## Fields and Waves

## Tutorial-5 (16 ${ }^{\text {th }}$ Feb, 2016)

Q1. Find the total charge on a circular disk defined by $r \leq a$ and $z=0$ if:
(a) $\rho_{s}=\rho_{s 0} \cos \phi\left(C / m^{2}\right)$
(b) $\rho_{s}=\rho_{s 0} \sin ^{2} \phi\left(C / m^{2}\right)$
(c) $\rho_{s}=\rho_{s o} e^{-r}\left(C / m^{2}\right)$
(d) $\rho_{s}=\rho_{s o} e^{-r} \sin ^{2} \phi\left(C / m^{2}\right)$
where $\rho_{\mathrm{so}}$ is a constant.

Q2. An infinitely long cylindrical shell extending from $r=1 \mathrm{~m}$ to $\mathrm{r}=3 \mathrm{~m}$ contains uniform charge density $\rho_{\mathrm{vo}}$. Using Gauss Law, find $\mathbf{D}$ in all directions.

Q3. Show that the electric potential difference $\mathrm{V}_{12}$ between two points in air at radial distances $r_{1}$ and $r_{2}$ from an infinite line of charge with density $\rho_{l}$ along the $z$-axis is

$$
V_{12}=\left(\rho_{1} / 2 \pi \varepsilon_{0}\right) \ln \left(r_{1} / r_{2}\right)
$$

## Home Assignment to be submitted and discussed during tutorial session.

Q1. Suppose we have two negative charges: one located at the origin and carrying charge -9C and the other located on the positive $x$-axis at a distance $d$ from the first charge with magnitude $-36 C$. Determine the location, polarity and magnitude of a third charge whose placement would bring the entire system into equilibrium. A charge system is in equilibrium if the force acting on any one charge is identical in magnitude and direction to the force acting on any of the other charges in the system.

Q2. Two infinite lines of charge, both parallel to the $z$-axis, lie in the $x-z$ plane, one with density $\rho_{I}$ and located at $x=a$ and the other with density $-\rho_{I}$ and located at $x=-a$. Obtain an expression for the electric potential $\mathrm{V}(\mathrm{x}, \mathrm{y})$ at a point $\mathrm{P}=(\mathrm{x}, \mathrm{y})$ relative to the potential at the origin.

