

Fields and Waves  
Tutorial-03 (February 2, 2016)

1. A 6-m section of 150- $\Omega$  lossless line is driven by a source with
$$v_s(t) = 5\cos(8\pi \times 10^7 t - 30^\circ) \text{ (V)}$$
and  $Z_s = 150 \Omega$ . If the line, which has a relative permittivity  $\epsilon_r = 2.25$ , is terminated in a load  $Z_L = (150 - j50) \Omega$ , determine:
  - (a) Electrical length of the line.
  - (b) The reflection coefficient at the load.
  - (c) The input impedance.
  - (d) The input voltage  $\tilde{V}_i$ .
  - (e) The time-domain input voltage  $v_i(t)$ .
2. A lossless transmission line of electrical length  $l = 0.35\lambda$  and characteristic impedance of 100  $\Omega$  is terminated in a load impedance of  $(60 + j30) \Omega$ . Find  $\Gamma$ ,  $S$ , and  $Z_{in}$ .
3. A 50- $\Omega$  lossless line terminated in a purely resistive load has a voltage standing-wave ratio of 3. Find all possible values of  $Z_L$ .
4. Convert:
  - a)  $(-1, 1, \sqrt{2})$  from Cartesian to spherical.
  - b)  $(1/2, (\sqrt{3})/2, 5)$  from Cartesian to cylindrical
  - c)  $(\sqrt{6}, \pi/4, \sqrt{2})$  from cylindrical to spherical.

Home Assignment Questions:

(To be submitted at the start of the tutorial and be subsequently discussed)

1. A 50- $\Omega$  lossless transmission line is terminated in a load with impedance  $Z_L = (30 - j50) \Omega$ . The wavelength is 8 cm. Find:
  - a) The reflection coefficient at the load
  - b) The standing-wave ratio on the line
  - c) The position of the voltage maximum nearest the load
  - d) The position of the current maximum nearest the load.
2. Express in the Cartesian coordinate system and mention what geometric shape/surface they signify (eg: if in Cartesian:  $z^2/a + y^2/b = 0$  - an ellipse with semi major/minor axis =  $a/b$  at a height of  $x=c$ ):
  - a)  $r=3$
  - b)  $\rho=5; z=10$