



Lecture – 6

Date: 24.08.2015

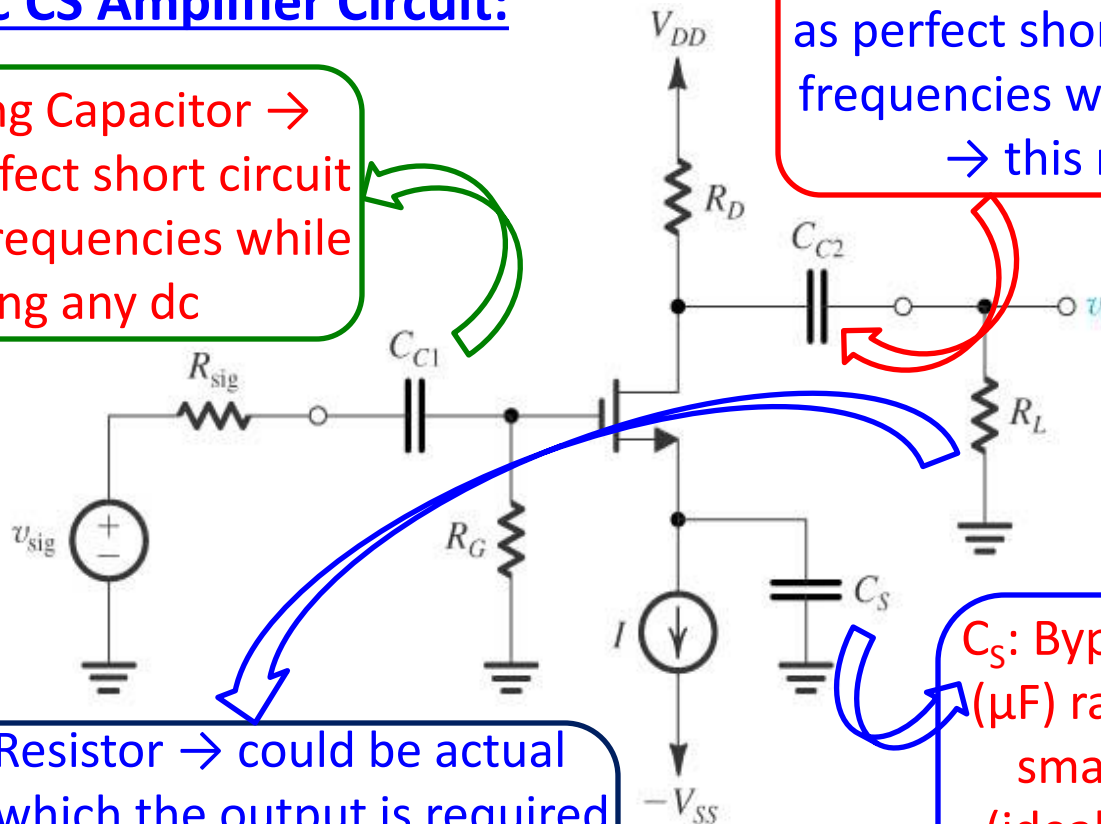
- Common Source Amplifier
- MOSFET Amplifier Distortion

Example – 1

One Realistic CS Amplifier Circuit:

C_{c1} : Coupling Capacitor \rightarrow serves as perfect short circuit at all signal frequencies while blocking any dc

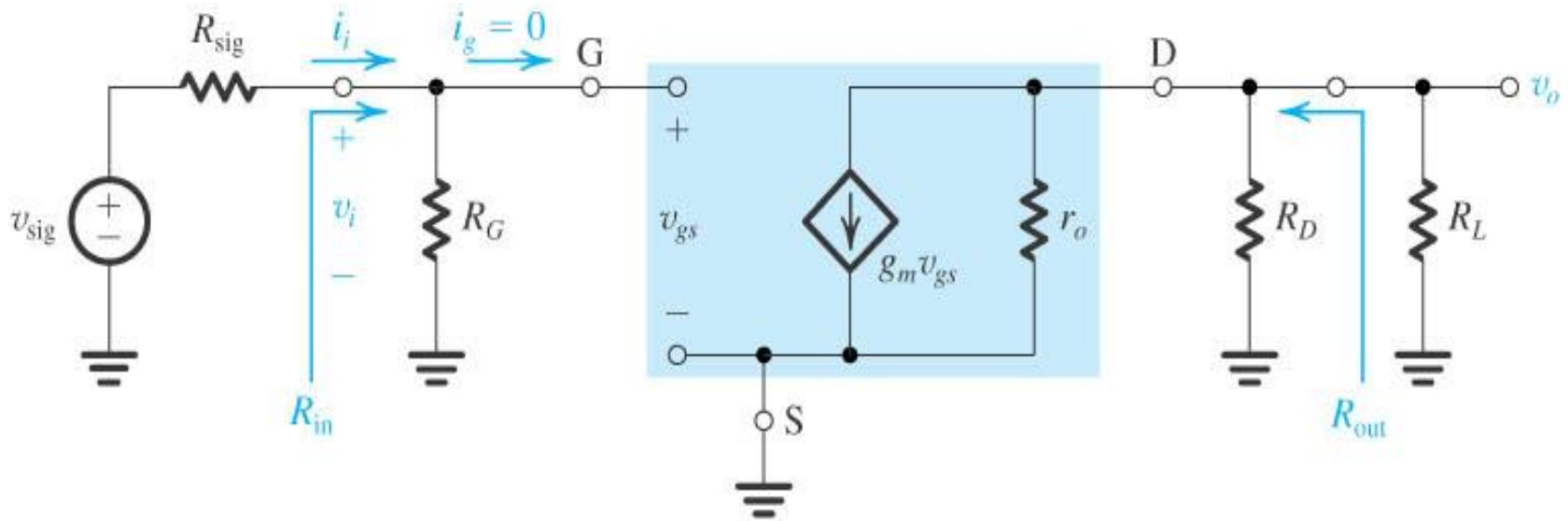
C_{c2} : Coupling Capacitor \rightarrow serves as perfect short circuit at all signal frequencies while blocking any dc \rightarrow this makes $v_o = v_d$



R_L : Load Resistor \rightarrow could be actual resistor to which the output is required or could be input resistance of another amplifier stage where more than one amplification stage is needed

C_S : Bypass Capacitor \rightarrow (μ F) range \rightarrow provides small impedances (ideally perfect short circuit) at all signal frequencies

Example – 1 (contd.)



$$i_g = 0$$

$$R_{in} = R_G$$

$$v_i = v_{sig} \frac{R_{in}}{R_{in} + R_{sig}} \Rightarrow v_i = v_{sig} \frac{R_G}{R_G + R_{sig}}$$

Usually, R_G is very high (of the order of M Ω) and therefore: $v_i \cong v_{sig}$

Now, $v_{gs} = v_i \Rightarrow v_o = -g_m v_{gs} (r_o \parallel R_D \parallel R_L)$

$$\therefore A_v = \frac{v_o}{v_{in}} = \frac{v_o}{v_{gs}} = -g_m (r_o \parallel R_D \parallel R_L)$$

Example – 1 (contd.)

Open Loop Voltage Gain (ie, when there is no feedback loop from o/p to the i/p) is:

$$A_{vo} = -g_m (r_o \parallel R_D)$$

The overall voltage gain from the signal-source to the load is:

