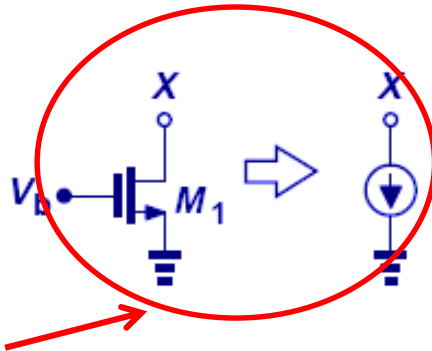


Lecture – 6

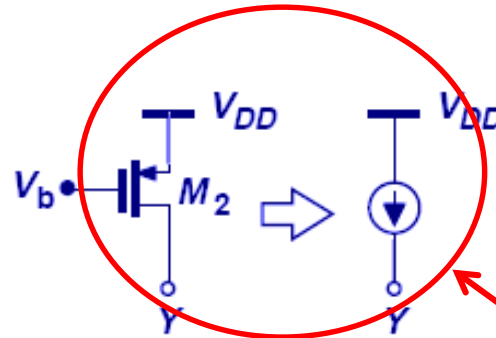
Date: 29.08.2016

- CS Amplifier with Constant Current Source, Triode Load, Source Degenerated Resistor, Examples
- Common Drain Amplifier
- Examples

Constant Current Source



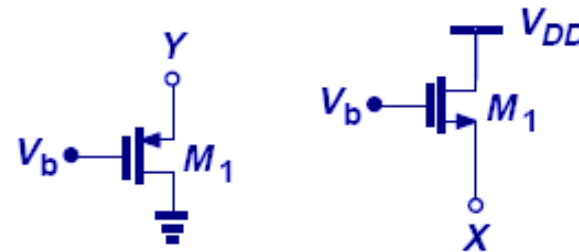
NFET ideal current source



PFET ideal current source

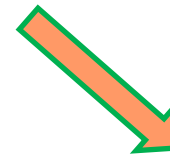
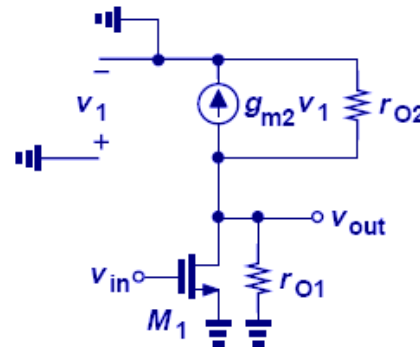
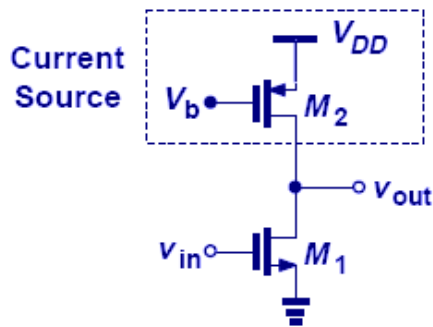
- As long as a MOS transistor is in saturation region and $\lambda=0$, the current is independent of the drain voltage and it behaves as an ideal current source seen from the drain terminal.

Example of poor current source

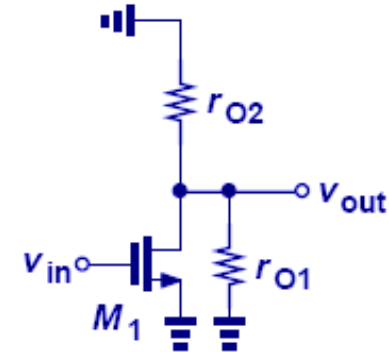


- Since the variation of the source voltage directly affects the current of a MOS transistor, it does not operate as a good current source if seen from the source terminal

CS Amplifier with Constant Current Source (contd.)



The dc voltage V_{GS2} is constant and therefore $v_1 = 0 \rightarrow$ leads to $g_{m2}v_1 = 0$



$$A_v = -g_{m1}(r_{o1} \parallel r_{o2})$$

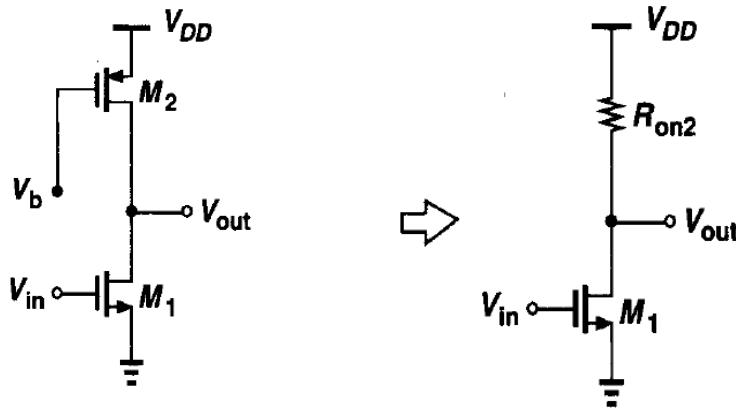


- Both the load and the device operates in saturation
- The gain is loosely dependent on $|V_{DS}|$ of $M_2 \rightarrow$ as it regulates r_{o2}
- The voltage $|V_{DS2,min}| = |V_{GS2} - V_{T2}|$ can be reduced \rightarrow by increasing $(W/L)_2 \rightarrow$ increases $V_{D1} \rightarrow$ in essence the output voltage swing
- r_{o2} can be increased \rightarrow by reducing the channel length modulation effect \rightarrow through increasing the length and width of $M_2 \rightarrow$ while keeping $|V_{GS2} - V_{T2}|$ constant \rightarrow However, this also brings large capacitance at the output of M_2 .

CS Amplifier with Constant Current Source (contd.)

- At a given drain current, W has to increase with the increasing L ($r_o \propto L/I_D$) for obtaining higher gain.
- If length of M_1 is increased by a factor \rightarrow then the width has to be increased proportionally \rightarrow for a given I_{D1} , $V_{GS1}-V_{T1}$ is directly proportional to $(W/L)_1 \rightarrow$ if W_1 is not scaled properly then it will reduce $V_{GS1}-V_{T1} \rightarrow$ will effectively lead to reduced voltage swing.
- Furthermore, just scaling of L_1 leads to reduced $g_{m1} \rightarrow$ in essence possibility of reduced gain.
- However, $g_{m1}r_{o1} = \sqrt{2\left(\frac{W}{L}\right)_1 \mu_n C_{ox} I_D} \frac{1}{\lambda I_D}$
- The gain will increase with increasing L_1 considering that λ depends more strongly on length than g_m does.
- for M_2 , increase in L_2 while keeping W_2 constant \rightarrow increases $r_{o2} \rightarrow$ increases gain of the CS amplifier \rightarrow but decreases $|V_{DS2}| \rightarrow$ reduces the output voltage swing.

