

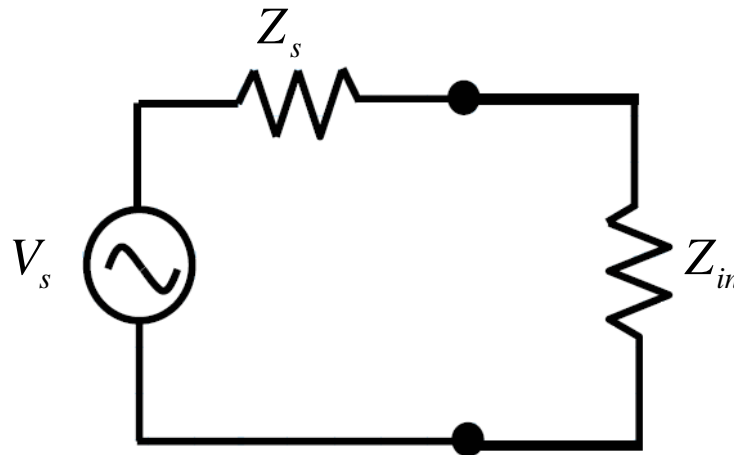
## **Lecture – 21**

**Date: 11.04.2016**

- Stability
- Transistor Amplifier Design
  - Maximum Gain Amplifier
  - The Ideal Gain Element
  - Design for Specified Gain

## Quiz – 6

- Solve the following two-port network to determine the maximum absorbed power by the input impedance  $Z_{in}$  or the maximum power delivered by the source ( $P_{avs}$ ) to the input impedance  $Z_{in}$



## Introduction

**Q:** So all there is to making a good RF/microwave amplifier is the design of proper **matching networks**?

**A:** There is one other problem that confronts the RF/microwave amplifier designer. That problem is **stability** (of the amplifier, not the designer).

An unstable amplifier is also known as an **oscillator**—a source of RF/microwave energy!

**Q:** Under what **conditions** will an amplifier oscillate?

**A:** An amplifier will go **unstable** if **either** of these two conditions are true:

$$|\Gamma_{out}| = \left| S_{22} + \frac{S_{12}S_{21}\Gamma_s}{1 - S_{11}\Gamma_s} \right| > 1.0$$

$$|\Gamma_{in}| = \left| S_{11} + \frac{S_{12}S_{21}\Gamma_L}{1 - S_{22}\Gamma_L} \right| > 1.0$$

In other words, the amplifier will oscillate if either the input or output reflection coefficient of the gain element has a **magnitude greater than one**.

## Introduction

**Q:** Hey wait! I thought we learnt that the **maximum** value of any reflection coefficient magnitude was 1 (i.e.,  $\Gamma \leq 1.0$ ) → this defined the **validity region** of our Smith Chart!

**A:** Remember, the inequality  $\Gamma \leq 1.0$  is true for any **passive** load or device. Our gain element is an **active** device → it must have a DC source of power → As a result, we find that  $\Gamma > 1.0$  is quite **possible**!

**Q:** But, we learnt that the region outside the  $\Gamma = 1.0$  circle on the Smith Chart corresponded to loads with negative **values of resistance**. Does this mean that  $Z_{in}$  or  $Z_{out}$  could have real (i.e. resistive) components that are **negative**?

**A:** That's **exactly** what it means!

**Q:** What is a negative resistor exactly?

**A:** Ohm's law still applies. **However**, the current through a negative resistor is  $180^\circ$  **out-of-phase** with the voltage across it.

The resistor current is at its minimum value when the voltage across it is at its maximum —and **vice versa**!

## Stability

- This behavior (**the occurrence of negative resistance**) drives our amplifier circuit a little **wacky**, and it begins to oscillate!
- Then the question is – how to avoid such an unfortunate occurrence?
- Remember, the amplifier instability occurs when:

$$|\Gamma_{out}| = \left| S_{22} + \frac{S_{12}S_{21}\Gamma_s}{1 - S_{11}\Gamma_s} \right| > 1.0$$

$$|\Gamma_{in}| = \left| S_{11} + \frac{S_{12}S_{21}\Gamma_L}{1 - S_{22}\Gamma_L} \right| > 1.0$$

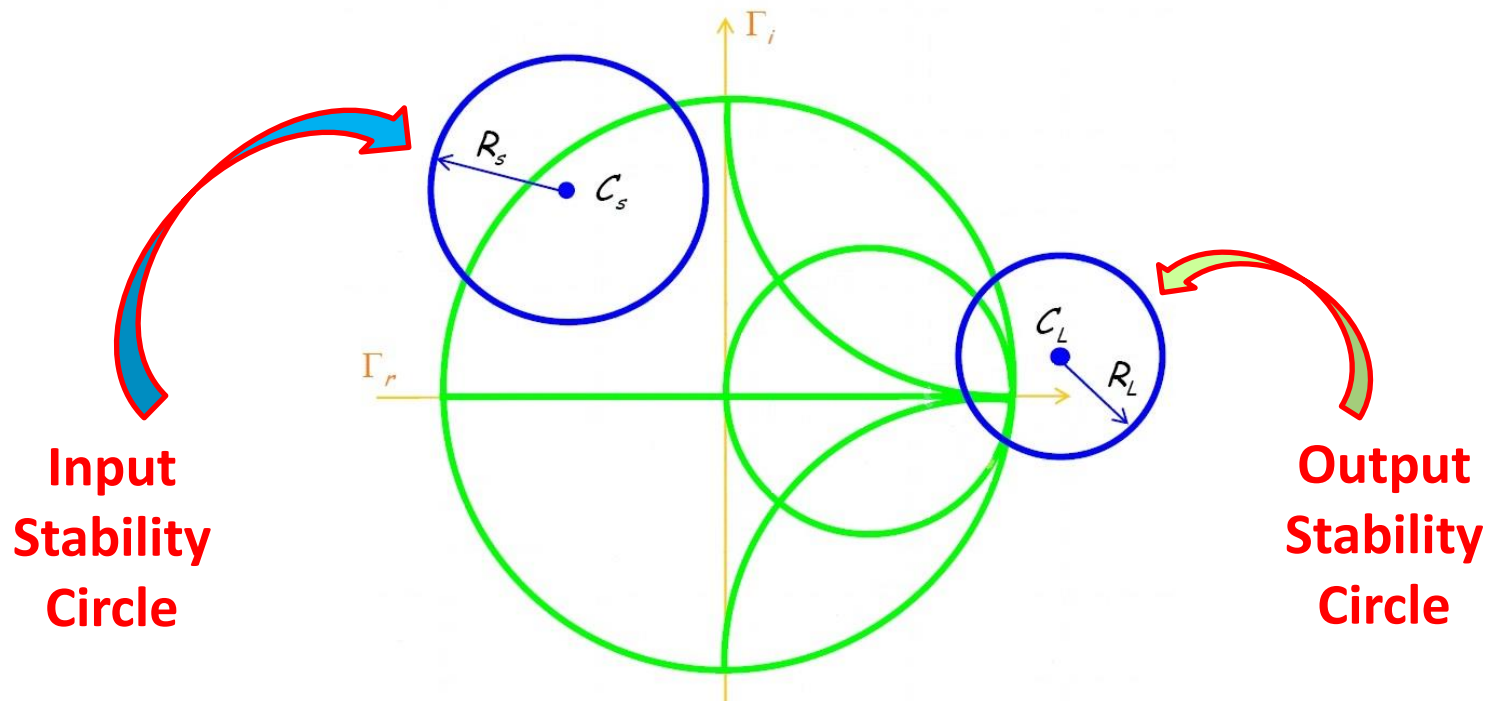
Thus, for a **given** gain element (i.e.,  $S_{11}$ ,  $S_{21}$ ,  $S_{22}$ ,  $S_{12}$ ), the amplifier stability is determined by the value of  $\Gamma_L$  and  $\Gamma_s$

We can **solve** these equations to determine the specific range of values of  $\Gamma_L$  and  $\Gamma_s$  that will **induce oscillation**.