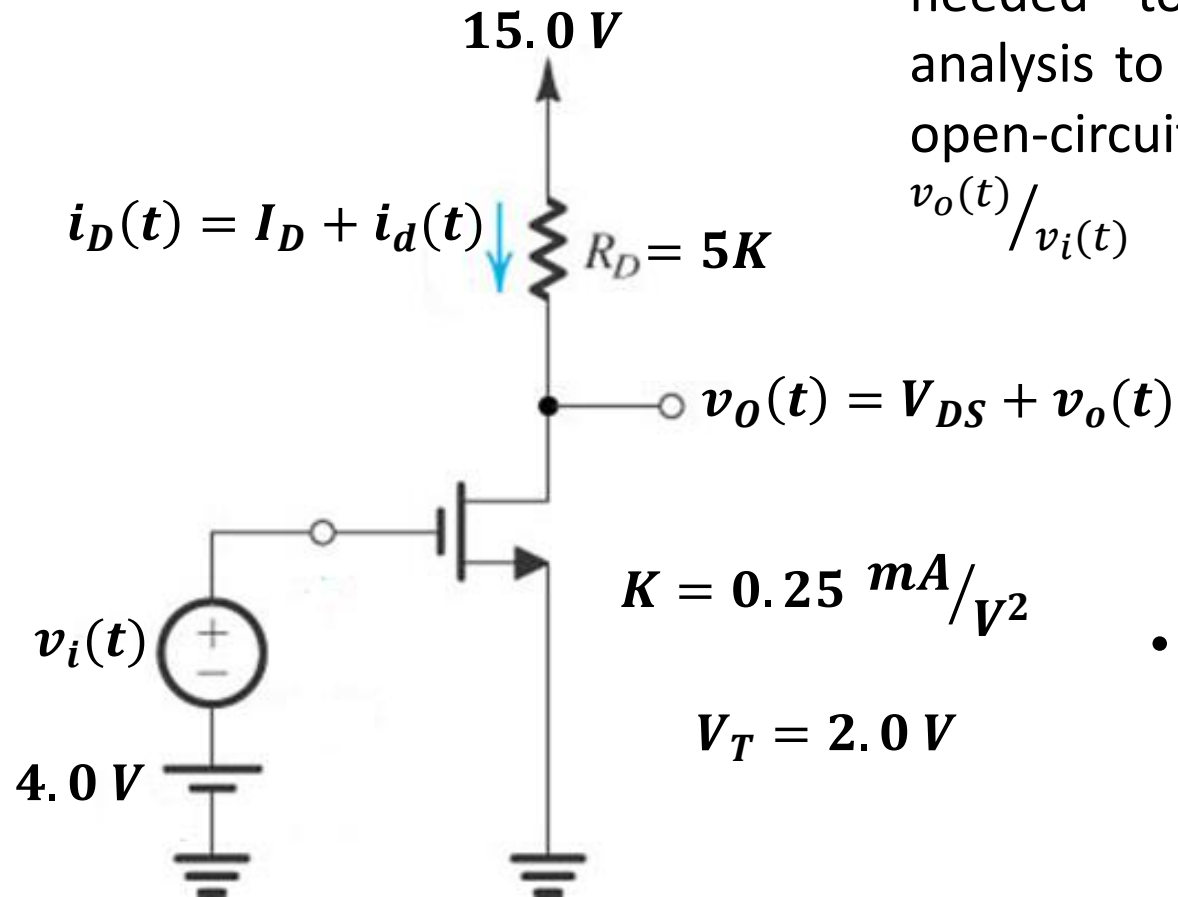
$$G_v = -\frac{R_G}{R_G + R_{sig}} g_m (r_o \parallel R_D \parallel R_L)$$

For the determination of R_{out} , the signal v_{sig} has to be set to zero (replace the signal generator with a short circuit) → simple inspection gives:

$$R_{out} = (r_o \parallel R_D)$$

It is apparent that inclusion of r_o slightly decreases the gain and the output impedance → in many applications lower R_{out} is beneficial

MOSFET Amplifier Distortion



Lets look at the last example. You needed to perform a small-signal analysis to determine the small-signal open-circuit **voltage gain** $A_v = v_o(t)/v_i(t)$

- We found that the small-signal **voltage gain** is:

$$A_v = \frac{v_o(t)}{v_i(t)} = -5.0$$

MOSFET Amplifier Distortion (contd.)

- Say the **input** voltage to this amplifier is: $v_i(t) = V_i \cos \omega t$

Q: What is the **largest** value that V_i can take without producing a **distorted** output?

A: Well, we know that the **small-signal output** is:
$$v_o(t) = A_{v_o} v_i(t) = -5.0 V_i \cos \omega t$$

BUT, this is **not** the output voltage!

→ The **total** output voltage is the **sum** of the **small-signal** output voltage and the **DC** output voltage!

- Note for this example, the **DC output** voltage is the **DC drain** voltage, and we recall we determined in an earlier handout that its value is:

$$V_O = V_D = 10 \text{ V}$$

MOSFET Amplifier Distortion (contd.)

- Thus, the **total output voltage** is :
$$v_o(t) = V_D + v_o(t)$$
$$= 10.0 - 5.0 V_i \cos \omega t$$



*It is very important that you realize there is a **limit** on both how high and how low the **total** output voltage $v_o(t)$ can go.*

*That's right! If the **total** output voltage $v_o(t)$ tries to exceed these limits—even for a moment—the MOSFET will leave **saturation mode**.*



MOSFET Amplifier Distortion (contd.)



And leaving saturation mode results in signal distortion!

- Let's break the problem down into **two** separate problems:

- 1)** If **total** output voltage $v_o(t)$ becomes too small, the MOSFET will enter the **triode** mode
- 2)** If **total** output voltage $v_o(t)$ becomes too large, the MOSFET will enter the **cutoff** mode

MOSFET Amplifier Distortion (contd.)

We'll first consider **problem 1.**

- For a MOSFET to remain in saturation, $v_{DS}(t)$ must remain greater than the excess gate voltage $V_{GS} - V_T$ all the time t .

$$v_{DS}(t) > V_{GS} - V_T$$

- Since the source terminal of the MOSFET in **this** circuit is connected to ground, we know that $V_S = 0$. Therefore:

$$v_{DS}(t) = v_D(t) = v_O(t) \qquad V_{GS} = V_G$$

- And so the MOSFET will remain in saturation **only** if the total output voltage remains **larger** than $V_{GS} - V_T = V_G - V_T$.

$$v_O(t) > V_{GS} - V_T$$

- Thus, we conclude for this amplifier that the output “floor” is: $L_- = V_G - V_t$

MOSFET Amplifier Distortion (contd.)

- Here, $V_{GS} = 4.0\text{ V}$ and $V_T = 2.0\text{ V}$. Therefore: $V_{GS} - V_T = 4 - 2 = 2.0\text{ V}$
- Thus, to remain in saturation, the **total** output voltage must remain larger than the “floor” voltage at all time t . $v_o(t) > V_{GS} - V_T = 2.0\text{ V}$
- Since this **total** voltage is: $v_o(t) = 10.0 - 5.0 V_i \cos \omega t$

- we can determine the **maximum** value of small-signal **input** magnitude:

$$10.0 - 5.0 V_i \cos \omega t > 2.0$$

$$\Rightarrow 8.0 > 5.0 V_i \cos \omega t$$

$$\Rightarrow V_i \cos \omega t < 1.6$$

- Since $\cos \omega t$ can be as large as 1.0, we find that the **magnitude** of the **input** voltage can be **no larger** than 1.6 V, i.e.,

$$V_i < 1.6\text{ V}$$

If the **input** magnitude exceeds this value, the MOSFET will (momentarily) leave the saturation region and enter the dreaded **triode** mode!

MOSFET Amplifier Distortion (contd.)

Now let's consider problem 2

- For the MOSFET to remain in saturation, the **drain** current must be **greater** than zero ($i_D > 0$). Otherwise, the MOSFET will enter **cutoff** mode.
- Applying **Ohm's Law** to the drain resistor, we find the **drain current** is:

$$i_D = \frac{V_{DD} - v_O}{R_C} = \frac{15 - v_O}{5}$$
- it is evident that drain current is **positive** only if: $v_O < 15 V$
- In other words, the **upper** limit (i.e., the “ceiling”) on the **total** output voltage is:

$$L_+ = V_{DD} = 15.0 V$$
- Since this **total** voltage is: $v_O(t) = 10.0 - 5.0 V_i \cos \omega t$
- we can conclude that in order for the MOSFET to remain in **saturation** mode:

$$10.0 - 5.0 V_i \cos \omega t > 15.0$$

MOSFET Amplifier Distortion (contd.)

- Therefore, we find: $V_i \cos \omega t > \frac{-5.0}{5.0} = -1.0$
- Since $\cos \omega t$ can be as large as 1.0, we find that the **magnitude** of the **input** voltage can be **no larger** than: $V_i < 1.0 \text{ V}$

If the input magnitude **exceeds** 1.0 V, the MOSFET will (momentarily) leave the saturation and enter the **cutoff** region!