CS Amplifier with Triode Load

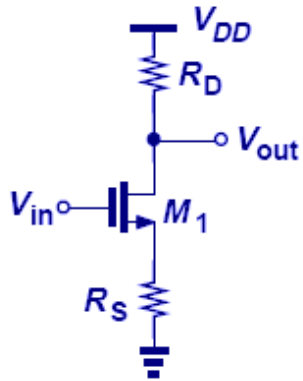


$$R_{on2} = \frac{1}{\mu_p C_{ox} (W/L)_2 (V_{DD} - V_b - |V_{TP}|)}$$

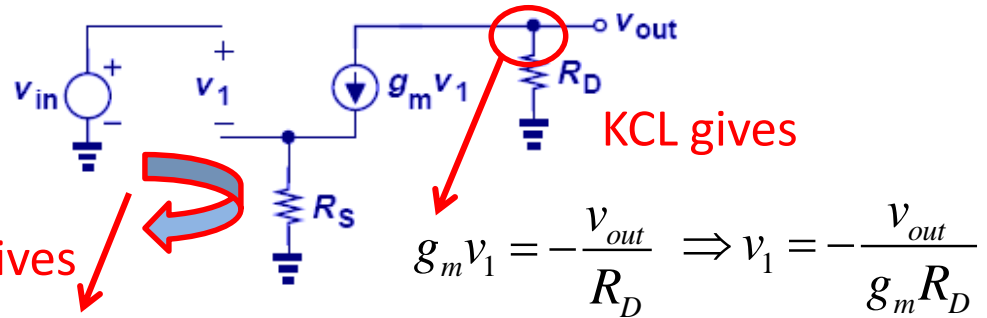
$$A_v = -g_{m1} R_{on2} \quad A_v = -g_{m1} (r_{o1} \parallel R_{on2})$$

- The main limitation of this technique is the dependence of gain on the process parameters → because R_{on} is dependent on these parameters.
- Process parameters are temperature dependent → makes gain dependent on temperature.
- Triode loads consume less voltage headroom as compared to diode-connected load → Here, $V_{out,max} = V_{DD}$.

CS Amplifier with Source Degeneration



small signal
model



$$v_{in} = v_1 + g_m v_1 R_S$$

$$\therefore v_{in} = -\frac{v_{out}}{g_m R_D} (1 + g_m R_S)$$

- Therefore the voltage gain: $A_v = \frac{v_{out}}{v_{in}} = -\frac{g_m R_D}{(1 + g_m R_S)}$
- The input resistance: $R_{in} = \infty$
- The output resistance: $R_{out} = R_D$
- For large R_S : $A_v = -\frac{R_D}{R_S}$ ← **Linear**

Valid as long as M_1
is in saturation

$$V_{DD} - V_{in} + V_T > I_D R_D \longrightarrow V_{DD} - I_D R_D > V_{in} - V_T$$

CS Amplifier with Source Degeneration (contd.)

- A_v drops when: $V_{DD} - V_{in} + V_T < I_D R_D$ ← M_1 goes in triode

Even with all the supposed benefits of this configuration, the major drawback is the reduced small-signal gain

$$A_v = \frac{v_{out}}{v_{in}} = - \frac{g_m}{(1 + g_m R_S)} R_D$$

Ratio of impedances in the drain and source path

$$G_m = \frac{g_m}{1 + g_m R_S} = \frac{1}{(1/g_m) + R_S}$$

Equivalent Circuit Transconductance

$$\Rightarrow A_v = - \frac{R_D}{R_S}$$

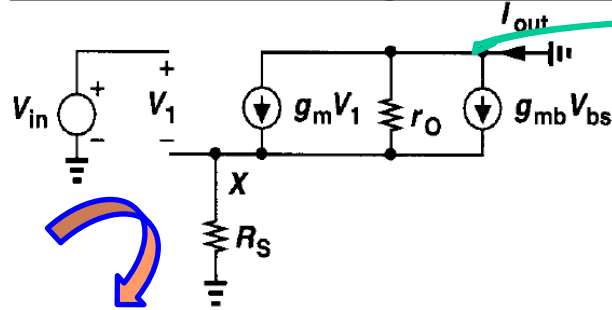
Linear

For large V_{in} (while M_1 still in saturation) $\rightarrow g_m$ is high $\rightarrow G_m$ approaches $1/R_S$

Reduced Gain

CS Amplifier with Source Degeneration (contd.)

With channel length modulation and body effect



KCL at output:

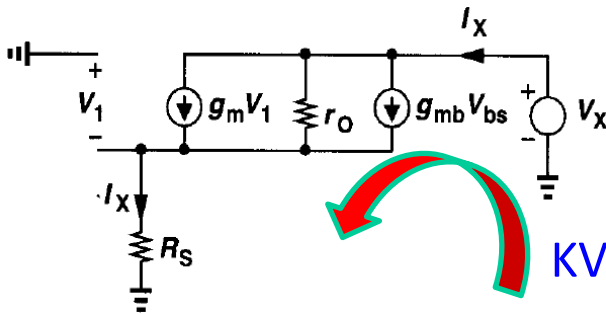
$$I_{out} = g_m V_1 - g_{mb} V_x - \frac{I_{out} R_S}{r_o}$$

$$\Rightarrow I_{out} = g_m (V_{in} - I_{out} R_S) + g_{mb} (-I_{out} R_S) - \frac{I_{out} R_S}{r_o}$$

KVL at input: $V_{in} = V_1 + I_{out} R_S$

$$\therefore G_m = \frac{I_{out}}{V_{in}} = \frac{g_m r_o}{R_S + [1 + (g_m + g_{mb}) R_S] r_o}$$

Output Resistance



Current through R_S is I_x

$$\Rightarrow V_1 = -I_x R_S$$

Current through r_o is:

$$\Rightarrow I_{r_o} = I_x - (g_m + g_{mb}) V_1$$

KVL at the output: $V_x = r_o [I_x + (g_m + g_{mb}) R_S I_x] + I_x R_S$

$$\Rightarrow R_{out} = \frac{V_x}{I_x} = r_o [1 + (g_m + g_{mb}) R_S] + R_S = [1 + (g_m + g_{mb}) r_o] R_S + r_o$$

CS Amplifier with Source Degeneration (contd.)

Usually, $(g_m + g_{mb})r_o \gg 1$ $\therefore R_{out} \approx (g_m + g_{mb})r_o R_S + r_o$

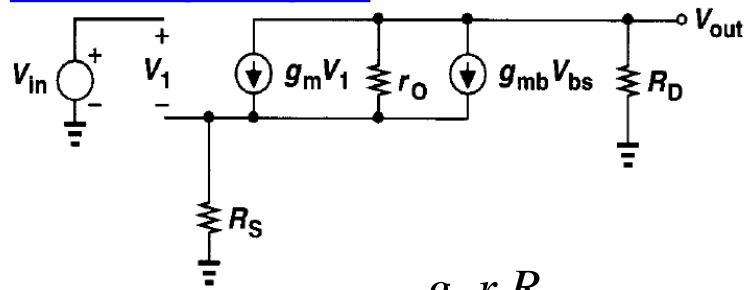
Output impedance has increased by this factor

$\Rightarrow R_{out} \approx [1 + (g_m + g_{mb})R_S]r_o$

Definitely a good prospect for applications requiring higher output impedance

Yes! It comes with a price \rightarrow reduced gain

Small-signal gain



$$A_v = -\frac{V_{out}}{V_{in}} = -\frac{g_m r_o R_D}{R_D + R_S + [1 + (g_m + g_{mb})R_S]r_o}$$

$$A_v = -\frac{g_m r_o R_D}{R_D + R_S + [1 + (g_m + g_{mb})R_S]r_o} \cdot \frac{R_S + [1 + (g_m + g_{mb})R_S]r_o}{R_S + [1 + (g_m + g_{mb})R_S]r_o}$$

