

Fields and Waves

Tutorial-6 19th February, 2016

Ques1: Given the potential $V = \frac{10}{r^2} \sin \theta \cos \phi$,

- (a) Find the electric flux density \vec{D} at $(2, \pi/2, 0)$
- (b) Calculate the work done in moving a $10\mu\text{C}$ charge from point A($1, 30^\circ, 120^\circ$) to B($4, 90^\circ, 60^\circ$)

Ques2: A spherically symmetric charge distribution is given by

$$\rho_v = \begin{cases} \rho_o \left(1 - \frac{r}{a}\right)^2 & r \leq a \\ 0 & r \geq a \end{cases}$$

- (a) Find \vec{E} and V for $r \geq a$
- (b) Find \vec{E} and V for $r \leq a$
- (c) Find the total charge

Ques3: If $\vec{J} = \frac{1}{r^3} (2 \cos \theta \hat{a}_r + \sin \theta \hat{a}_\theta) \text{ A/m}^2$, calculate the current passing through

- (a) A hemispherical shell of radius 20cm, $0 < \theta < \pi/2, 0 < \phi < 2\pi$
- (b) A spherical shell of radius 10cm

Home Assignment to be submitted and discussed during tutorial session.

Ques1: A positive point charge Q is at the center of a spherical conducting shell of an inner radius R_i and an outer radius R_o . Determine \vec{E} and V as a function of R.

Ques2: Find the work done in moving a charge of $10\mu\text{C}$ along an incremental 1mm long path from $(1, 2, -1)$ to $(2, 2, -1)$ in a field given by

$$\vec{E} = (2y + 1)\hat{a}_x + 2x\hat{a}_y + 2\hat{a}_z$$

At the point $(1, 2, -1)$