In summary:

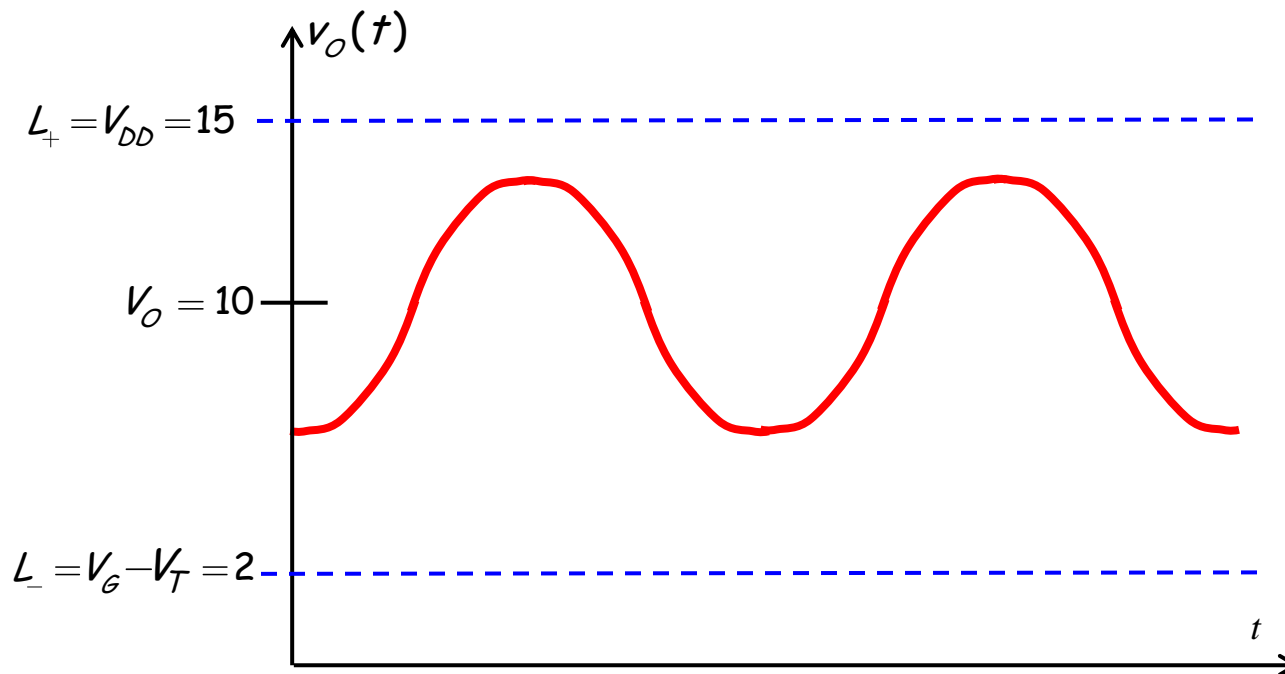
- 1) If, $V_i > 1.6 \text{ V}$, the MOSFET will at times enter **triode**, and **distortion** will occur!
- 2) If, $V_i > 1.0 \text{ V}$, the MOSFET will at times enter **cutoff**, and **even more** distortion will occur!

MOSFET Amplifier Distortion (contd.)

- To demonstrate this, let's consider **three** examples:

1. $V_i < 1.0 V$

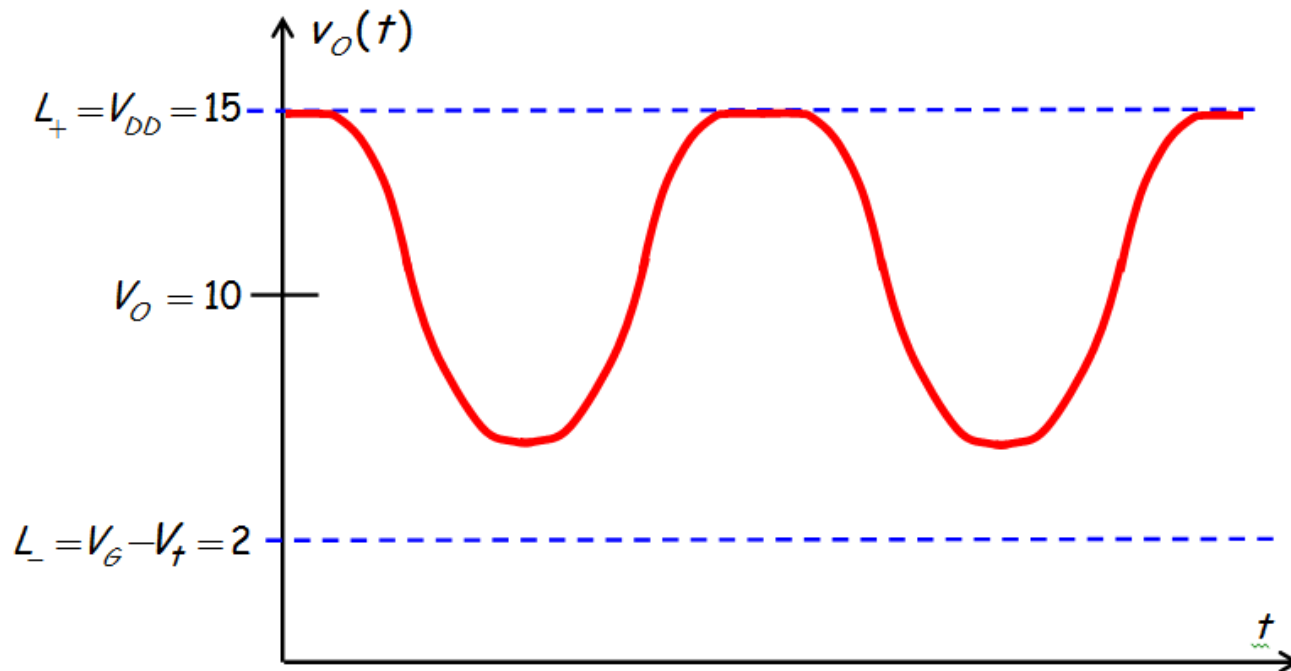
- The output signal in this case remains between $V_{DD} = 15.0V$ and $V_G - V_T = 2.0 V$ for **all** time t . Therefore, the output signal is **not distorted**.



MOSFET Amplifier Distortion (contd.)

2. $1.6\text{ V} > V_i > 1.0\text{ V}$

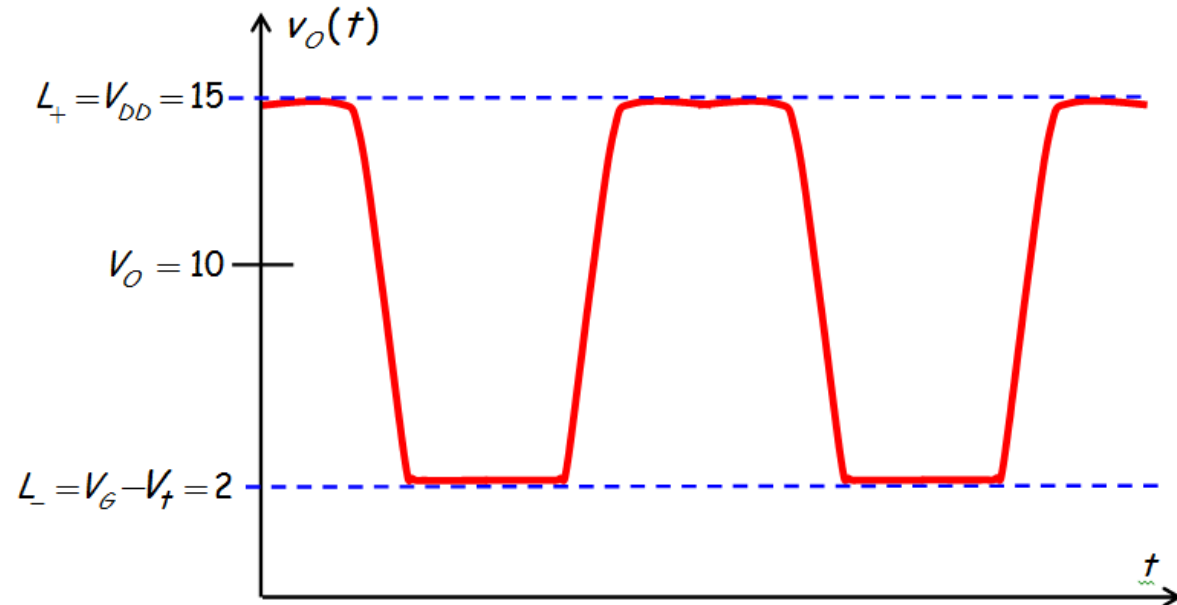
- The output signal in this case remains greater than $L_- = V_G - V_T = 2$ for all time t . However, the small-signal output is now large enough so that the total output voltage at times tries to **exceed** $L_+ = V_{DD} = 15$. For these times, the MOSFET will enter **cutoff**, and the output signal will be **distorted**.



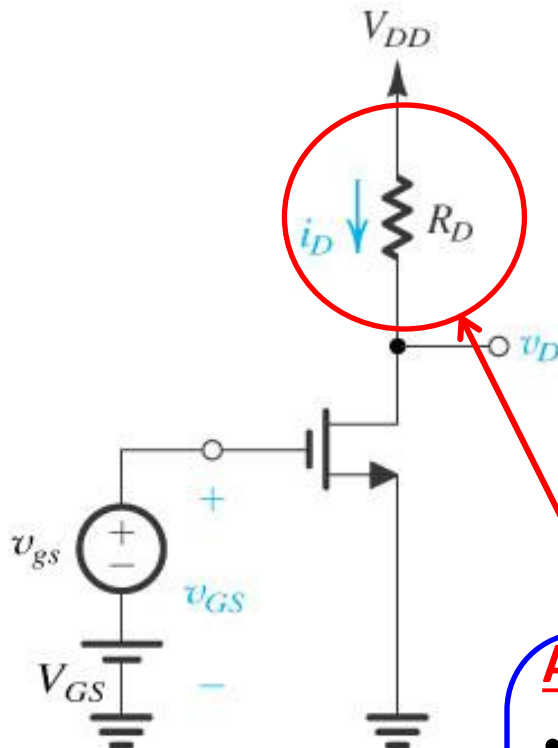
MOSFET Amplifier Distortion (contd.)