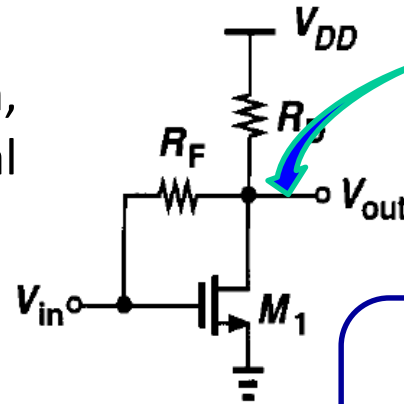
For Simplification

$$A_v = -\frac{g_m r_o}{R_S + [1 + (g_m + g_{mb})R_S]r_o} \cdot \frac{[R_S + [1 + (g_m + g_{mb})R_S]r_o]R_D}{R_D + R_S + [1 + (g_m + g_{mb})R_S]r_o}$$

$R_D || R_{out}$

Example – 1

- Assuming M_1 in saturation, calculate the small signal voltage gain of the following:



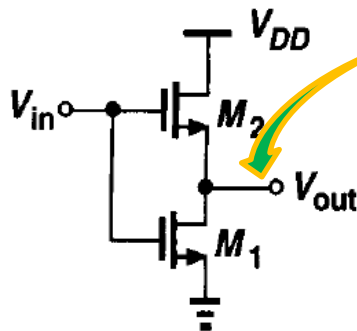
KCL at the output node:

$$\frac{v_{out} - v_{in}}{R_F} + g_{m1}v_{in} + \frac{v_{out}}{r_{o1}} + \frac{v_{out}}{R_D} = 0$$

$$A_v = \frac{v_{out}}{v_{in}} = -\frac{g_{m1} - \frac{1}{R_F}}{\frac{1}{R_F} + \frac{1}{r_{o1}} + \frac{1}{R_D}}$$

Example – 2

- Assuming both M_1 and M_2 in saturation, calculate the small signal **voltage** gain of the following:



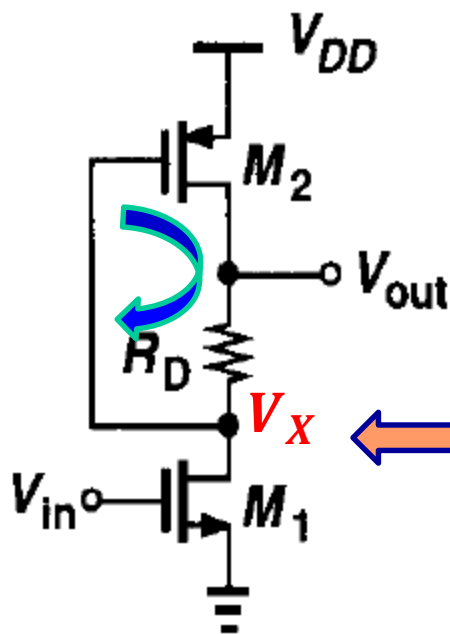
KCL at the output node:

$$g_{m2}(v_{in} - v_{out}) + \left(\frac{-v_{out}}{r_{o2}} \right) = g_{m1}v_{in} + \frac{v_{out}}{r_{o1}}$$

$$A_v = \frac{v_{out}}{v_{in}} = -\frac{g_{m1} - g_{m2}}{g_{m2} + \frac{1}{r_{o2}} + \frac{1}{r_{o1}}}$$

Example – 3

- Assuming both M_1 and M_2 in saturation, calculate the small signal voltage gain of the following:



KVL in the mesh created by M_2 :
$$\left(g_{m1}v_{in} + \frac{v_x}{r_{o1}} \right) R_D + v_x = v_{out}$$

KCL at this node:

$$-\left(g_{m2}v_x + \frac{v_{out}}{r_{o2}} \right) = g_{m1}v_{in} + \frac{v_x}{r_{o1}}$$

$$v_x \left(-g_{m2} - \frac{1}{r_{o1}} \right) = g_{m1}v_{in} + \frac{v_{out}}{r_{o2}}$$

$$\therefore v_x = -\frac{g_{m1}v_{in} + \frac{v_{out}}{r_{o2}}}{g_{m2} + \frac{1}{r_{o1}}}$$

Example – 3 (contd.)

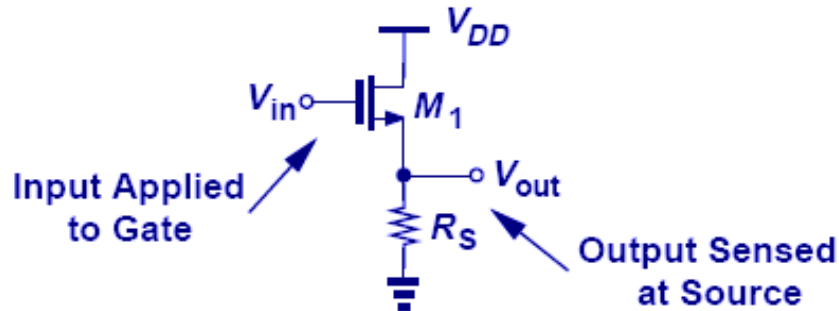
$$\left(g_{m1} v_{in} + \frac{v_x}{r_{o1}} \right) R_D + v_x = v_{out} \quad \longrightarrow \quad g_{m1} R_D v_{in} + \left(1 + \frac{R_D}{r_{o1}} \right) v_x = v_{out}$$

- Simplification of the expressions gives:

$$g_{m1} R_D v_{in} - \frac{\left(1 + \frac{R_D}{r_{o1}} \right) \left(g_{m1} v_{in} + \frac{v_{out}}{r_{o2}} \right)}{g_{m2} + \frac{1}{r_{o1}}} = v_{out}$$

$$A_v = \frac{v_{out}}{v_{in}} = \frac{g_{m1} (g_{m2} R_D - 1)}{g_{m2} + \frac{1}{r_{o1}} + \frac{1}{r_{o2}} \left(1 + \frac{R_D}{r_{o1}} \right)}$$

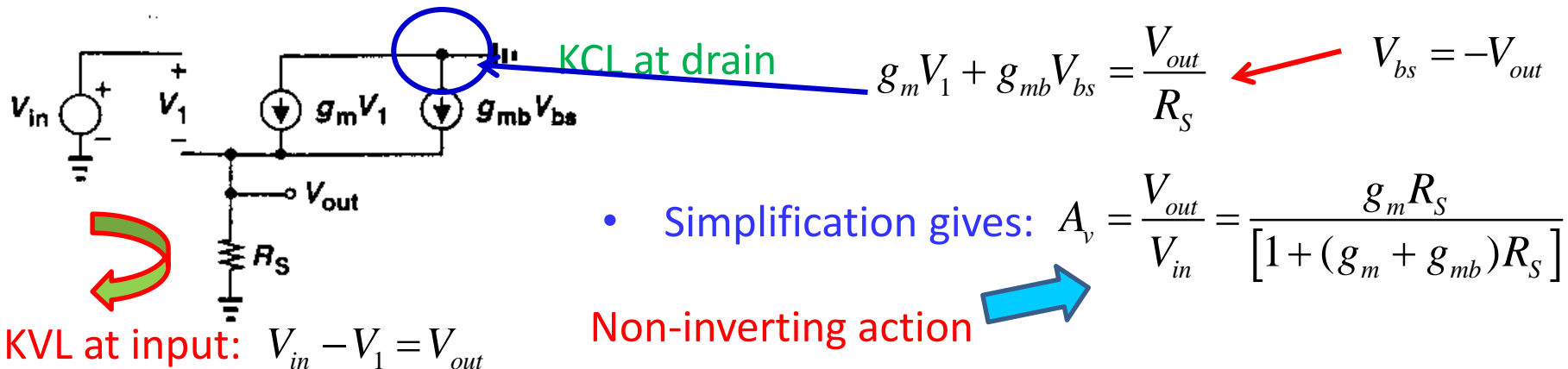
CD Amplifier (Source Follower)



It senses the input at the gate and produces the output at the source

CS-stage can achieve high voltage gain if the load impedance is large → if CS-stage is to be succeeded by a low impedance circuitry then a buffer is needed → CD-stage works as a buffer

Let us look at the small-signal voltage gain of CD-stage:



Can you derive A_v without explicitly using the small signal model ?