We find that these unstable values—when plotted on the **complex  $\Gamma$  plane**—form a circle. These circles are known as a **stability circles**.

## Stability (contd.)

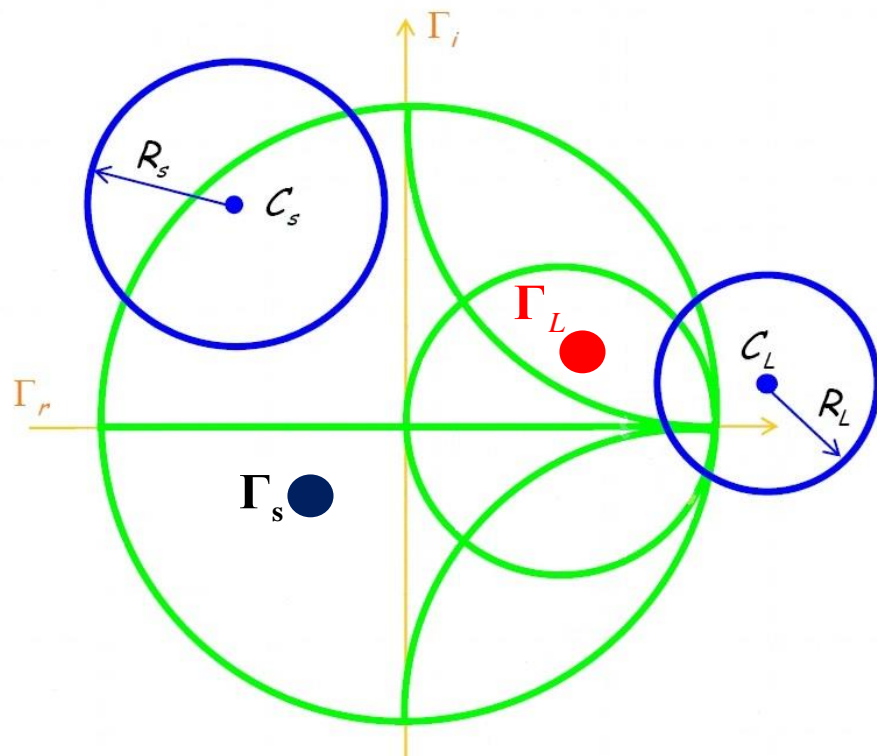
- These gain circles are defined in terms of a complex value  $C$ , which specifies the location of the stability circle **center** on the complex  $\Gamma$  plane, and a real value  $R$ , which specifies the **radius** of the stability circle.
- There is **one** stability circle for  $\Gamma_L$  (i.e.,  $C_L$  and  $R_L$ ) and **another** for  $\Gamma_s$  (i.e.,  $C_s$  and  $R_s$ ). Typically, the  $\Gamma$  values that lie **inside** the stability circle will create amplifier oscillation.



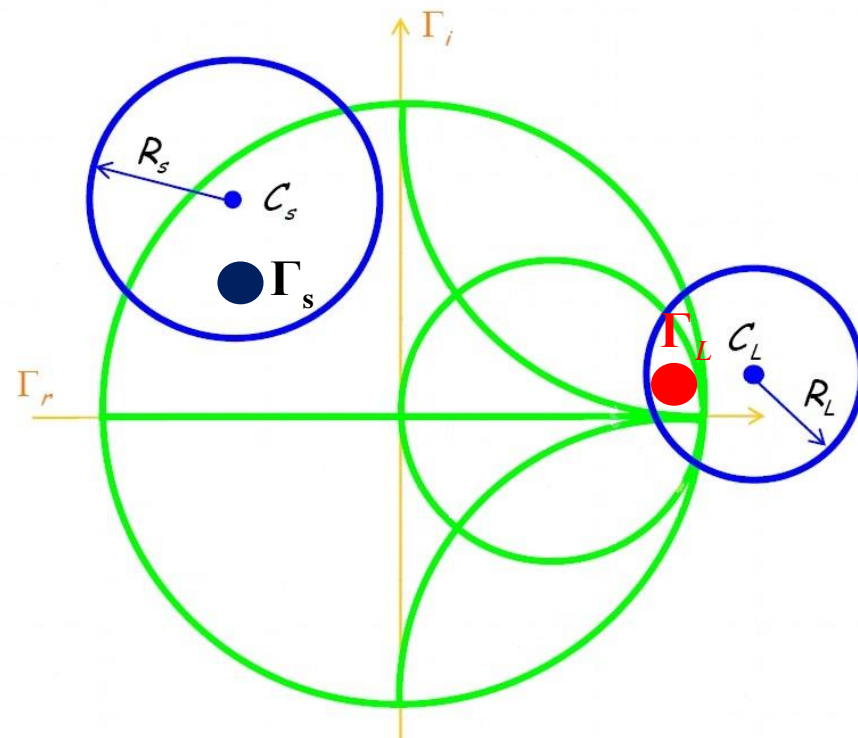
## Stability (contd.)

**Q:** So what do we **use** these stability circles for?

**A:** As an amplifier designer, we must make sure that our **design values**  $\Gamma_L$  and  $\Gamma_s$  lie **outside** these circles—otherwise, our well-designed amplifiers will **oscillate**!



