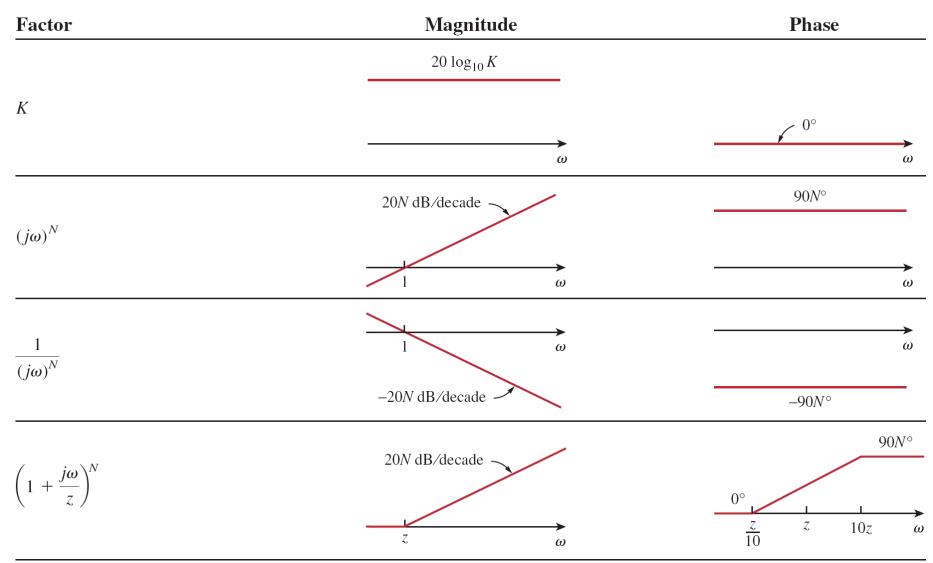
# <u>Lecture – 16</u>

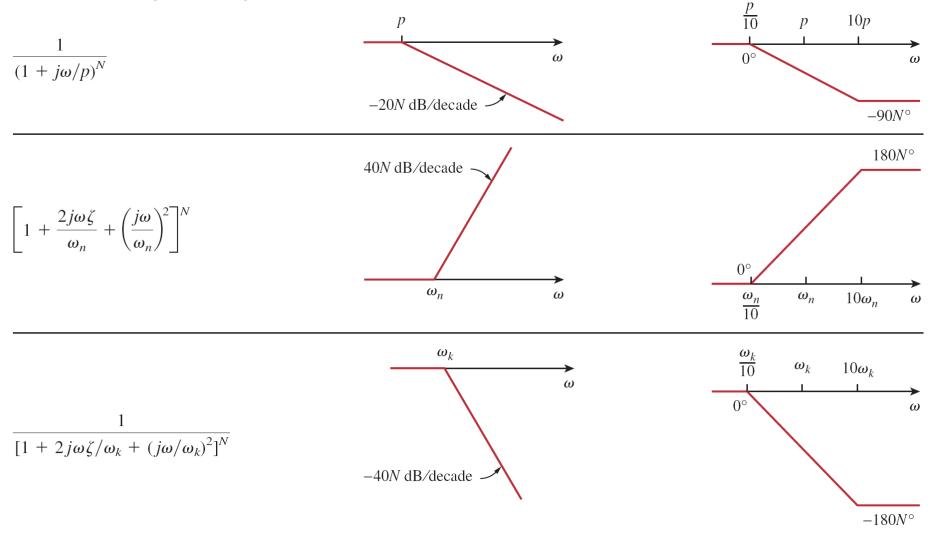
# Date: 03.10.2017

• Frequency Response (Contd.)