CD Amplifier (Source Follower) – contd.

Observations

- For $V_{in} = V_T$, the transconductance $g_m = 0$ and therefore $A_v = 0$.
- V_{in} increases $\rightarrow I_D$ increases \rightarrow leads to increase in $g_m \rightarrow A_v$ increases and approaches:

$$A_v = \frac{V_{out}}{V_{in}} = \frac{g_m R_S}{[1 + (g_m + g_{mb})R_S]}$$

$$A_v = \frac{g_m}{g_m + g_{mb}} = \frac{1}{1 + \eta}$$

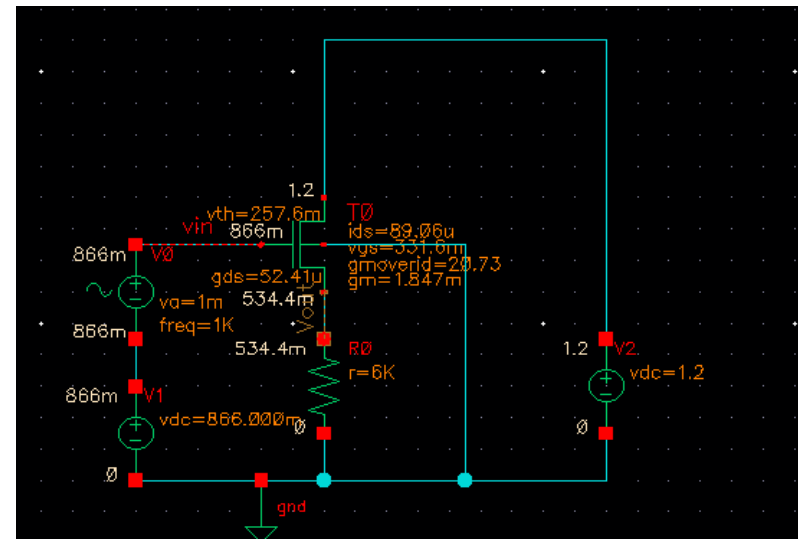
η decreases with increase in $V_{out} \rightarrow$ leads to increase in $A_v \rightarrow \eta$ is typically 0.2 and therefore $A_v < 1$

Even for $R_S = \infty$, the small signal voltage gain $A_v < 1$

Example: $g_m = 2 \text{ mS}$
 $g_{mb} = 0.328 \text{ mS}$
 $R_S = 6 \text{ k}\Omega$



Calculated $A_v = 0.801$



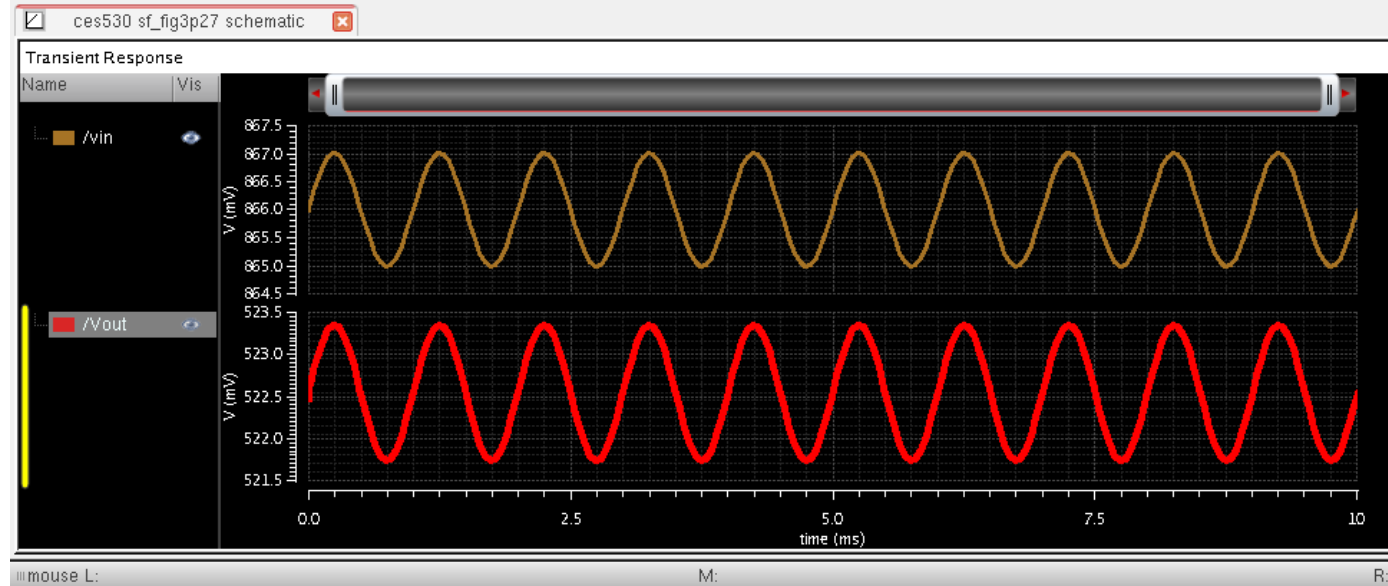
CD Amplifier (Source Follower) – contd.

Example (contd.):

$$V_{in, pp} = 2 \text{ mV}$$

$$V_{out, pp} = 1.596 \text{ mV}$$

$$\text{Simulated: } A_v = 0.798$$



$$A_v < 1$$



Definitely not an amplifier

- In the best case scenario when R_S is extremely high and body effect is ignored then:
- How can you ignore body effect?