A Stable Design



An Unstable Design

## Stability (contd.)

**Q:** Yikes! Must we **always** determine these circles and check our design for instability?

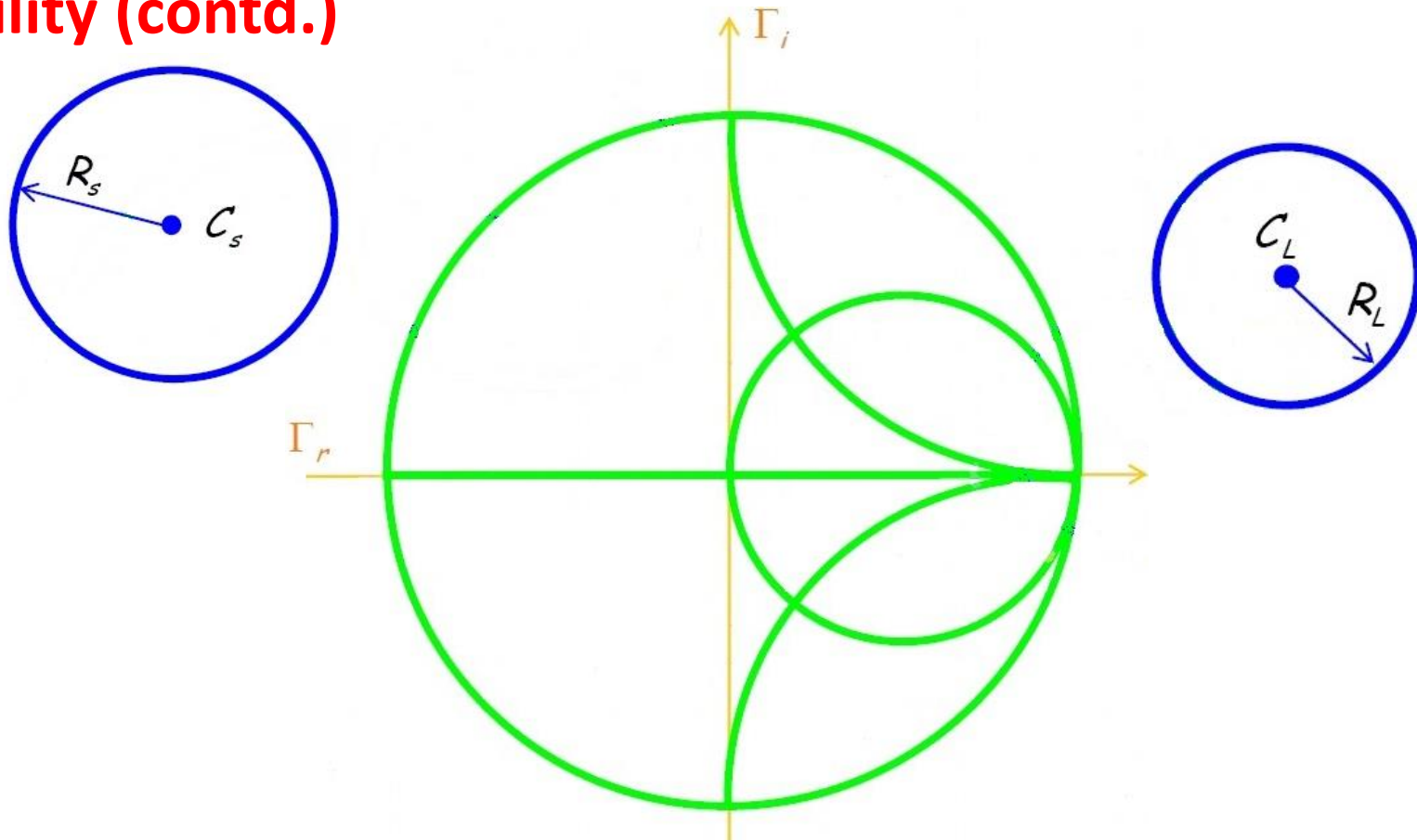
**A:** Not necessarily! Some gain elements are **unconditionally stable**. As the name suggests, these gain elements result in stable amplifiers for any and all **realizable** values of  $\Gamma_L$  and  $\Gamma_S$ .

**Q:** So an unconditionally stable gain element has stability circles with **zero radius** (i.e.,  $R = 0$ )?

**A:** **Could** be, but all that is required for a gain element to be unconditionally stable is for its stability circles to lie completely **outside** the  $\Gamma = 1$  circle (i.e., the Smith chart)



## Stability (contd.)



### An Unconditionally Stable Gain Element

For this condition, we find that the values of  $\Gamma_L$  and  $\Gamma_s$  that result in an unstable amplifier must have a magnitude **greater than 1** (i.e.,  $\Gamma_L > 1$  or  $\Gamma_s > 1$ )

## Stability (contd.)

Obviously, it is always assumed that the loads and sources attached to amplifier will **always** have **positive** resistances, such that  $\Gamma_L < 1$  and  $\Gamma_s < 1$ .

Therefore, an **amplifier** constructed with an unconditionally stable gain element will be **unconditionally stable**!

**Q:** How will I **recognize** an unconditionally stable gain element if I see one? Must I determine and plot the stability circles?

**A:** There are three **tests** that we can apply—using the scattering parameters  $S_{11}$ ,  $S_{21}$ ,  $S_{22}$ ,  $S_{12}$  — to **directly** determine if a gain element is unconditionally stable.

## Stability (contd.)

### Test-1

Check the S-matrix of the gain element and check the following condition. The **necessary conditions** for a gain element to be unconditionally stable are:


$$|S_{11}| < 1.0$$

$$|S_{22}| < 1.0$$

However, this gives unconditional stability to only **unilateral** gain element (i.e.,  $S_{12} = 0$  or approx.  $|S_{12}| \ll |S_{21}|$ )

Otherwise there will be always situations when  $\Gamma_{in} > 1$  and  $\Gamma_{out} > 1$ , leading to instability as can be seen in the following expressions:

$$|\Gamma_{out}| = \left| S_{22} + \frac{S_{12}S_{21}\Gamma_s}{1 - S_{11}\Gamma_s} \right| > 1.0$$

$$|\Gamma_{in}| = \left| S_{11} + \frac{S_{12}S_{21}\Gamma_L}{1 - S_{22}\Gamma_L} \right| > 1.0$$

Therefore, (for  $S_{12} \neq 0$ ) we find that our gain element must pass **two more tests**

## Stability (contd.)

### Test-2

Alternatively, it can be shown that the amplifier will be unconditionally stable if the following conditions are met:

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2}{2|S_{12}S_{21}|} > 1.0$$

and

$$|\Delta| < 1.0$$

Where, **K** is called the **Rollett Factor** and **Δ** is the determinant of the S-matrix

### Test-3

Furthermore, the amplifier can be shown to be unconditionally stable if the following condition holds true:

$$\mu = \frac{1 - |S_{11}|^2}{|S_{22} - S_{11}^* \Delta| + |S_{12}S_{21}|} > 1.0$$

Larger values of  $\mu$  imply  
greater stability

Ref: M. L. Edwards and J. H. Sinsky, "A New Criteria for Linear 2-Port Stability Using a Single Geometrically Derived Parameter," IEEE Trans. Microwave Theory and Tech., Vol. 40, Dec. 1992

## Example

$$S_{11} = 0.869 \angle -159^\circ,$$

$$S_{12} = 0.031 \angle -9^\circ,$$

$$S_{21} = 4.250 \angle 61^\circ,$$

$$S_{22} = 0.507 \angle -117^\circ.$$



$$|\Delta| = |S_{11}S_{22} - S_{12}S_{21}| = 0.336,$$

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2}{2|S_{12}S_{21}|} = 0.383$$

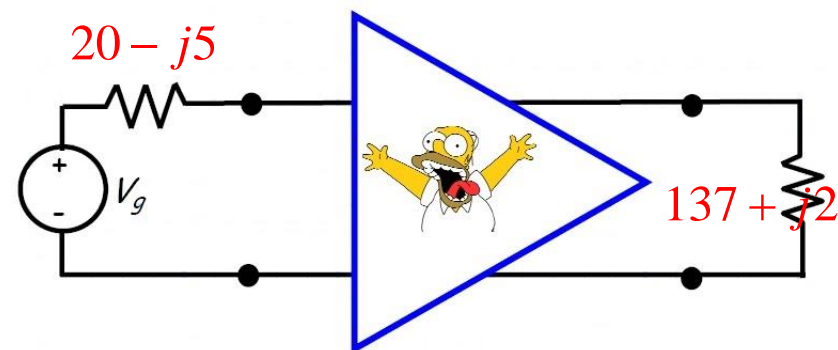
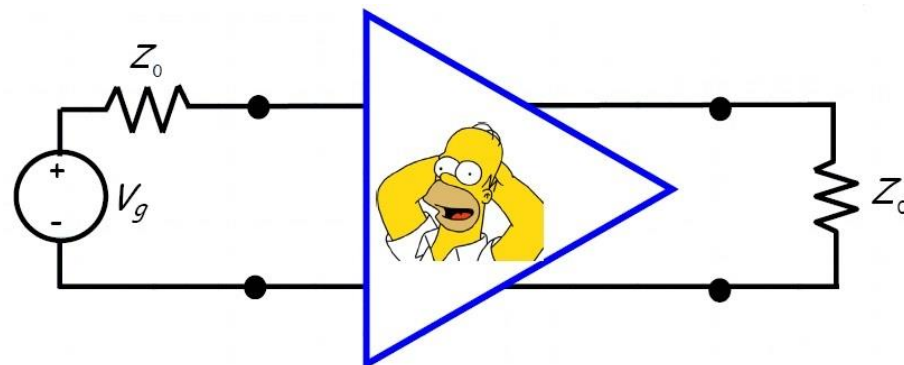
Potentially Unstable !

$$\mu = 0.678$$

## Stability (contd.)

**Q:** Do we really need to **care** if our design is unconditionally stable? Aren't we really **just** concerned with whether our design values  $\Gamma_L$  and  $\Gamma_s$  lie inside the stability circle?