## **Bode Plot (contd.)**



## **Bode Plot (contd.)**



## Bode Plot (contd.)

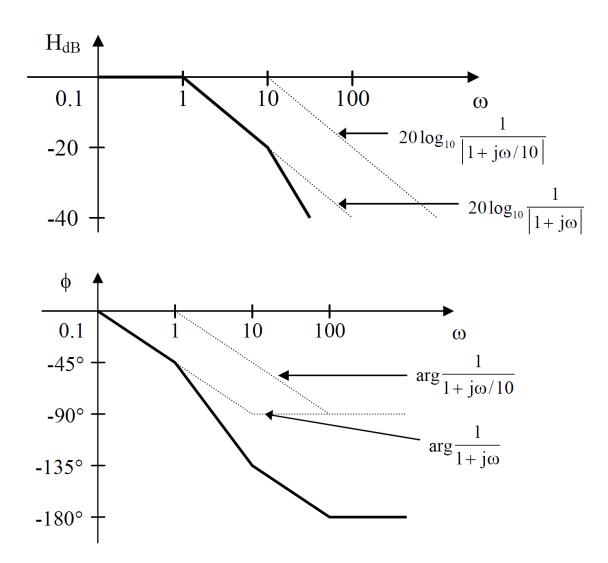
- not every transfer function has all seven factors.
- To sketch the Bode plots for a generic function  $H(\omega)$ , we first record the corner frequencies on the semilog graph paper, and sketch the factors one at a time as discussed.
- Then combine additively the graphs of the factors.
- The combined graph is usually drawn from left to right, changing the slopes appropriately each time a corner frequency is encountered.

## Example – 1

A ladder network has a voltage gain of  $\mathbf{H}(\omega) = \frac{10}{(1+j\omega)(10+j\omega)}$ 

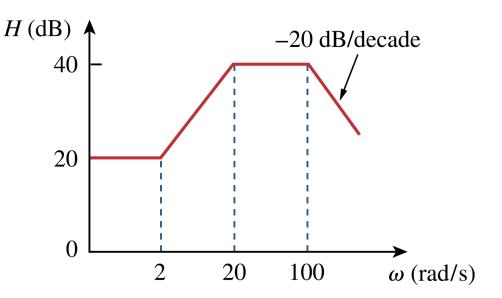
Sketch the Bode plots for the gain.

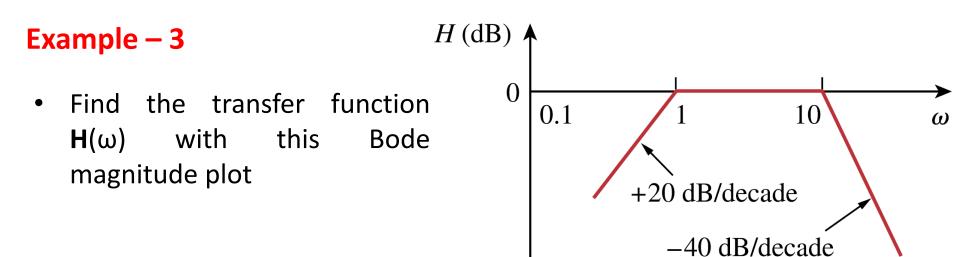
## Solution – 1



#### Example – 2

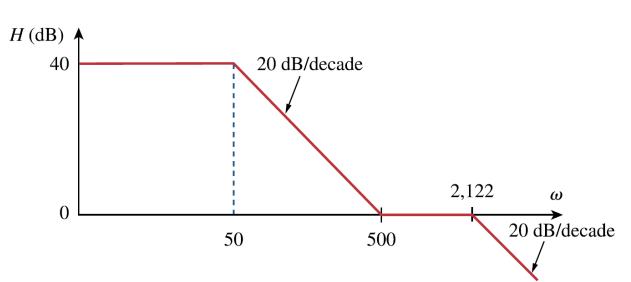
Find the transfer function
H(ω) with this Bode
magnitude plot





#### Example – 4

This magnitude plot represents the transfer function of a preamplifier. Find *H*(*s*).