$$A_v = 1$$



Usefulness as buffer

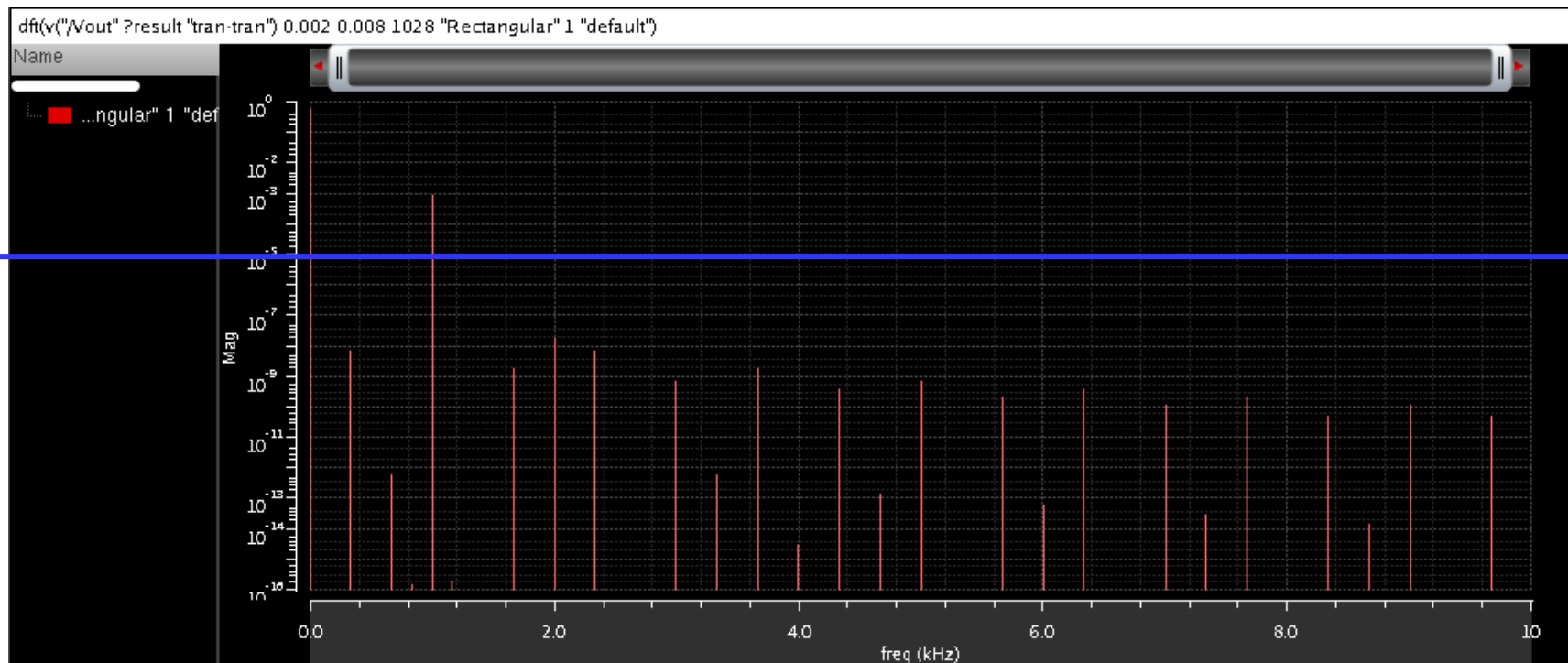
Definitely not for NMOS

By employing a PMOS and with appropriate biasing

CD Amplifier (Source Follower) – contd.

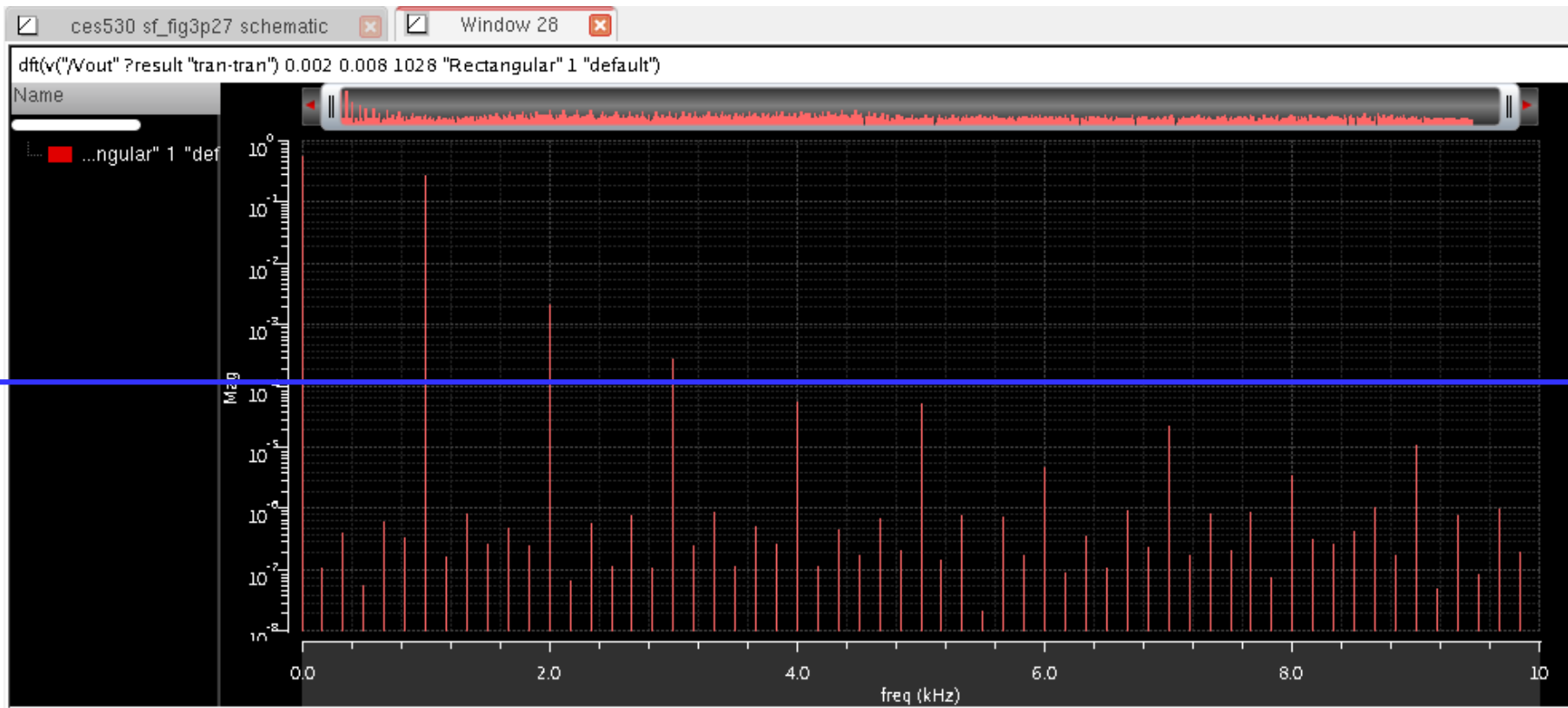
- Furthermore, the strong dependence of A_v on the input voltage makes it a nonlinear configuration → Its due to strong dependence of I_D and therefore g_m on the input voltage V_{in}

$$V_{in} = 1\text{mV}$$



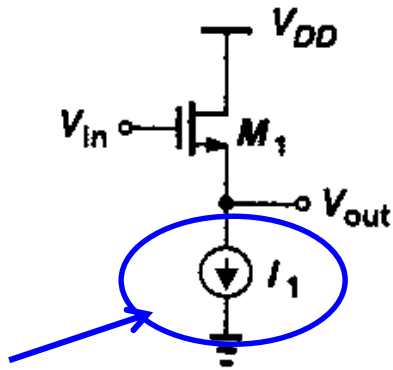
CD Amplifier (Source Follower) – contd.

$$V_{in} = 330\text{mV}$$

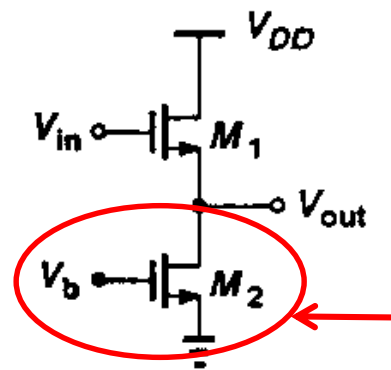


CD Amplifier (Source Follower) – contd.