**A:** Remember, the values  $\Gamma_L$  and  $\Gamma_s$  are determined for the **specific** values of source and load impedances connected to the amplifier (**presumably**  $Z_0$ ).



- But what if the resulting amplifier is **not** connected to these ideal impedances? The ideal source or load impedance  $Z_0$  is **never** achieved with **perfection**, and often achieved **not at all** (consider all the **narrow-band** devices we have studied!).

**We do not specifically** know what source and load impedances our amplifier might encounter, we have to generally design an amplifier that is stable for them **all**—one that's **unconditionally stable**!

## Stability (contd.)

**Q:** Anything **else** we need to know about amplifier stability?

**A:** One last **very** important thing → Recall that amplifiers, like all microwave devices, are **dependent on frequency**. Thus, all of the important values involved in our design (e.g.,  $S_{11}$ ,  $S_{21}$ ,  $S_{22}$ ,  $S_{12}$ ,  $\Gamma_L$  and  $\Gamma_s$ ) will **change** as a function of frequency!

**Q:** I see, amplifier performance, most notably **gain**, will change as a function of frequency, and so maximum power transfer will occur at just our **design frequency** → We've seen this kind of thing **before**!

**A:** **True**, but for amplifiers there is also a **new** twist → The amplifier stability conditions (i.e., stability tests) must be satisfied at **any and all frequencies**!

## Stability (contd.)

- If for **even one frequency** we find that either:

$$|\Gamma_{out}| = \left| S_{22} + \frac{S_{12}S_{21}\Gamma_s}{1 - S_{11}\Gamma_s} \right| > 1.0$$

or

$$|\Gamma_{in}| = \left| S_{11} + \frac{S_{12}S_{21}\Gamma_L}{1 - S_{22}\Gamma_L} \right| > 1.0$$

→ then our amplifier will **oscillate—even** if that frequency is **not** our “design frequency”!

This makes amplifier stability a much more **significant** and **difficult** problem than you might otherwise think.

An unconditionally stable amplifier must be unconditionally stable at **all frequencies**!

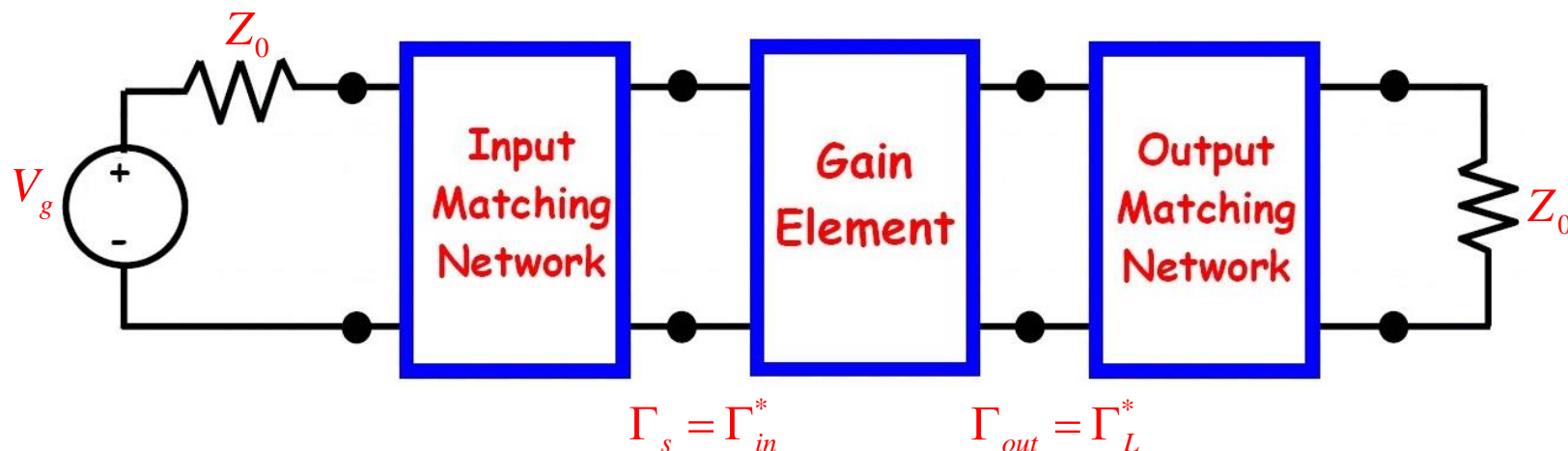


## Transistor Amplifier Design

**Q:** What happens if we don't like the resulting transducer gain? How can we identify a more suitable gain element?

**Q:** Since we are using lossless matching networks, won't our resulting device be relatively narrow band? How can we increase the bandwidth of our design?

## Maximum Gain Amplifiers



**Q:** If we design our amplifier such that the source is **matched** to the input of the gain element, and the output of the gain element is **matched** to the load, what **is** the resulting gain?

- If the amplifier is a **unilateral** amplifier ( $S_{12} \ll S_{21}$ ), where:

$$\Gamma_{in} = S_{11} \quad \Gamma_{out} = S_{22}$$

- Then the transducer gain is called **unilateral transducer gain**:

$$G_{TU} = \frac{(1 - |\Gamma_s|^2) |S_{21}|^2 (1 - |\Gamma_L|^2)}{(|1 - \Gamma_s S_{11}|^2) (|1 - \Gamma_L S_{22}|^2)}$$

## Maximum Gain Amplifiers (contd.)

- Inserting the **matched conditions** in the transducer gain expressions we get:

$$G_{TU \max} = \frac{1}{1 - |\Gamma_s|^2} |S_{21}|^2 \frac{1 - |\Gamma_L|^2}{|1 - \Gamma_L S_{22}|^2}$$

$$G_{TU \max} = \frac{1}{1 - |\Gamma_s|^2} |S_{21}|^2 \frac{1}{1 - |\Gamma_L|^2} = \frac{1}{1 - |S_{11}|^2} |S_{21}|^2 \frac{1}{1 - |S_{22}|^2}$$