3. $V_i > 1.6 V$

- In this case, the small-signal input signal is sufficiently **large** so that the total output will attempt to exceed **both** limits (i.e., $V_{DD} = 15.0 V$ and $V_G - V_T = 2.0 V$). Therefore, there are periods of time when the MOSFET will be in **cutoff**, and periods when the MOSFET will be in **saturation**.



Common Source (CS) Amplifier



Major Limitations:

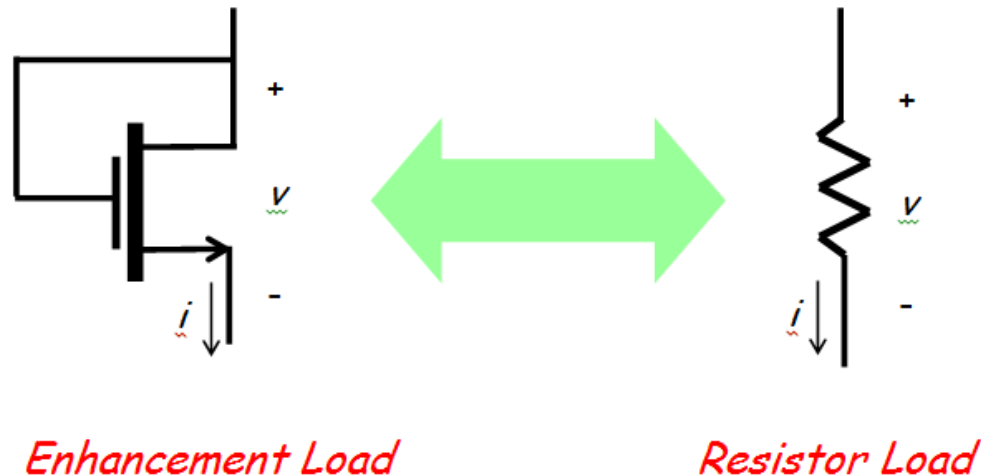
- Increase in A_v by increasing the R_D leads to smaller V_D i.e, the voltage $V_{DS} \rightarrow$ essentially limits the voltage swing
- R_D difficult to fabricate in smaller chip area \rightarrow a major constraint for ICs
- Problems with the precision of R_D

Active loads overcome these problems

- Diode-connected load (FETs in which drain and gate are tied to work as resistors)
- Current source (such as a FET operating in saturation mode)
- FET operating in triode mode

Diode-Connected Load or Enhancement Load

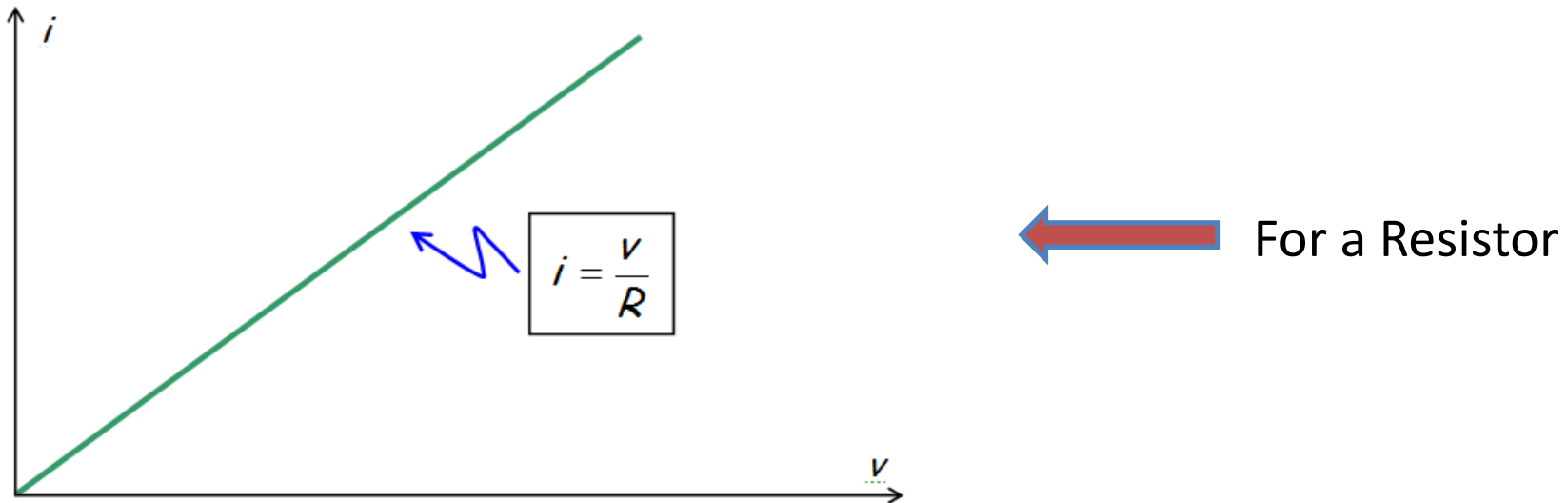
- We can make a two terminal device from a MOSFET by **connecting** the gate and the drain!



Q: How does this “**enhancement load**” resemble a resistor?

A: For this we need to consider the i - v curves for both.

Diode-Connected Load (contd.)

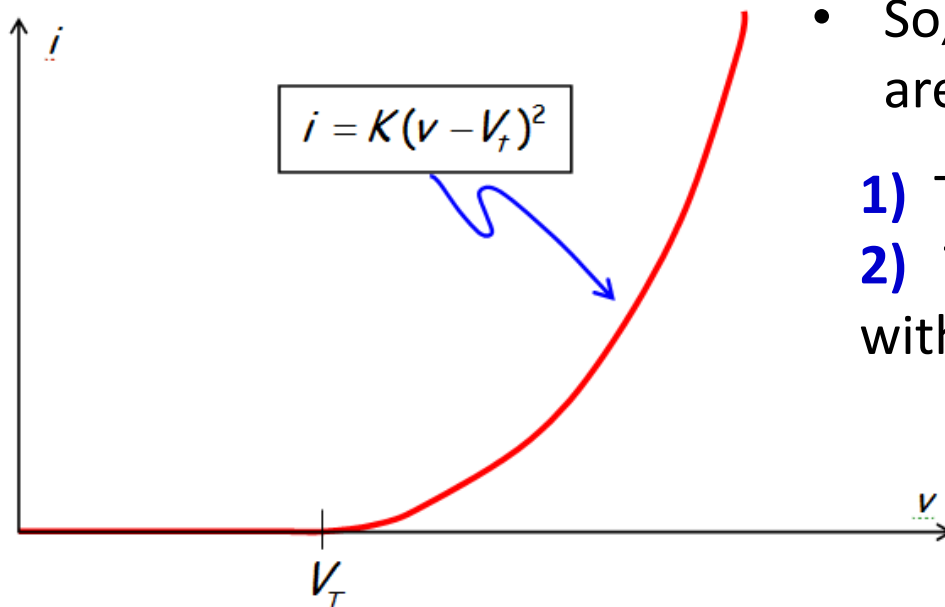


- Now consider the same curve for an **enhancement load**.
 - Since the gate is tied to the drain, we find $v_G = v_D$, and thus $v_{GS} = v_{DS}$. As a result, we find that $v_{DS} > v_{GS} - V_T$ **always**.
 - Therefore, we find that if $v_{GS} > V_T$, the MOSFET will be in **saturation** ($i_D = K(v_{GS} - V_T)^2$), whereas if $v_{GS} < V_T$, the MOSFET is in **cutoff** ($i_D = 0$).

Diode-Connected Load (contd.)