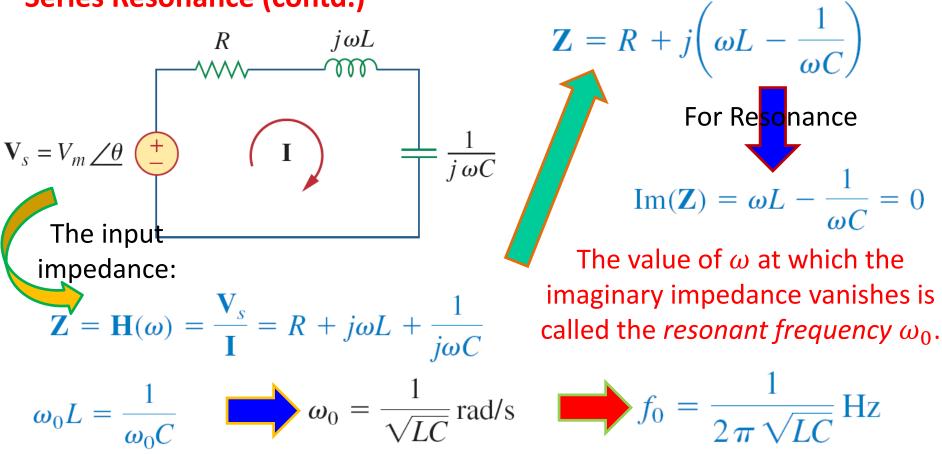


## **Series Resonance**

- Resonance occurs in any system having a complex conjugate pair of poles; due to oscillations of stored energy from one form to another.
- It allows frequency discrimination in communications networks.

Resonance is a condition in an *RLC* circuit in which the capacitive and inductive reactances are equal in magnitude, thereby resulting in a purely resistive impedance.

Resonant circuits (series or parallel) are useful for constructing highly frequency selective filters. They are used in many applications such as selecting the desired stations in radio and TV receivers.

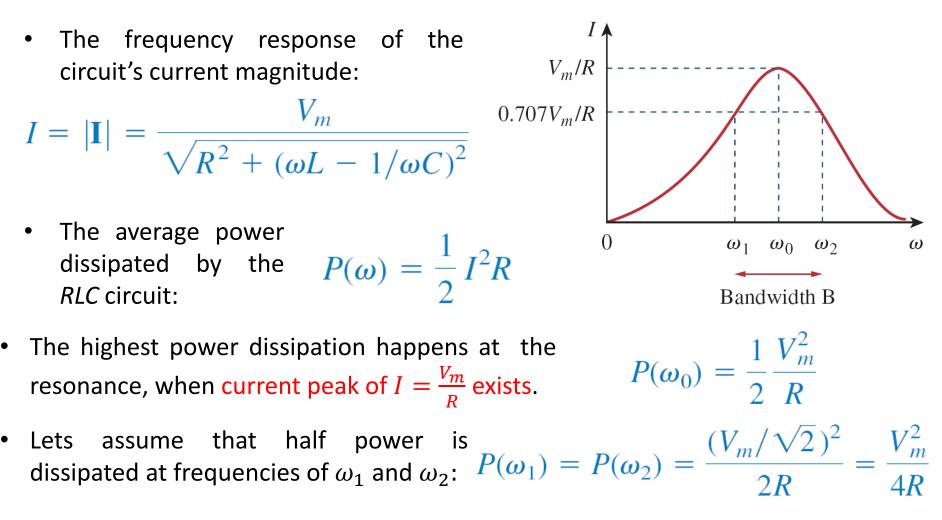


At resonance:

- The impedance is purely resistive, i.e., the *LC* series combination acts like a short circuit, and the entire voltage is across *R*.
- Voltage and Current are in phase and therefore the power factor is unity.

At resonance:

- The magnitude of the transfer function is minimum.
- The inductor and capacitor voltages can be much more than the source voltage.