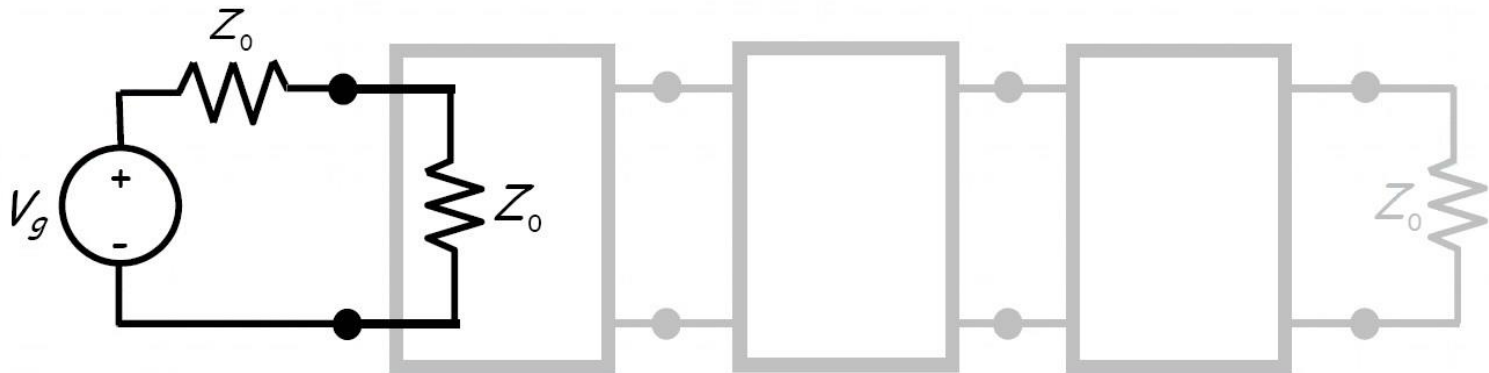
These of course are the **maximum** transducer gain possible, **given** a specific gain element, and a source and load impedance of  $Z_0$

## Maximum Gain Amplifiers (contd.)

**Q:** What about the **scattering matrix** of the **amplifier**? Can we determine the scattering parameters of the resulting amplifier?

**A:** We can certainly determine their **magnitude**!

- First of all, remember that if a matching network establishes a match at its **output**, then a match is likewise present at its **input**.
- As a result, we know that the input impedance of the input matching network must be  $Z_0$ :

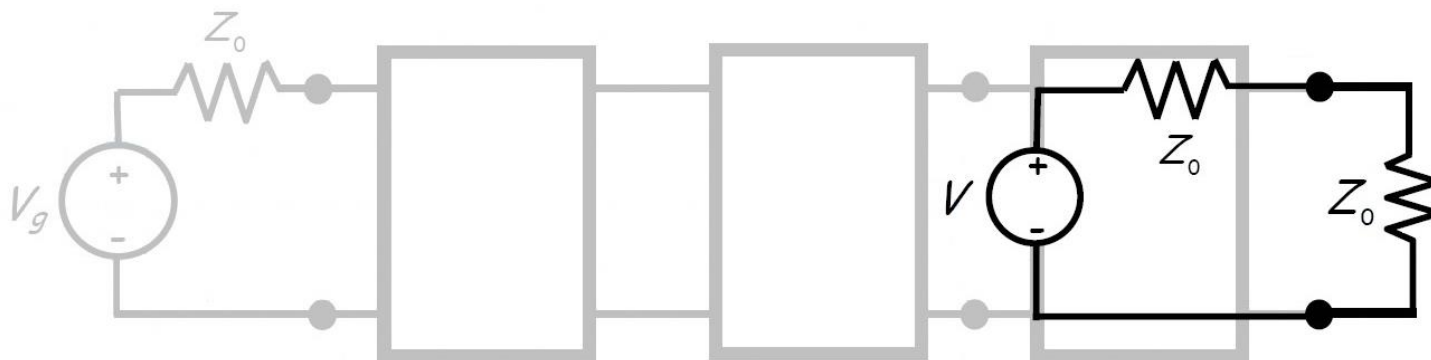


- Meaning that the scattering parameter  $S_{11}$  of the matched amplifier is **zero**!

$$S_{11}^{amp} = 0$$

## Maximum Gain Amplifiers (contd.)

- Likewise, the output impedance of the output matching network must be also be  $Z_0$ :



- As a result, the scattering parameter  $S_{22}$  of the matched amplifier is also **zero!**

$$S_{22}^{amp} = 0$$

- Now, since both ports of the amplifier are matched, we can determine that the magnitude of the **amplifier** scattering parameter  $S_{21}$  is simply the transducer gain  $G_{Tmax}$ .

S-parameters are  
those of gain element

$$|S_{21}^{amp}| = G_{TU \max} = \frac{1}{1 - |\Gamma_s|^2} |S_{21}|^2 \frac{1 - |\Gamma_L|^2}{|1 - \Gamma_L S_{22}|^2}$$

## Maximum Gain Amplifiers (contd.)

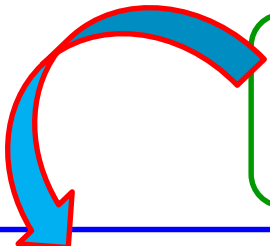
- Similarly, we can conclude the remaining scattering parameter:

$$|S_{12}^{amp}| = \frac{1}{1 - |\Gamma_L|^2} |S_{12}|^2 \frac{1 - |\Gamma_s|^2}{|1 - \Gamma_s S_{11}|^2}$$

Note that **if** the gain element is **unilateral**, then so too will be the **amplifier**!

## The Ideal Gain Element

- Recall that the maximum possible transducer gain, **given a specific gain element**, and a source and load impedance of  $Z_0$  is:


$$G_{T \max} = \frac{1}{1 - |\Gamma_s|^2} |S_{21}|^2 \frac{1 - |\Gamma_L|^2}{|1 - \Gamma_L S_{22}|^2}$$

This is achieved by properly constructing input and output matching networks  $\rightarrow$  it's the largest value that we can get for **that particular gain element**

**Q:** But what if this gain is **insufficient**?

**A:** In that case we must **change the gain element**, but what should we change the gain element to? What are the characteristics of an **ideal gain element**?

- The answers to these questions are best determined by examining the maximum **unilateral** transducer gain:

$$G_{TU \max} = \frac{1}{1 - |S_{11}|^2} |S_{21}|^2 \frac{1}{1 - |S_{22}|^2}$$

## The Ideal Gain Element (contd.)

- Recall that for most gain elements,  $S_{12}$  is small (i.e., approximately unilateral), and in fact  $S_{12} = 0$  is **one** ideal characteristic of an **ideal gain element**.
- From the maximum unilateral gain expression, we can determine the remaining **ideal characteristics** of a gain element. Some of these results are rather **self evident**, but others are a bit **surprising**!
- For example, it is clear that **gain** is increased as  $S_{21}$  is **maximized**—no surprise here. What might catch you off guard are the conclusions we reach when we observe the **denominator** of  $G_{TUmax}$

$$G_{TUmax} = \frac{1}{1 - |S_{11}|^2} |S_{21}|^2 \frac{1}{1 - |S_{22}|^2}$$

It appears that the gain will go to **infinity** if  $|S_{11}| = 1$  and/or  $|S_{22}| = 1$ !

**Q:** But that would mean the input and/or output impedance of the gain element is **purely reactive** (e.g. and open or a short). Is this conclusion **accurate**?

**A:** Yes and No.



## The Ideal Gain Element (contd.)

$$G_{TU \max} = \frac{1}{1 - |S_{11}|^2} |S_{21}|^2 \frac{1}{1 - |S_{22}|^2}$$

It appears that the gain will go to **infinity** if  $|S_{11}| = 1$  and/or  $|S_{22}| = 1$ !