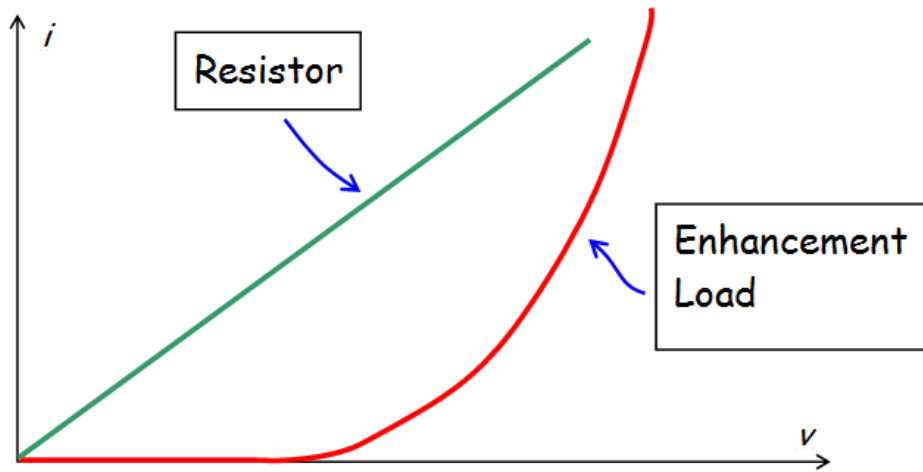
- Since for enhancement load $i = i_D$ and $v = v_{GS}$, we can describe the enhancement load as:

$$i = \begin{cases} 0 & \text{for } v < V_T \\ K(v - V_T)^2 & \text{for } v > V_T \end{cases}$$

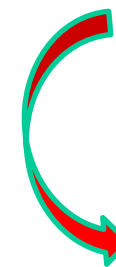


- So, resistors and enhancement loads are far from **exactly** the same, but:
 - 1) They **both** have $i = 0$ when $v = 0$.
 - 2) They **both** have increasing current i with increasing voltage v .

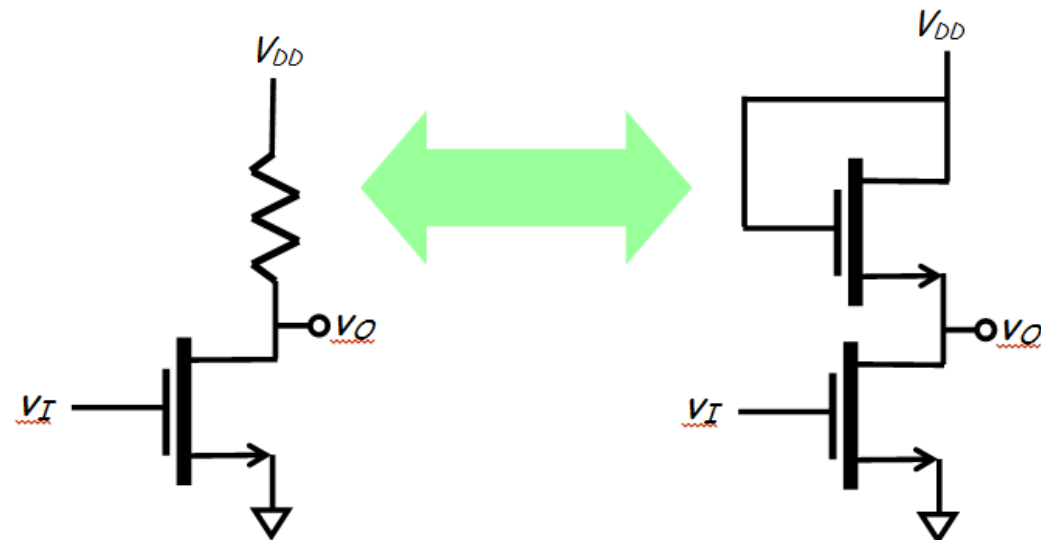
Diode-Connected Load (contd.)



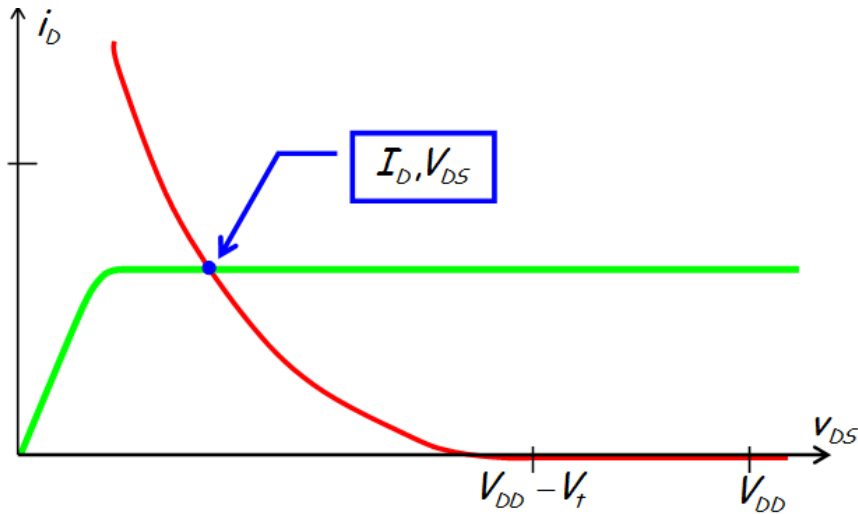
Therefore, we can build a **common source** amplifier with either a resistor, or in the case of an **integrated circuit**, an enhancement load.



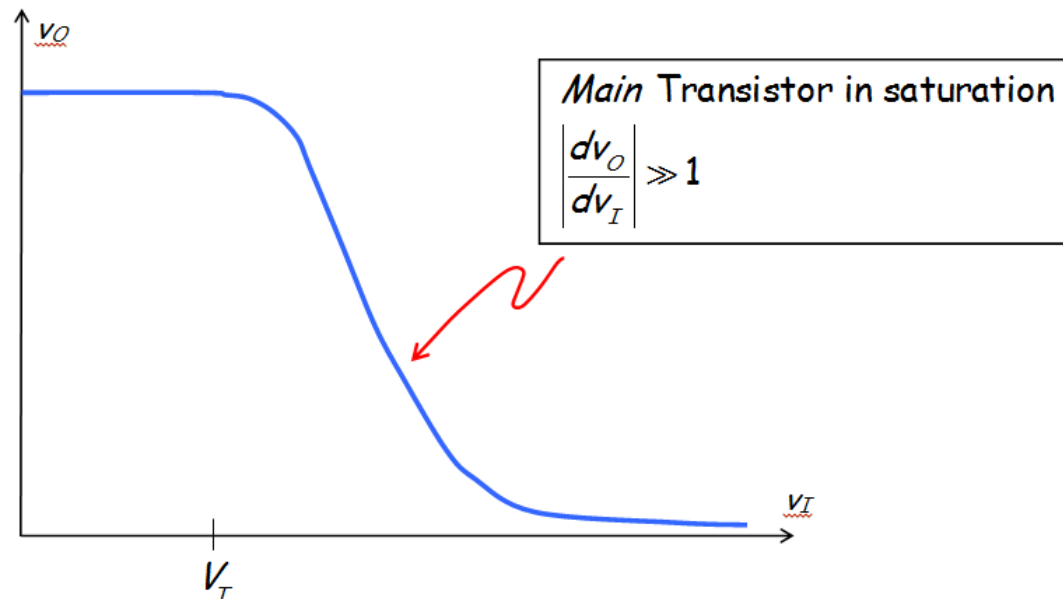
For the diode-connected load amplifier, the **load line** is replaced with a **load curve** ($v = V_{DD} - v_{DS}$)!



Diode-Connected Load (contd.)



And the **transfer function** of the CS Amplifier is:

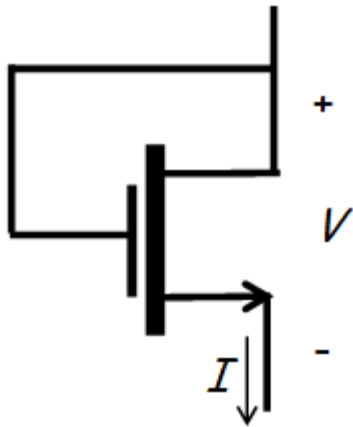


Diode-Connected Load (contd.)

Q: What is the **small signal** behavior of an enhancement load?

A: The enhancement load is made of a MOSFET device, and we **understand** the small-signal behavior for a MOSFET!