- To mitigate this dependence → resistor R_S is replaced by a current source → the current source is realized using an NMOS operating in saturation mode



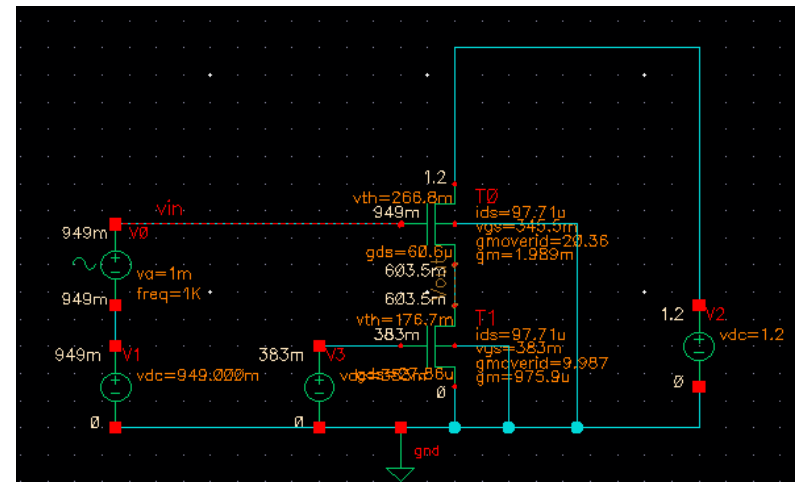
Current source providing high R_S



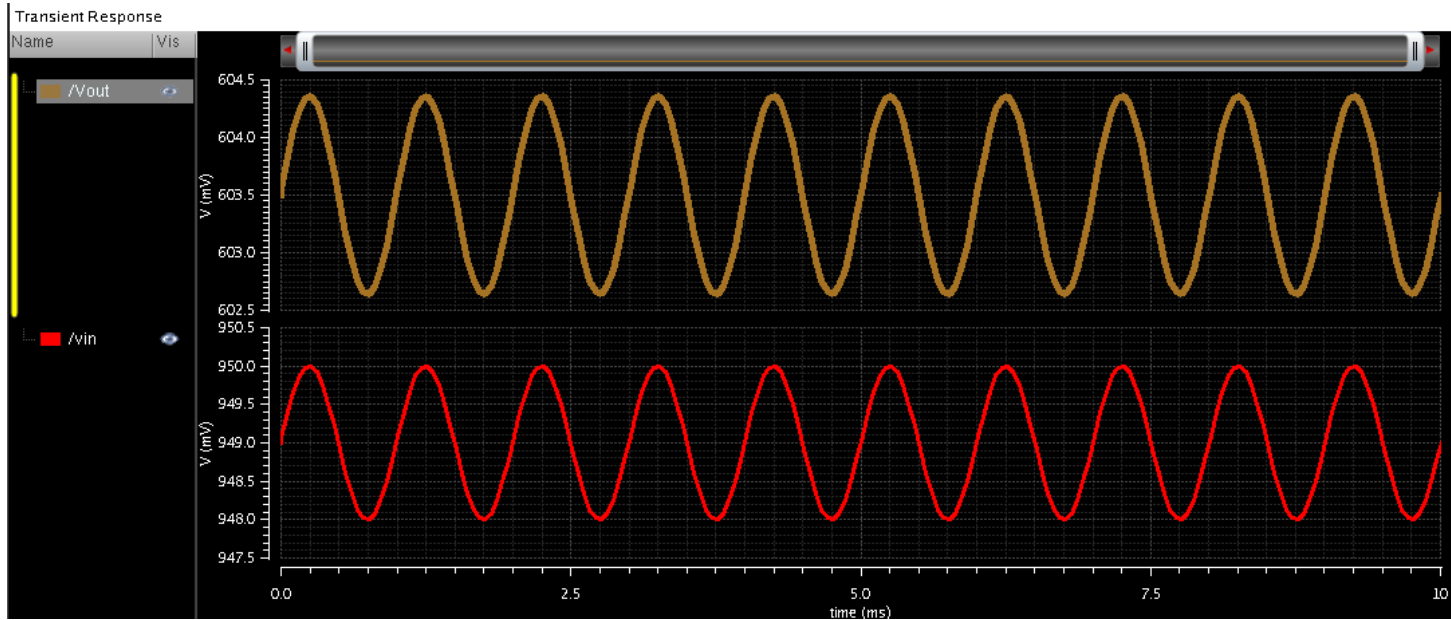
NMOS Operating in Saturation

$$A_v = \frac{\frac{1}{g_{mb1}} \parallel r_{o1} \parallel r_{o2}}{\frac{1}{g_{mb1}} \parallel r_{o1} \parallel r_{o2} + \frac{1}{g_{m1}}}$$

- Let us get back to that example:



CD Amplifier (Source Follower) – contd.



