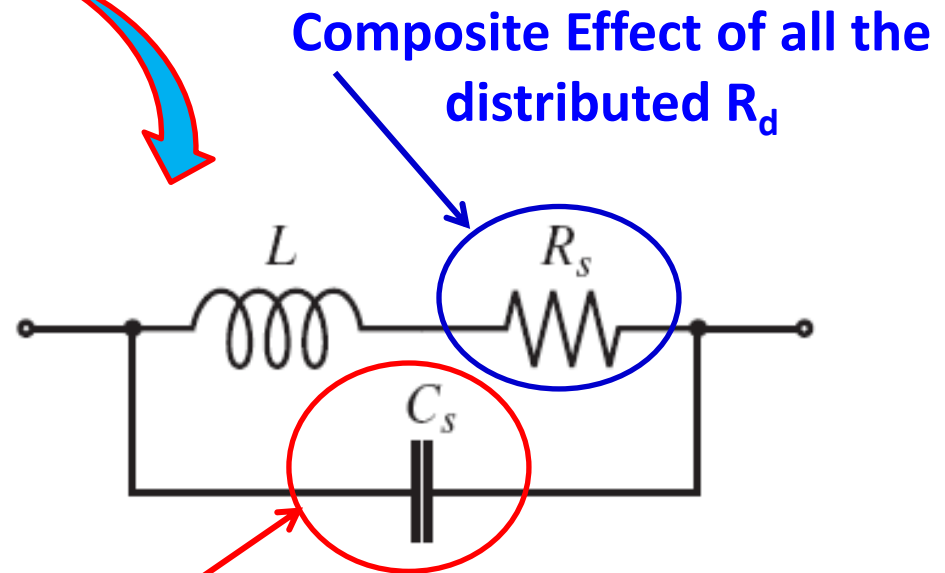
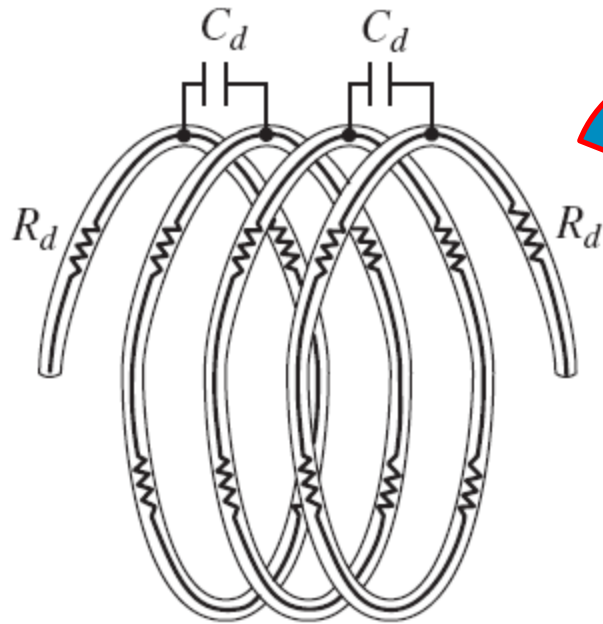


Quadrupole capacitor



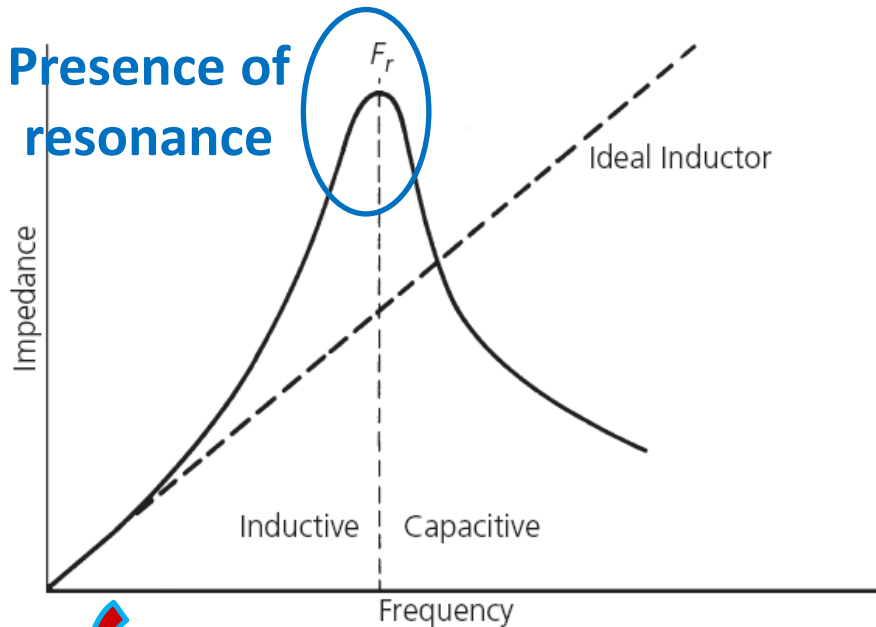
Inductors at High Frequencies

Equivalent Circuit Representation of an Inductor → coil type



**Composite Effect of all the
distributed C_d**

Inductors at High Frequencies (contd.)



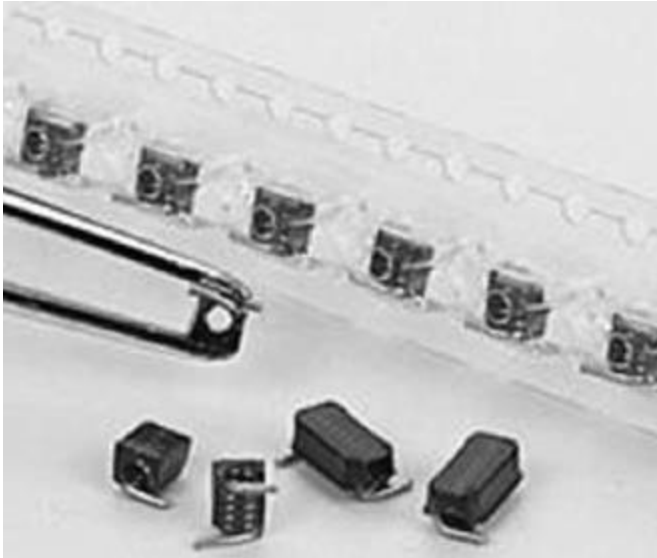
- Initially the reactance of inductor follows the ideal but soon departs from it and increases rapidly until it reaches a peak at the inductor's resonant frequency (F_r). **Why?**
- Above F_r , the inductor starts to behave as a capacitor.

Implement this in
MATLAB or ADS



HW#0

Chip Inductors



Surface mounted inductors still come as wire-wound coil → these are comparable in size to the resistors and capacitors