Step 1 - DC Analysis



If, $V > V_T$ then $I = K(V - V_T)^2$ or:

$$V = \sqrt{\frac{I}{K}} + V_T$$

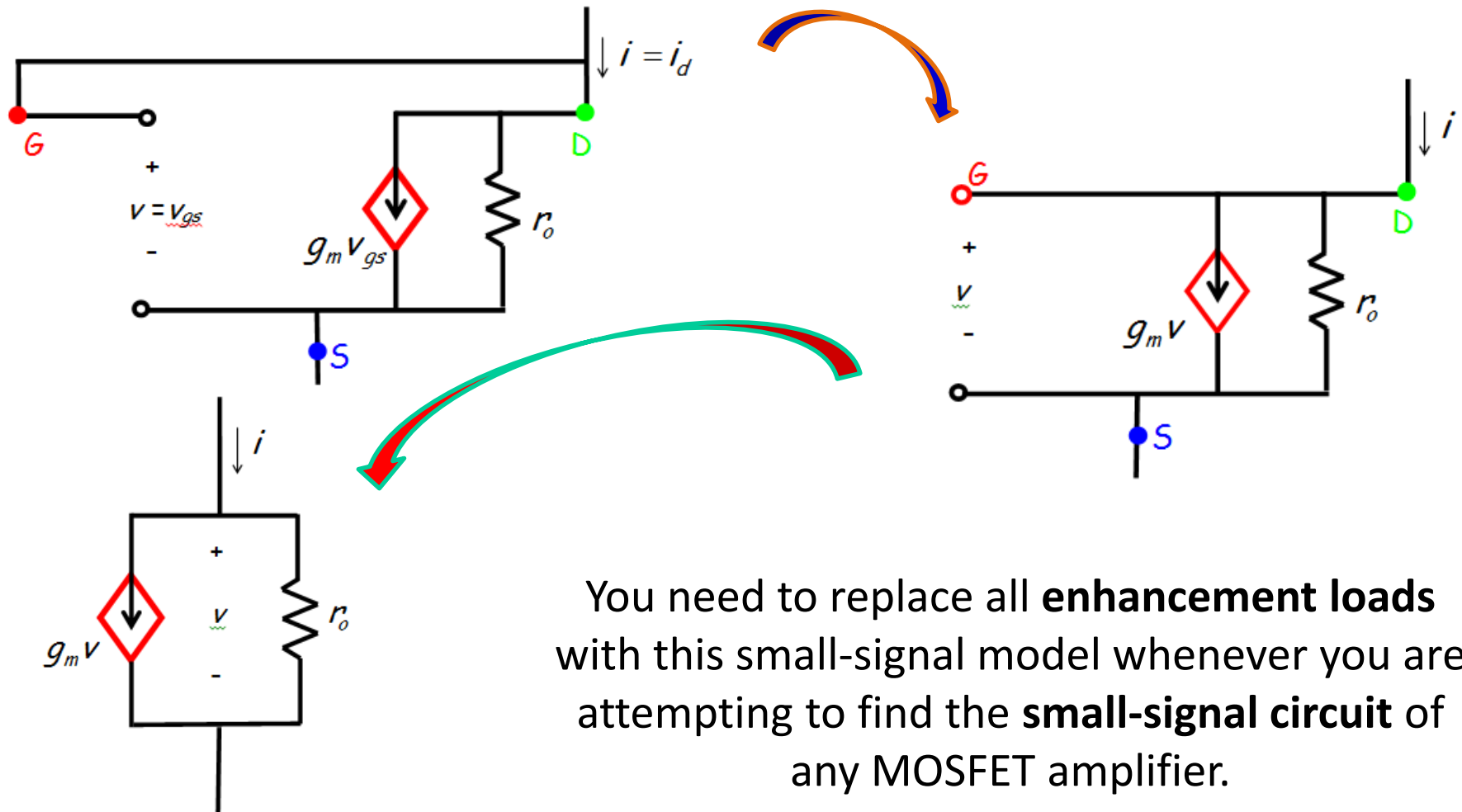
$$g_m = 2K(V_{GS} - V_T) = 2K(V - V_T)$$

Step 2 – Determine g_m and r_o

$$r_o = \frac{1}{\lambda I_D} = \frac{1}{\lambda I} = \frac{1}{\lambda K(V - V_T)^2}$$

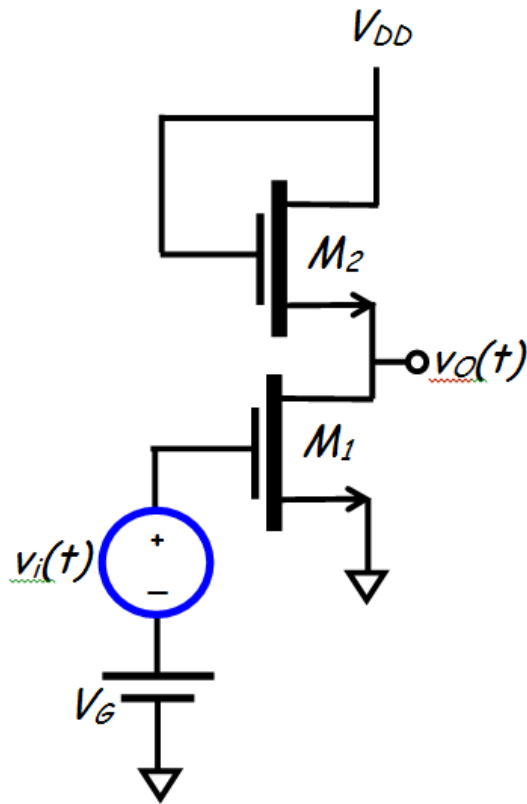
Diode-Connected Load (contd.)

Step 3 – Determine the small-signal circuit



You need to replace all **enhancement loads** with this small-signal model whenever you are attempting to find the **small-signal circuit** of any MOSFET amplifier.

CS Amplifier with Diode-connected load

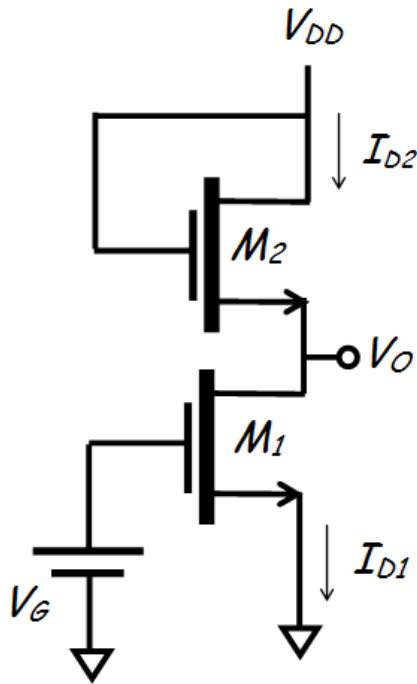


Q: What is the small-signal open-circuit voltage gain, input resistance, and output resistance of this amplifier?

A: The values that we will determine when we follow precisely the same steps as before!!

CS Amplifier with Diode-connected load (contd.)

Step 1 – DC Analysis



Note that:

$$I_{D1} = I_{D2} \doteq I_D$$

and that:

$$V_{GS1} = V_G - 0 = V_G$$

and also that:

$$V_{DS2} = V_{GS2}$$

and finally that:

$$V_{DS1} = V_{DD} - V_{DS2}$$

- Let's of course **ASSUME** that both M_1 and M_2 are in saturation. Therefore we **ENFORCE**:

$$\begin{aligned} I_{D1} &= K_1 (V_{GS1} - V_{T1})^2 \\ &= K_1 (V_G - V_{T1})^2 \end{aligned}$$

- Continuing with the **ANALYSIS**, we can find the drain current through the enhancement load (I_{D2}),

$$I_{D2} = K_2 (V_{GS2} - V_{T2})^2$$

CS Amplifier with Diode-connected Load (contd.)

$$I_{D1} = I_{D2}$$

$$K_1 (V_G - V_{T1})^2 = K_2 (V_{GS2} - V_{T2})^2 \quad \longrightarrow \quad V_{GS2} = \sqrt{\frac{K_1}{K_2}} (V_G - V_{T1}) + V_{T2}$$

- Since $V_{DS2} = V_{GS2}$ and $V_{DS1} = V_{DD} - V_{DS2}$, we can likewise state that:

$$V_{DS2} = \sqrt{\frac{K_1}{K_2}} (V_G - V_{T1}) + V_{T2} \qquad V_{DS1} = V_{DD} - V_{T2} - \sqrt{\frac{K_1}{K_2}} (V_G - V_{T1})$$

Now, we must **CHECK** to see if our assumption is correct.

- The saturation assumption will be correct if:

$$V_{DS1} > V_{GS1} - V_{T1} \qquad V_{GS1} > V_{T1} \quad \therefore \text{if } V_G > V_{T1}$$

$$> V_G - V_{T1}$$

CS Amplifier with Diode-connected Load (contd.)