Remember, this maximum gain is achieved when we establish a **conjugate match**. The equation above says that this maximum gain will increase to infinity if we match to a **reactive** input/output impedance.

And **that's** the catch.

It is **impossible** to match  $Z_0$  to load that is purely reactive!

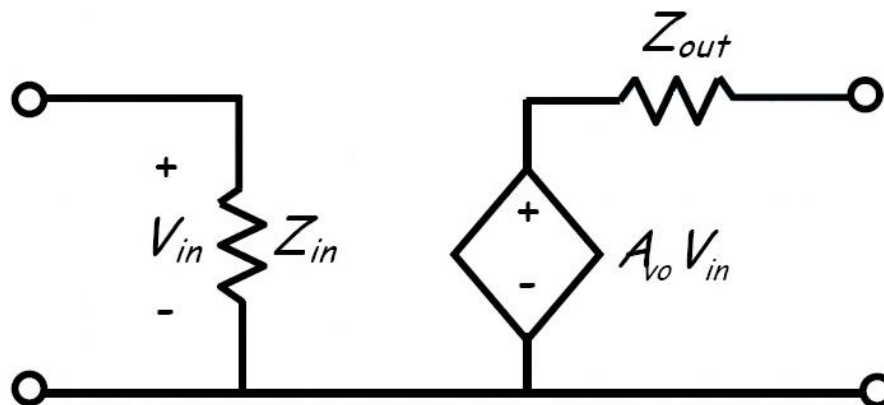
- Even otherwise, for maximum power absorption we can only match to an impedance that has a **non-zero resistive component** (i.e.,  $\Gamma < 1$ ); else, there's no way for the available power to be **absorbed**!
- Still, it is quite evident that—all other things being equal—a **gain element** with **larger values** of  $|S_{11}|$  and  $|S_{22}|$  will produce **more gain** than **gain elements** with **smaller values**  $|S_{11}|$  and  $|S_{22}|$

## The Ideal Gain Element (contd.)

**Q:** This seems very **counter intuitive**; I would think that an inherently **better-matched** gain element (e.g.,  $|S_{11}| \approx 0$  and  $|S_{22}| \approx 0$ ) would provide **more gain**.

**A:** Recall you studied **four types** of amplifier (gain element) models in Analog Circuits: voltage gain, current gain, trans-impedance, and transconductance. Each of these amplifiers were likewise characterized in terms of **input impedance** and **output impedance**.

- Recall also that for each of these models, the **ideal** values of input/output impedance was **always** either zero (a short) or infinity (an open)!
- In other words, **ideal** amplifiers (**gain elements**) always need to have  $|S_{11}| = |S_{22}| = 0$ !



Ideally:

$|Z_{in}|$  very small

$|Z_{out}|$  very small

$|A_{vo}|$  very small

## The Ideal Gain Element (contd.)

- However take example of an **ideal voltage amplifier**: it has a **high input** impedance ( $|S_{11}| \approx 1$ ) and a **low output** impedance ( $|S_{22}| \approx 1$ ). If we construct matching networks on either side of this ideal gain element, the result is an amplifier with **very** high transducer gain !

**Q:** So how do we “**change**” a gain element to a **more ideal** one?

**A:** Of course we could always select a **different** transistor, but we could also simply change the **DC bias** of the transistor we are using!

- Recall the **small-signal parameters** (and thus the scattering parameters) of a transistor change as we modify the **DC bias** values. We can select our DC bias such that the value of  $G_{TUmax}$  **is maximized**.

**Q:** Is there any **downside** to this approach?

**A:** Absolutely! Recall that we can theoretically match to a very low or very high resistance—at precisely **one frequency**! But we found that the resulting match will typically be **extremely narrowband** for these cases.

Thus, we might consider **reducing** the amplifier gain (i.e., reducing the values  $|S_{11}|$  and  $|S_{22}|$ ), in return for achieving a more moderate gain over a **wider frequency bandwidth**!

Additionally, DC bias likewise affects **other** amplifier characteristics, including compression points and noise figure and therefore absolute care is must!

## Design for Specified Gain

- The **conjugate matched** design of course **maximizes** the transducer gain of an amplifier. But there are times when wish to design an amplifier with **less** than this maximum possible gain!

**Q:** Why on Earth would we want to design such a **sub-optimal** amplifier?

**A:** A general characteristic about amplifiers is that we can always trade **gain** for **bandwidth** (the gain-bandwidth product is an approximate **constant!**). Thus, if we desire a **wider** bandwidth, we must **decrease** the amplifier gain.

**Q:** Just **how** do we go about doing this?

**A:** We simply design a “matching” network that is actually **mismatched** to the gain element. We know that the **maximum** transducer gain will be achieved if we design a matching network such that:

$$\Gamma_{in} = \Gamma_{in}^* \quad \Gamma_L = \Gamma_{out}^*$$

- Thus, a **reduced gain** (and so wider bandwidth) amplifier must have the characteristic such that:

$$\Gamma_{in} \neq \Gamma_{in}^* \quad \Gamma_L \neq \Gamma_{out}^*$$

## Design for Specified Gain (contd.)

- Specifically, we should select  $\Gamma_s$  and  $\Gamma_L$  (and then design the matching network) to provide the **desired** transducer gain  $G_T$ :

$$G_T = \frac{(1 - |\Gamma_s|^2) |S_{21}|^2 (1 - |\Gamma_L|^2)}{(|1 - \Gamma_s \Gamma_{in}|^2) (|1 - \Gamma_L S_{22}|^2)} < G_{T_{\max}}$$

It is apparent that there are **many values** of  $\Gamma_s$  and  $\Gamma_L$  that will provide this sub-optimal gain.

**Q:** So **which** of these values do we choose?

**A:** We choose the values of  $\Gamma_s$  and  $\Gamma_L$  that satisfies the above equation, **and** has the **smallest** of all possible magnitudes of  $|\Gamma_s|$  and  $|\Gamma_L|$

- Remember— **smaller**  $|\Gamma|$  leads to **wider** bandwidth!
- This design process is much easier if the gain element is **unilateral**. Recall for that case we find that the transducer gain is:

$$G_{TU} = \frac{(1 - |\Gamma_s|^2) |S_{21}|^2 (1 - |\Gamma_L|^2)}{(|1 - \Gamma_s S_{11}|^2) (|1 - \Gamma_L S_{22}|^2)}$$

We can write this as a product of three terms

$$G_{TU} = G_S G_0 G_L$$

## Design for Specified Gain (contd.)

Where:

$$G_s = \frac{1 - |\Gamma_s|^2}{|1 - \Gamma_s S_{11}|^2}$$

$$G_0 = |S_{21}|^2$$

$$G_L = \frac{1 - |\Gamma_L|^2}{|1 - \Gamma_L S_{22}|^2}$$

Notice that the value of  $\Gamma_s$  affects  $G_s$  **only**, and the value of  $\Gamma_L$  affects  $G_L$  **only**. Therefore, the unilateral case again decouples into two **independent** problems

- We can compare these three values with their **maximum** achievable values (when  $\Gamma_s = S_{11}^*$  and  $\Gamma_L = S_{22}^*$ ):

$$G_{s\max} = \frac{1}{1 - |S_{11}|^2}$$

$$G_{L\max} = \frac{1}{1 - |S_{22}|^2}$$

$$G_{0\max} = |S_{21}|^2$$

- Therefore, to increase the bandwidth of an amplifier, we need to **select** values of  $G_s$  and  $G_L$  that are **less** (typically by a few dB) than the maximum (i.e., matched) values  $G_{s\max}$  and  $G_{L\max}$ .
- Unlike the values  $G_{s\max}$  and  $G_{L\max}$ —where there is precisely **one** solution for each ( $\Gamma_s = S_{11}^*$  and  $\Gamma_L = S_{22}^*$ )—there are an **infinite** number of  $\Gamma_s$  ( $\Gamma_L$ ) solutions for a specific value of  $G_s$  ( $G_L$ ).