$$V_{in, pp} = 2 \text{ mV}$$

$$V_{out, pp} = 1.705 \text{ mV}$$

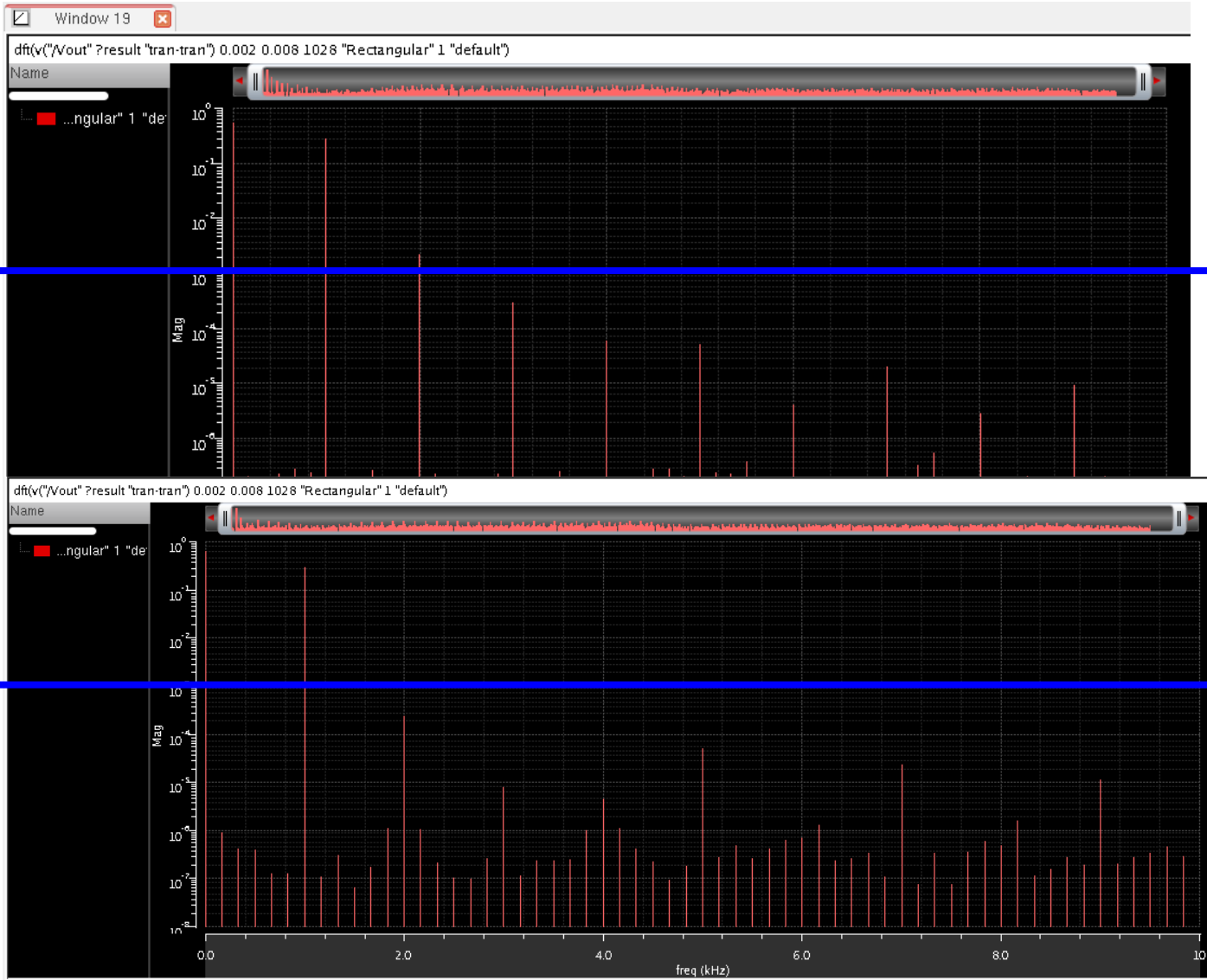
Simulated: $A_v = 0.8525$

CD Amplifier (Source Follower) – contd.

$$V_{in} = 330\text{mV}$$

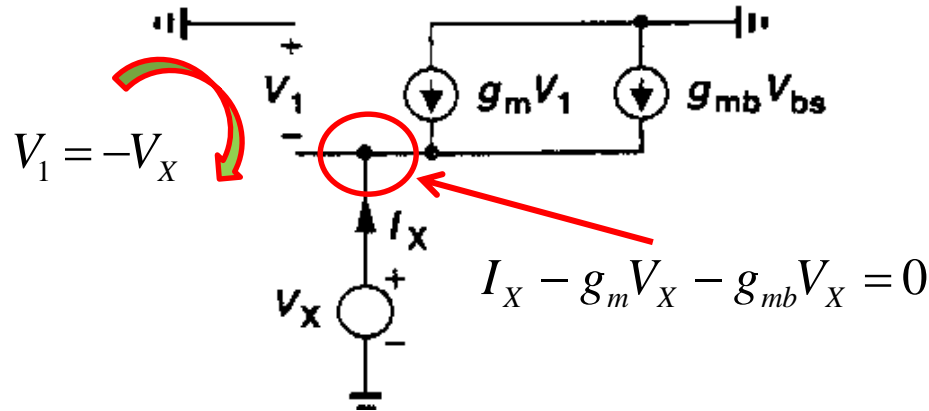
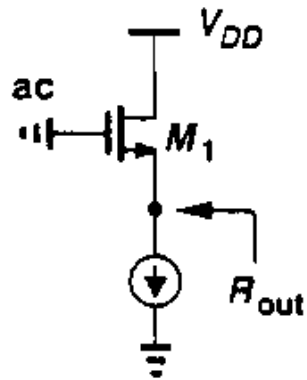
$$R_S = 6\text{k}\Omega$$

$$R_S = \text{Current Source}$$



CD Amplifier (Source Follower) – contd.

- Let us look into the small-signal output resistance:



$$R_{out} = \frac{1}{g_m + g_{mb}}$$

Body effect reduces the output impedance

- If channel length modulation is taken into account then:

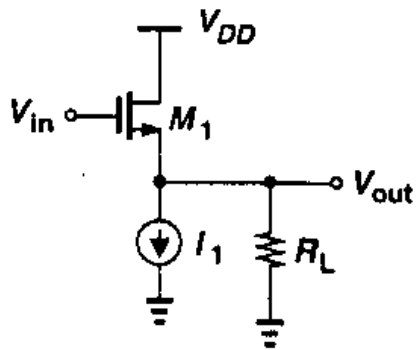
$$\therefore R_{out} = \frac{1}{g_m + g_{mb}} \parallel r_o$$

Further Reduction in output impedance

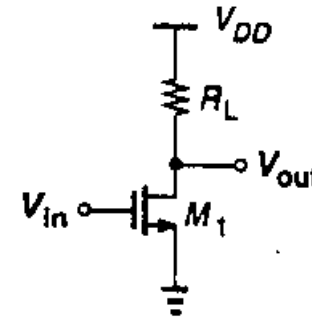
CD Amplifier (Source Follower) – contd.

- High input impedance and low output impedance with near unity gain enables CD stage to work as buffer (not always!) → useful for CS stage specially when the load impedance is raised very high to enhance the gain
- Reduced output voltage swing when used as buffer for a CS stage
- CD topology is nonlinear → due to body effect and channel length modulation → also the gain is dependent on g_m
- CD topology generates substantial noise → hence not suitable for low noise applications (beyond this course!!)

Comparison of CD and CS Stages



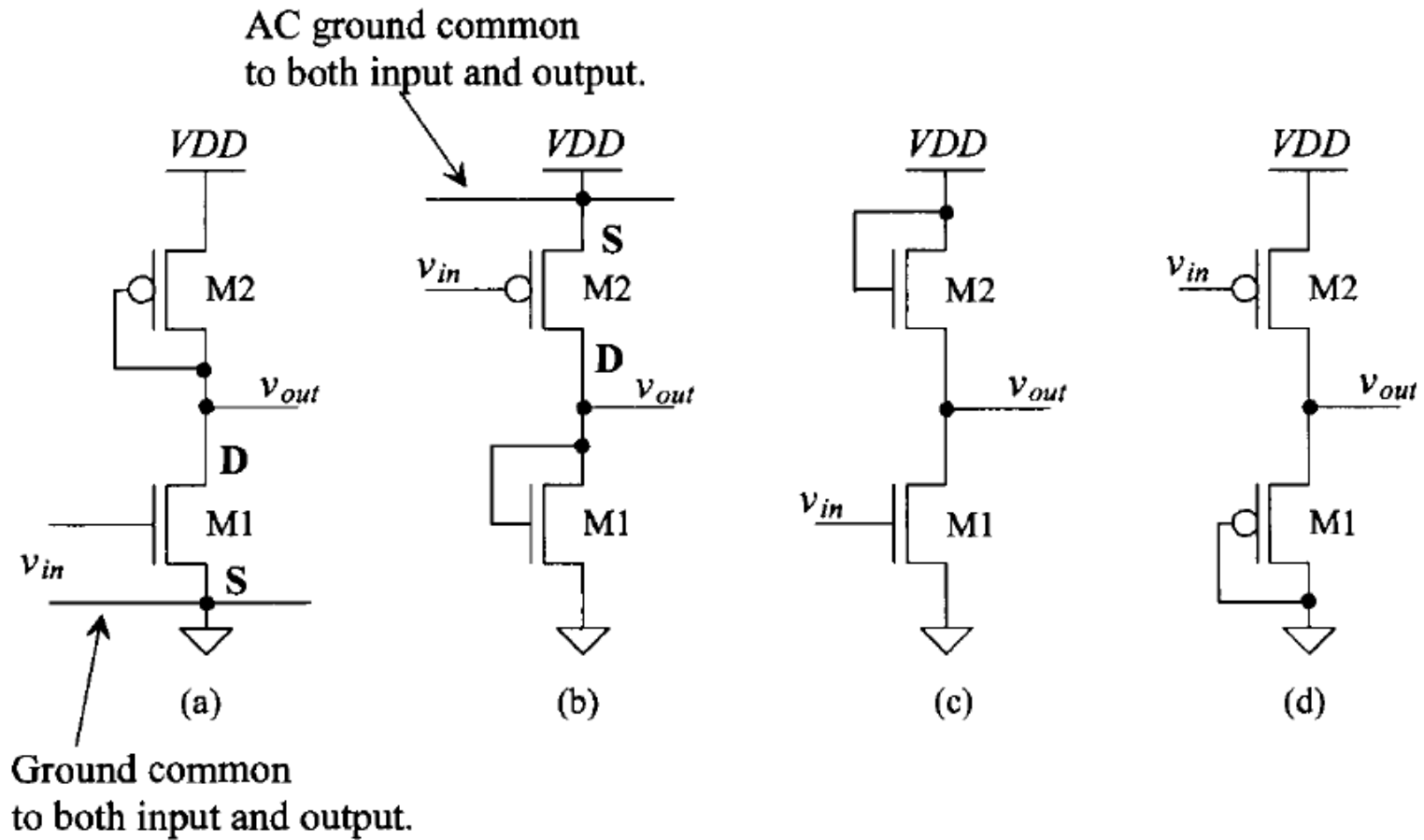
$$A_v |_{CD} \approx \frac{R_L}{R_L + \frac{1}{g_{m1}}}$$