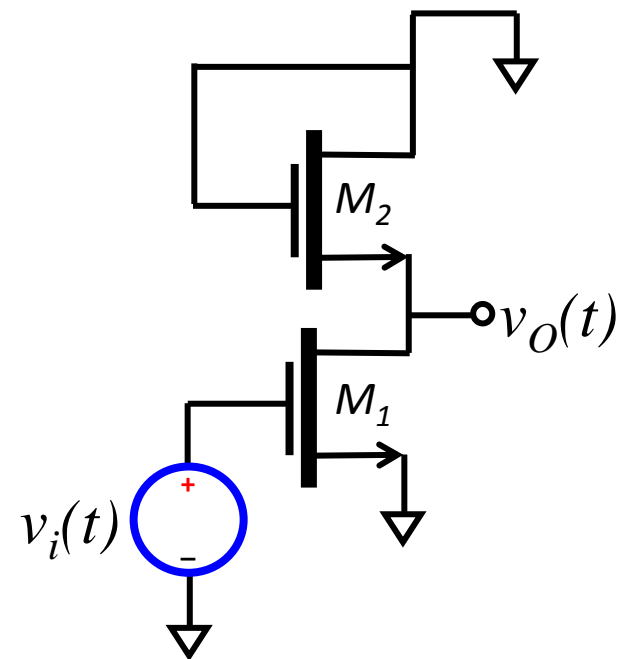
Step 2 – Calculate small-signal parameters

$$g_{m1} = 2K_1(V_G - V_{T1}) \quad \text{and} \quad g_{m2} = 2K_2(V_{GS2} - V_{T2})$$

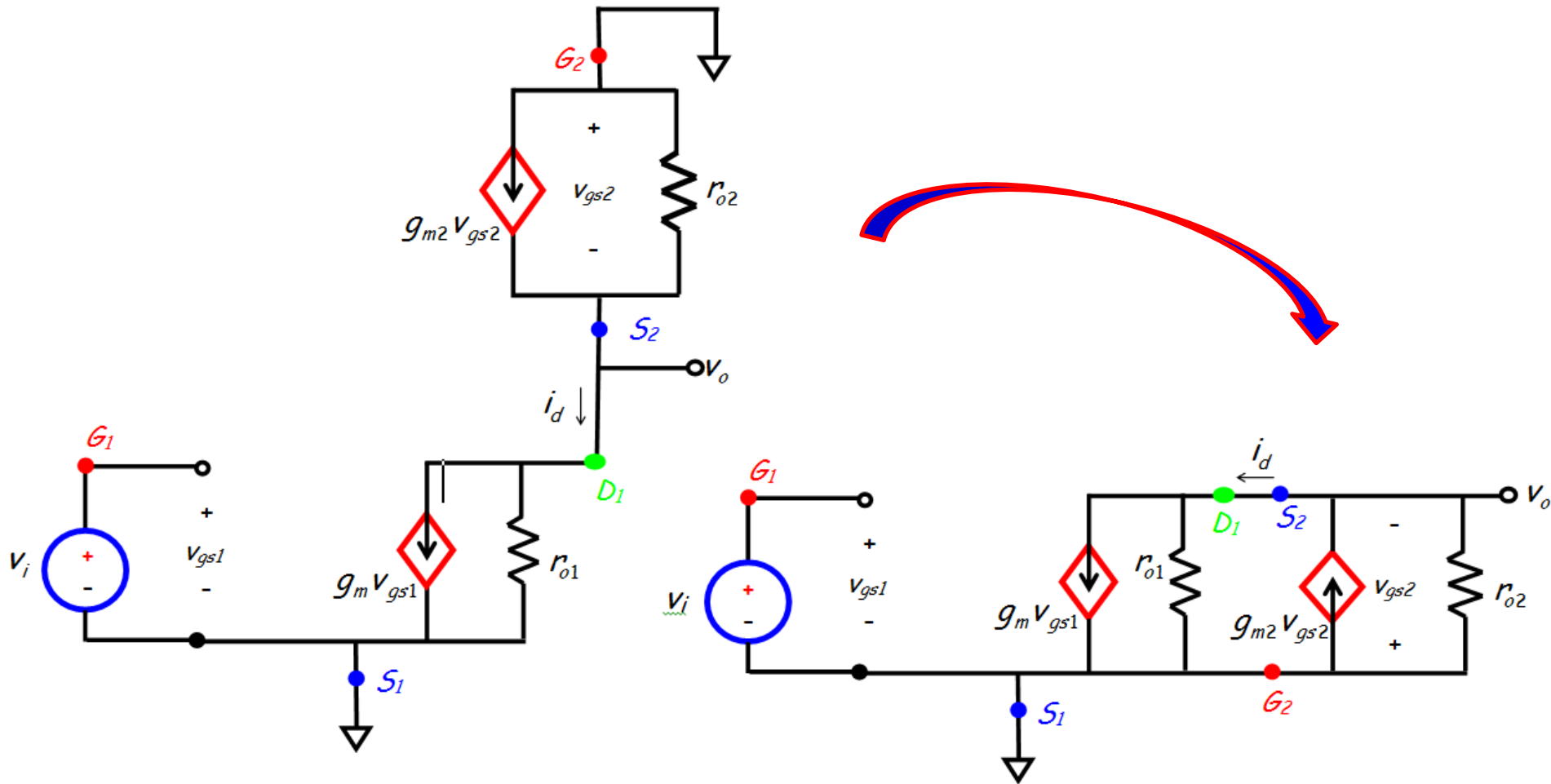
$$r_{o1} = \frac{1}{\lambda_1 I_D} \quad \text{and} \quad r_{o2} = \frac{1}{\lambda_2 I_D}$$

Step 3 – Determine the small-signal circuit

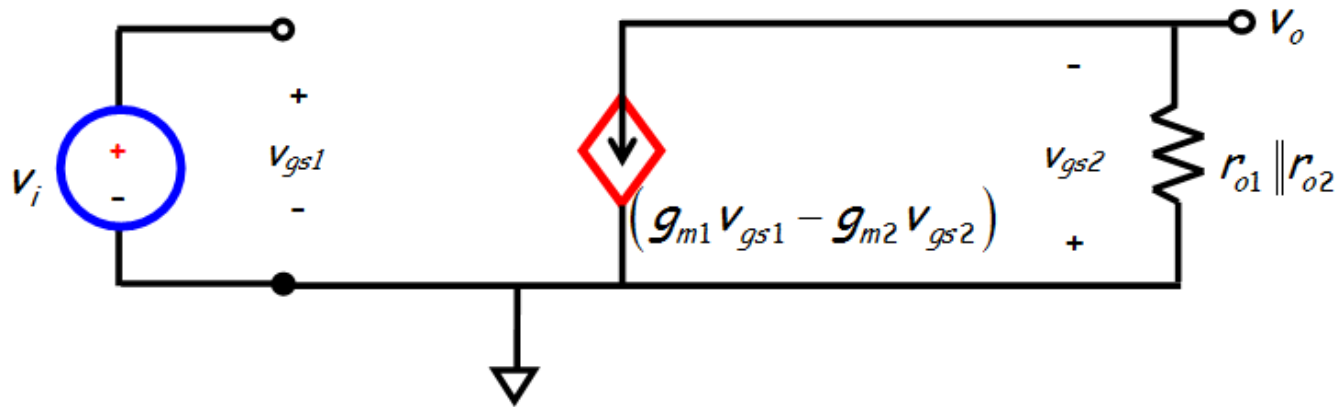
- First, let's turn off the DC sources:
- We now replace **MOSFET** M_1 with its equivalent small-signal model, **and** replace the **diode-connected load** with its equivalent small-signal model.



CS Amplifier with Diode-Connected Load (contd.)



CS Amplifier with Diode-Connected Load (contd.)



- We find that: $v_{gs1} = v_i$ $v_{gs2} = -v_o$

$$\begin{aligned} v_o &= -(g_{m1} v_{gs1} - g_{m2} v_{gs2}) (r_{o1} \parallel r_{o2}) \\ &= -(g_{m1} v_i + g_{m2} v_o) (r_{o1} \parallel r_{o2}) \end{aligned}$$

- Rearranging, we find:

$$A_v = \frac{v_o}{v_i} = \frac{-(r_{o1} \parallel r_{o2}) g_{m1}}{1 + (r_{o1} \parallel r_{o2}) g_{m2}} \approx \frac{-g_{m1}}{g_{m2}}$$

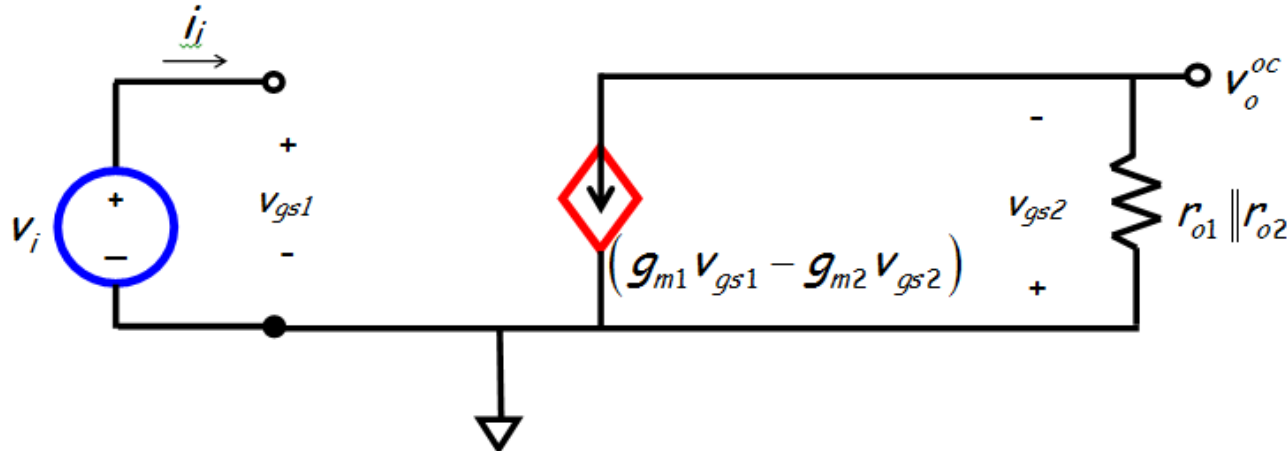
CS Amplifier with Diode-Connected Load (contd.)