## Design for Specified Gain (contd.)

**Q:** How do we **choose** the respective  $\Gamma_s$  ( $\Gamma_L$ ) and eventually  $G_s$  ( $G_L$ )?

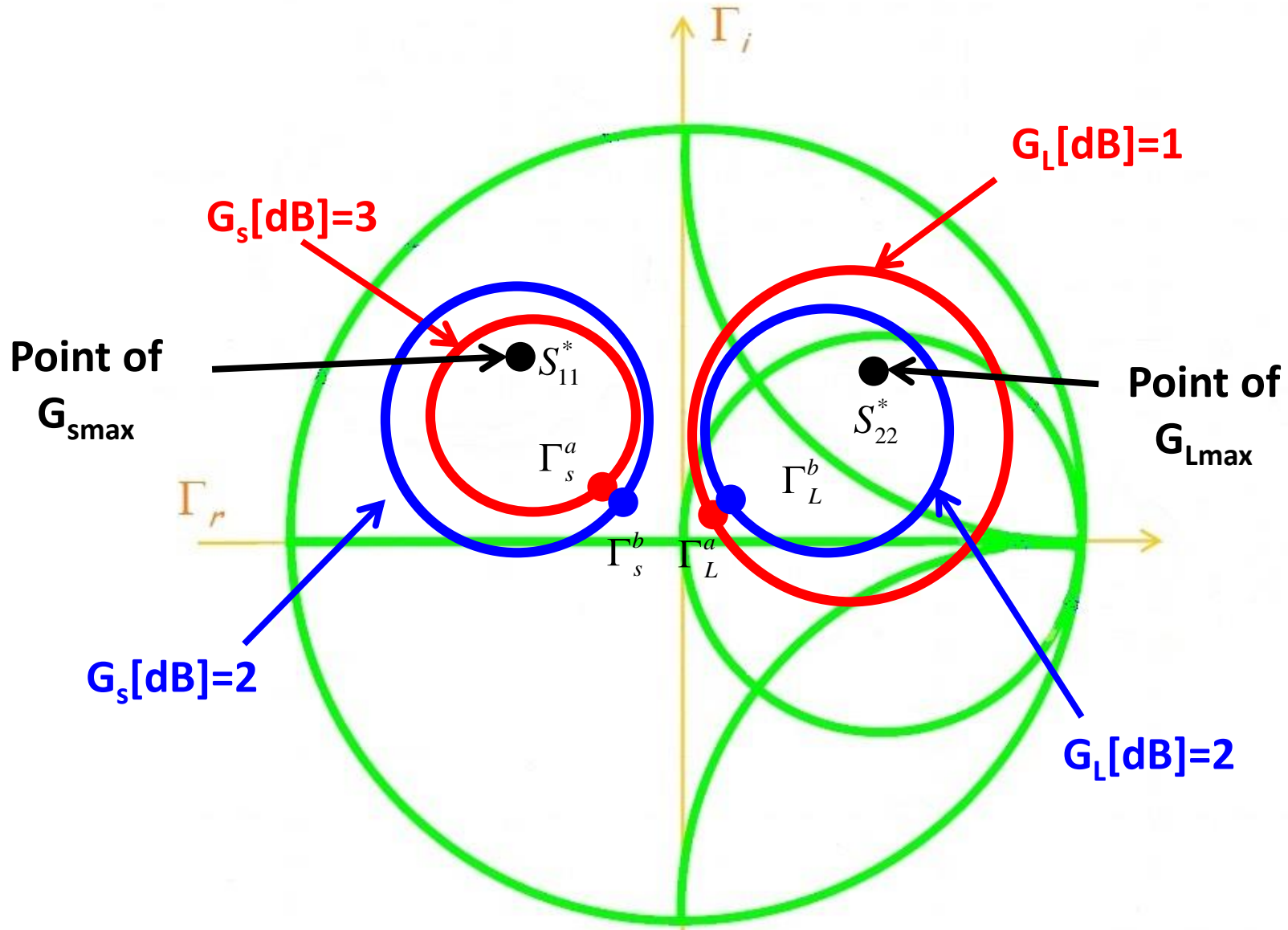
**A:** We can solve the equations to determine all  $\Gamma_s$  and  $\Gamma_L$  solutions for **specified** design values of  $G_s$  and  $G_L$ .

$$G_s = \frac{1 - |\Gamma_s|^2}{|1 - \Gamma_s S_{11}|^2}$$

$$G_L = \frac{1 - |\Gamma_L|^2}{|1 - \Gamma_L S_{22}|^2}$$

- Just as with our stability solutions, the solutions to the equations above form **circles** when plotted on the **complex  $\Gamma$ -plane**.
- These circles are known as **constant gain circles**, and are defined by two values: a **complex** value  $C_s$  ( $C_L$ ) that denotes the **center** of the circle on the **complex  $\Gamma$ -plane**, and a **real** value  $R_s$  ( $R_L$ ) that specifies the **radius** of that circle.
- Any  $\Gamma$  point **on** (not inside!) a constant gain circle denotes a value of  $\Gamma$  that will provide the requisite gain. To optimize the bandwidth we should choose the point on the circle that is **closest to the center** of the **complex  $\Gamma$ -plane**!

## Design for Specified Gain (contd.)





## Design for Specified Gain (contd.)

- For **example**, say we have an amplifier with:

$$G_{smax}[\text{dB}] = 4.0$$

$$G_0[\text{dB}] = 7.0$$

$$G_{Lmax}[\text{dB}] = 3.0$$

- such that its transducer gain is **14 dB** at its design frequency. To increase the **bandwidth** of this amplifier, we decide to **reduce** the gain to 11 dB.
- Thus, we find that our design goal is:  $G_s[\text{dB}] + G_L[\text{dB}] = 4.0$
- From the gain circles on the Smith Chart on the previous slide (assuming they represent the gain circles for this gain element), we find there are **two solutions**; we'll call them **solution a** and **solution b**.

### Solution a

We determine the  $\Gamma_s^a$  and  $\Gamma_L^a$  from the gain circles:

$$G_s[\text{dB}] = 3.0 \quad G_L[\text{dB}] = 1.0$$

### Solution b

We determine the  $\Gamma_s^b$  and  $\Gamma_L^b$  from the gain circles:

$$G_s[\text{dB}] = 2.0 \quad G_L[\text{dB}] = 2.0$$

## Design for Specified Gain (contd.)

There are of course an **infinite** number of possible solutions, as there are an infinite number of solutions to  $G_s[\text{dB}] + G_L[\text{dB}] = 4.0$ . The two solutions provided here are fairly **representative**.