$$A_v |_{CS} \approx -g_{m1} R_L$$

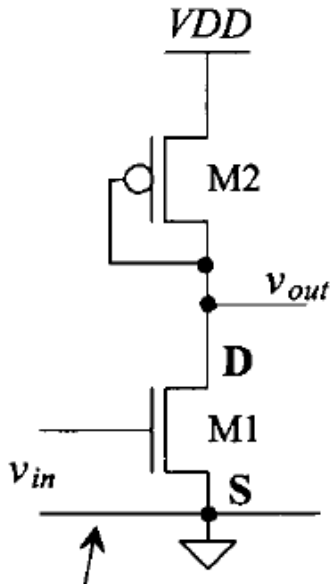
- CD is non-inverting whereas CS is inverting
- CS provides higher gain
- For example, if $1/g_{m1} = R_L$ then the gain provided by the CS stage equals 1 whereas the output of CD stage is 0.5 of the input

Intuitive Analysis - CS Stage

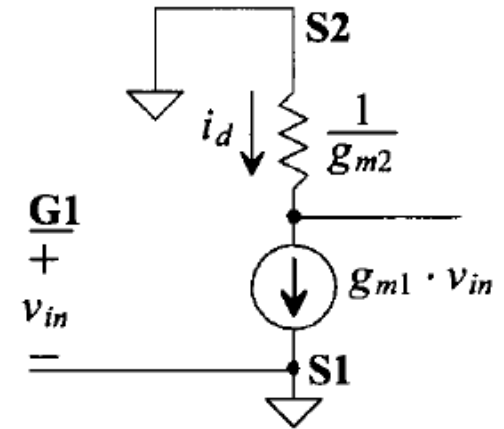


Four possible configurations of common-source amplifiers with diode-connected loads.

Intuitive Analysis - CS Stage (contd.)



To analyze the gain, begin by replacing M2 with a resistor $\frac{1}{g_{m2}}$ [Assume $\frac{1}{g_{m2}} \ll r_{o1} || r_{o2}$] and replacing M1 with a current source of $g_{m1} v_{in}$.



- The small-signal gain of the CS amplifier is given by

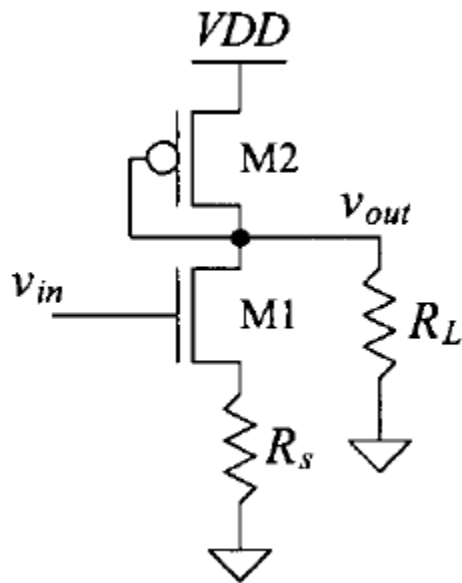
$$A_v = \frac{-i_d \cdot \frac{1}{g_{m2}}}{i_d \cdot \frac{1}{g_{m1}}} = -\frac{1}{\frac{1}{g_{m1}}} = -g_{m1}$$

Ratio of the resistance in the drain of M1 divided by the resistance in the source of M1

Caution: it is assumed that r_o is much greater than $\frac{1}{g_m}$.

Example – 4

Determine the small-signal AC gain of the following circuit.



$$A_v = \frac{v_{out}}{v_{in}} = - \frac{\text{resistance in the drain}}{\text{resistance in the source}}$$

resistance in the drain: $\frac{1}{g_{m2}} \parallel R_L$

For: $r_{o1} \parallel r_{o2} \gg \frac{1}{g_{m2}}$

resistance in the source: $\frac{1}{g_{m1}} + R_S$

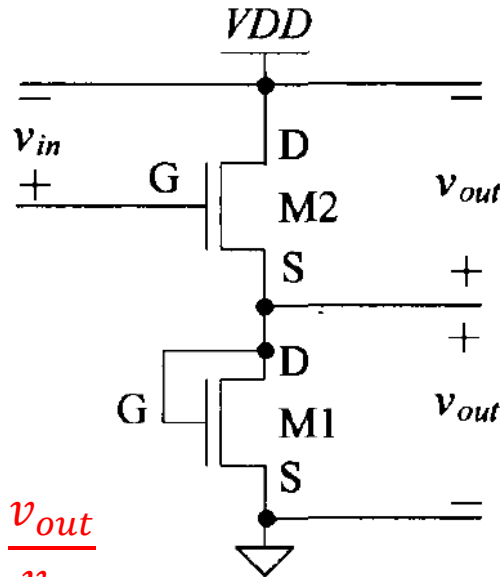
$$A_v = \frac{v_{out}}{v_{in}} = - \frac{\frac{1}{g_{m2}} \parallel R_L}{\frac{1}{g_{m1}} + R_S}$$

$R_L \rightarrow \infty$ and $R_S \rightarrow 0$



$$A_v = - \frac{g_{m1}}{g_{m2}}$$

Intuitive Analysis - CD Stage



$$A_v = \frac{v_{out}}{v_{in}}$$

resistance connected to the source

= resistance connected to the source + resistance looking into the source

$$A_v = \frac{1}{\frac{1}{g_{m1}} + \frac{1}{g_{m2}}}$$

output resistance = ??