- Therefore:
$$A_{vo} = \frac{-g_{m1}}{g_{m2}} = -\frac{2\sqrt{K_1}\sqrt{I_D}}{2\sqrt{K_2}\sqrt{I_D}} = -\sqrt{\frac{K_1}{K_2}} = -\frac{\sqrt{\left(\frac{W}{L}\right)_1}}{\sqrt{\left(\frac{W}{L}\right)_2}}$$

Strong main device and weak load device gives higher gain

In other words, we adjust the MOSFET channel geometry to set the small-signal gain of this amplifier!

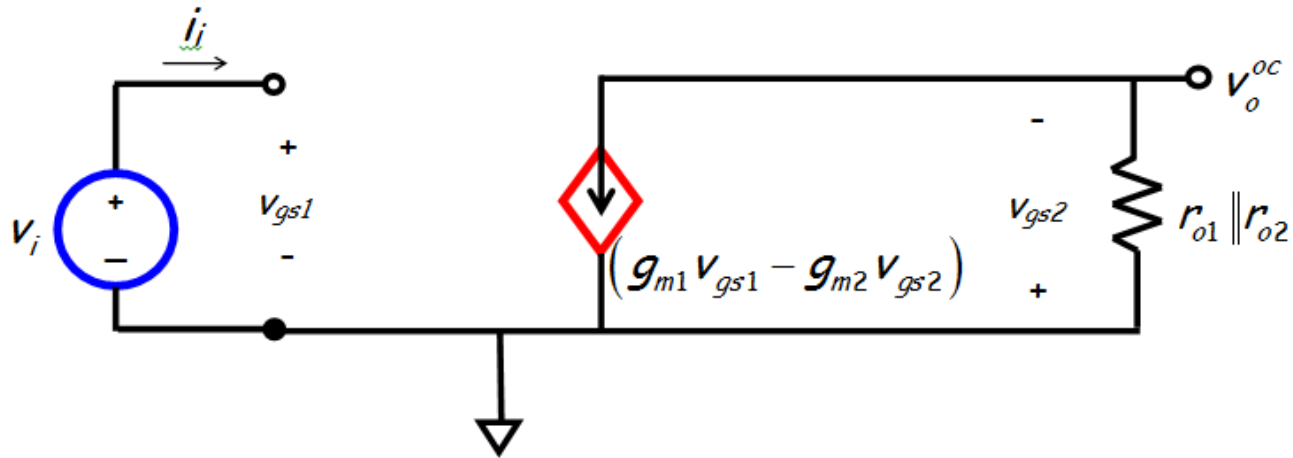
- Now let's determine the small-signal input and output resistances of this amplifier!



- It is evident that:

$$R_i = \frac{v_i}{i_i} = \infty$$

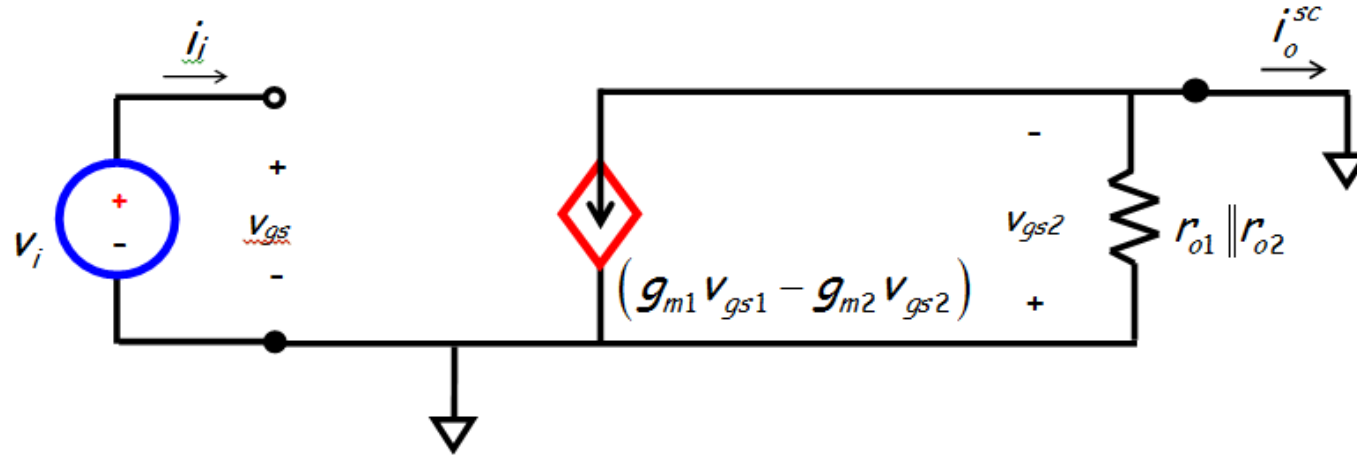
CS Amplifier with Diode-Connected Load (contd.)



- Now for the output resistance, we know that the open-circuit output voltage is:

$$v_o^{oc} = -(g_{m1} v_{gs1} - g_{m2} v_{gs2}) (r_{o1} \parallel r_{o2})$$

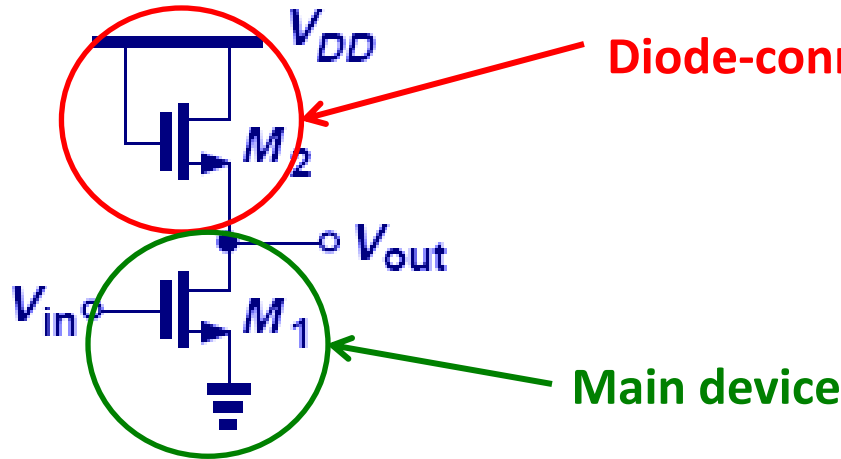
CS Amplifier with Diode-Connected Load (contd.)



- Likewise, the short-circuit output current is: $i_{os} = -(g_{m1} v_{gs1} - g_{m2} v_{gs2})$
- Thus, the small-signal output resistance of this amplifier is equal to:

$$R_o = \frac{v_o^{oc}}{i_o^{sc}} = \frac{-(g_{m1} v_{gs1} - g_{m2} v_{gs2})(r_{o1} \parallel r_{o2})}{-(g_{m1} v_{gs1} - g_{m2} v_{gs2})} = (r_{o1} \parallel r_{o2})$$

CS Amplifier with Diode-Connected Load (contd.)



Diode-connected load \Rightarrow

$$R_D = \frac{1}{g_{m2} + g_{mb2}}$$

$$A_v = -g_m R_D = -g_{m1} \frac{1}{g_{m2} + g_{mb2}}$$

Main device

$$\Rightarrow A_v = -\frac{g_{m1}}{g_{m2}} \frac{1}{1 + \eta} \quad \leftarrow \quad \eta = \frac{g_{mb2}}{g_{m2}}$$

$$\therefore A_v = -\frac{\sqrt{2\mu_n C_{ox} (W/L)_1 I_{D1}}}{\sqrt{2\mu_n C_{ox} (W/L)_2 I_{D2}}} \frac{1}{1 + \eta}$$

- **If variation of η with the output voltage is neglected \rightarrow the gain is independent of bias currents and voltages**
- **However, for this to happen the device M_1 has to remain in saturation \rightarrow this ensures that current I_{D1} is constant \rightarrow ensures constant g_{m1}**
- **In other words, the gain remains relatively constant for the variation in input and output signals \rightarrow ensures that input-output relationship is linear**