**Q:** So **which** solution should we use?

**A:** That choice is a bit **subjective**.

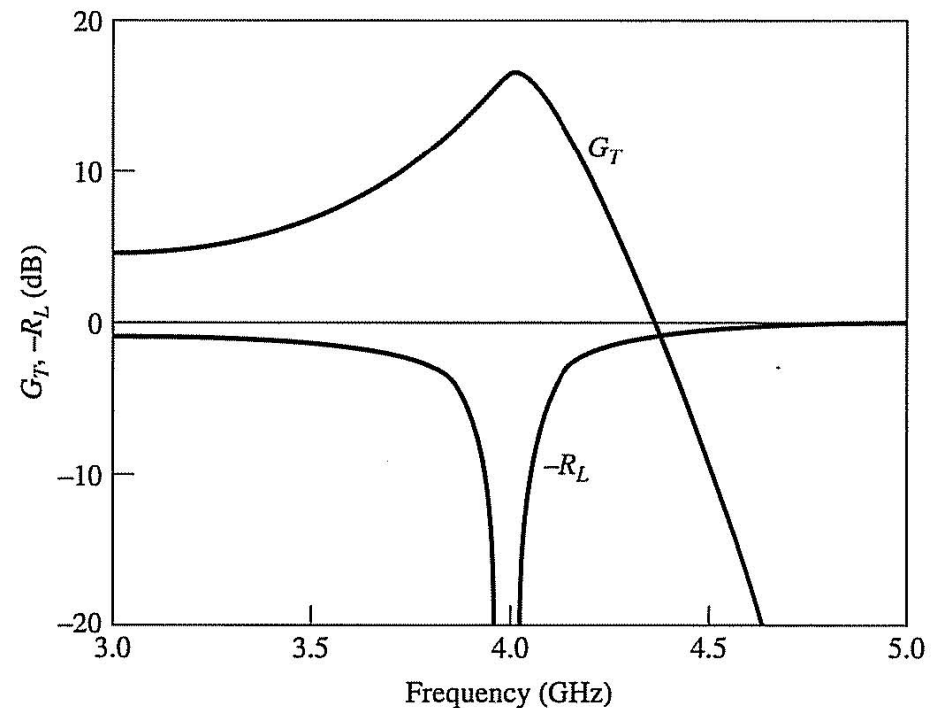
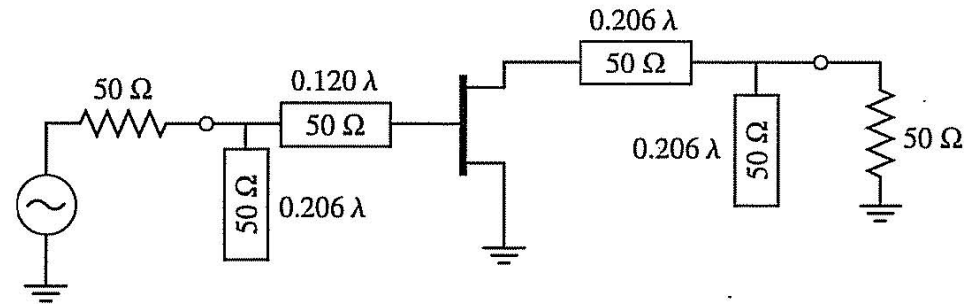
- We note that the point  $\Gamma_L^a$  is **very close** to the center, while the point  $\Gamma_s^a$  pretty **far away** (i.e.,  $\Gamma_L^a$  is small and  $\Gamma_s^a$  is large).
- In contrast, both  $\Gamma_s^b$  and  $\Gamma_L^b$  are **fairly close** to the center, although neither is as close as  $\Gamma_L^a$
- To get the widest bandwidth, I would choose **solution b**, but the only way to know for sure is to design and **analyze both solutions**.
- Often, the design with the widest bandwidth will depend on how you **define** bandwidth!

**Q:** So we reduce the transducer gain by designing and constructing a **mismatched** matching network. Won't that result in **return loss**?

**A:** Absolutely!

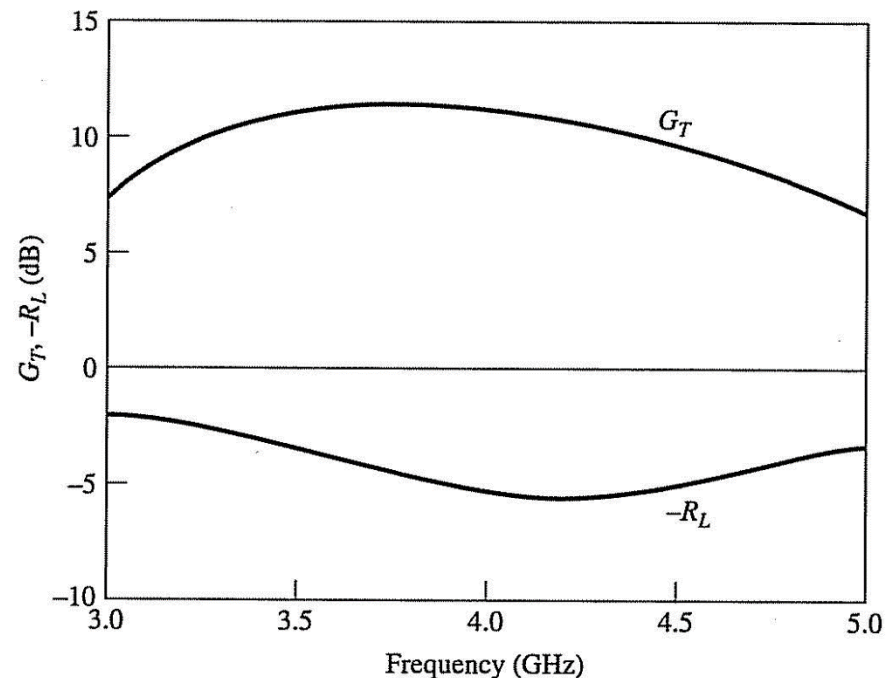
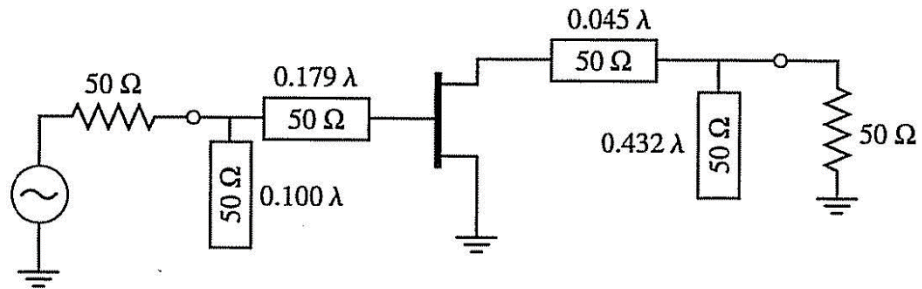
## Design for Specified Gain (contd.)

- A conjugate matched amplifier is not only narrow band with regard to gain, it is also **narrow band** with regard to **return loss**. **Only** at the design frequency will the amplifier ports be perfectly matched. As we move away from the design frequency, the return loss **quickly degrades!**



## Design for Specified Gain (contd.)

- With the “mismatched” design, we typically find that the return loss is **better** at frequencies away from the design frequency (as compared to the matched design), although at **no frequency** do we achieve a **perfect match** (unlike the matched design).



## Design for Specified Gain (contd.)

Generally speaking, a good (i.e., **acceptable**) return loss over a wide range of frequencies is **better** than a perfect return loss at one frequency and poor return loss everywhere else!

**Q:** Won't you **ever** stop talking??

**A:** Yup. I'm all done.