

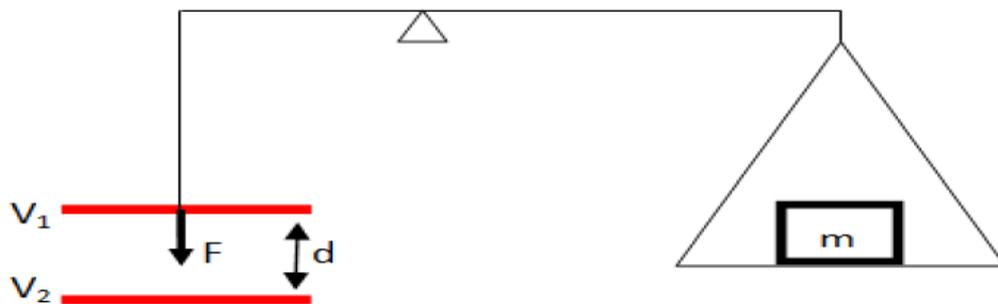
TUTORIAL 6

Ques 1. For the current density $J=10z\sin 2\phi \mathbf{a}_\rho$ A/m², find the current through the cylindrical surface $\rho=2$, $1 \leq z \leq 5$ m.

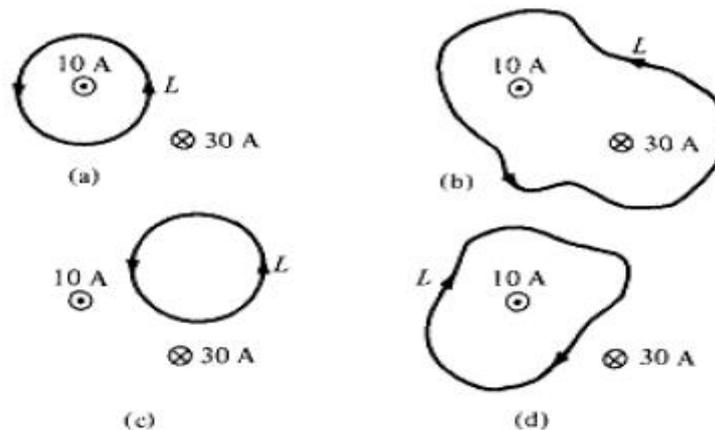
Ques 2. (a) What is field intensity on the surface of each plate of capacitor in terms of ρ_s (surface charge density), and ϵ (the permittivity of the dielectric filled in the capacitor)? Inside the capacitor?

(b) What is the force with which *each* plate of a parallel-plate capacitor attract the other in terms of ρ_s , S(plates area), and ϵ .

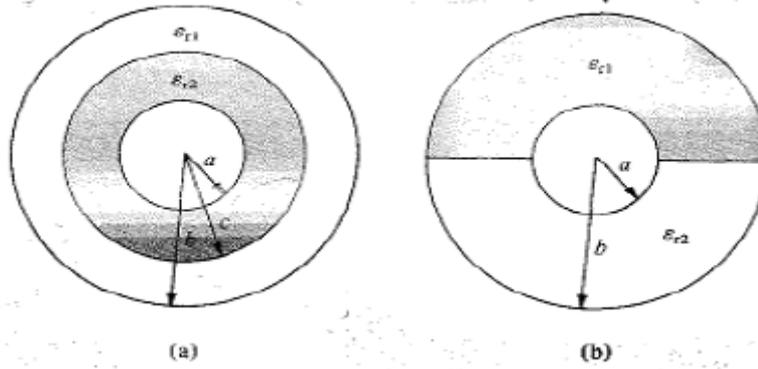
(c) In an interesting arrangement called *electrometer*, a balance is used to measure potential difference between the two plates as shown in Fig (bottom plane is fixed). Suppose a mass 'm' is what sets equilibrium, prove that V_1-V_2 (the potential difference) is equal to $(2mgd^2/S\epsilon)^{1/2}$.



Ques 3. For the currents and closed paths of Figure, calculate the value of $\oint \mathbf{H} \cdot d\mathbf{l}$



Ques 4. If Figure represents the cross sections of two spherical capacitors, determine their capacitances. Let $a=1$ mm, $b=3$ mm, $c=2$ mm, $\epsilon_{r1}=2.5$ and $\epsilon_{r2}=3.5$.



Ques 5. If $\mathbf{H} = y \mathbf{a}_x - x \mathbf{a}_y$ A/m on plane $z = 0$,

(a) Determine the current density and

(b) Verify Ampere's law by taking the circulation of \mathbf{H} around the edge of the rectangle $Z=0$, $0 < x < 3, -1 < y < 4$.

Ques 6. Given that $\mathbf{J} = 5e^{-10^4 t} / r \mathbf{a}_r$ A/m² at $t = 0.1$ ms, find: (a) the amount of current passing surface $r = 2$ m, (b) the charge density ρ_v on that surface.