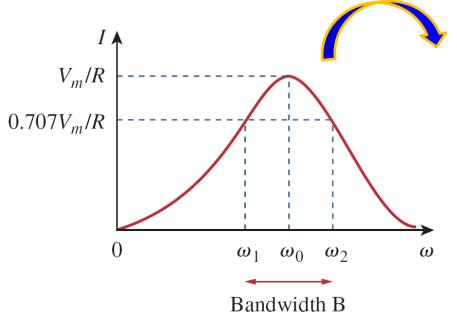


• The half-power frequencies can be obtained by setting Z equal to  $\sqrt{2}$ R.

$$\sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2} = \sqrt{2}R$$

$$\omega_{1} = -\frac{R}{2L} + \sqrt{\left(\frac{R}{2L}\right)^{2} + \frac{1}{LC}}$$
$$\omega_{2} = \frac{R}{2L} + \sqrt{\left(\frac{R}{2L}\right)^{2} + \frac{1}{LC}}$$
$$\omega_{0} = \sqrt{\omega_{1}\omega_{2}}$$

In general  $\omega_1$  and  $\omega_2$  are not symmetrical around the resonant frequency, because the frequency response is not generally symmetrical.



The height of the curve is determined by *R*, the width of the curve depends on the *bandwidth B* defined as:

$$B=\omega_2-\omega_1$$

B is essentially the half-power bandwidth, because it is the width of the frequency band between the half-power frequencies.

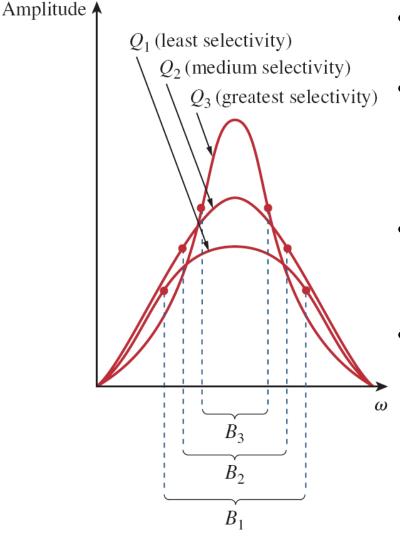
 The sharpness of the resonance in a circuit is measured by the *quality factor Q*

The *quality factor Q* relates the peak energy stored to the energy dissipated in the circuit per cycle of oscillation.

 $Q = 2\pi \frac{\text{Peak energy stored in the circuit}}{\text{Energy dissipated by the circuit}}$ in one period at resonance

The *quality factor Q* is also a measure of the energy storage property of a circuit in relation to its energy dissipation property

The quality factor of a resonant circuit is the ratio of its resonant frequency to its bandwidth.



- higher  $Q \rightarrow$  more selective circuit  $\rightarrow$  smaller the bandwidth.
- selectivity of an RLC circuit ↔ ability of the circuit to respond to a certain frequency and discriminate against all other frequencies.
- For narrow band of frequencies to be selected or rejected ↔ Q of the resonant circuit must be high.
- If the band of frequencies is wide, the quality factor must be low.

- A resonant circuit is designed to operate at or near its resonant frequency.
- It is said to be a *high-Q circuit* when its quality factor is equal to or greater than 10 ( $Q \ge 10$ ).
- For high-Q circuits the half-power frequencies are, for all practical purposes, symmetrical around the resonant frequency and can be approximated as:

$$\omega_1 \simeq \omega_0 - \frac{B}{2}, \qquad \omega_2 \simeq \omega_0 + \frac{B}{2}$$

a resonant circuit is characterized by five related parameters: the two half-power frequencies  $\omega_1$  and  $\omega_2$ , the resonant frequency  $\omega_0$ , the bandwidth *B*, and the quality factor *Q*.

#### Example – 5

A series *RLC* network has  $R = 2 \text{ k}\Omega$ , L = 40 mH, and  $C = 1 \mu\text{F}$ . Calculate the impedance at resonance and at one-fourth, one-half, twice, and four times the resonant frequency.

#### Example – 6

A coil with resistance  $3\Omega$  and inductance 100 mH is connected in series with a capacitor of 50 pF, a resistor of  $6\Omega$  and a signal generator that gives 110 V rms at all frequencies. Calculate  $\omega_0$ , Q, and B at resonance of the resultant series *RLC* circuit.

#### Example – 7

Design a series *RLC* circuit with *B* = 20 rad/s and  $\omega_0 = 1,000$  rad/s. Find the circuit's *Q*, L and C. Let *R* = 10 $\Omega$ .