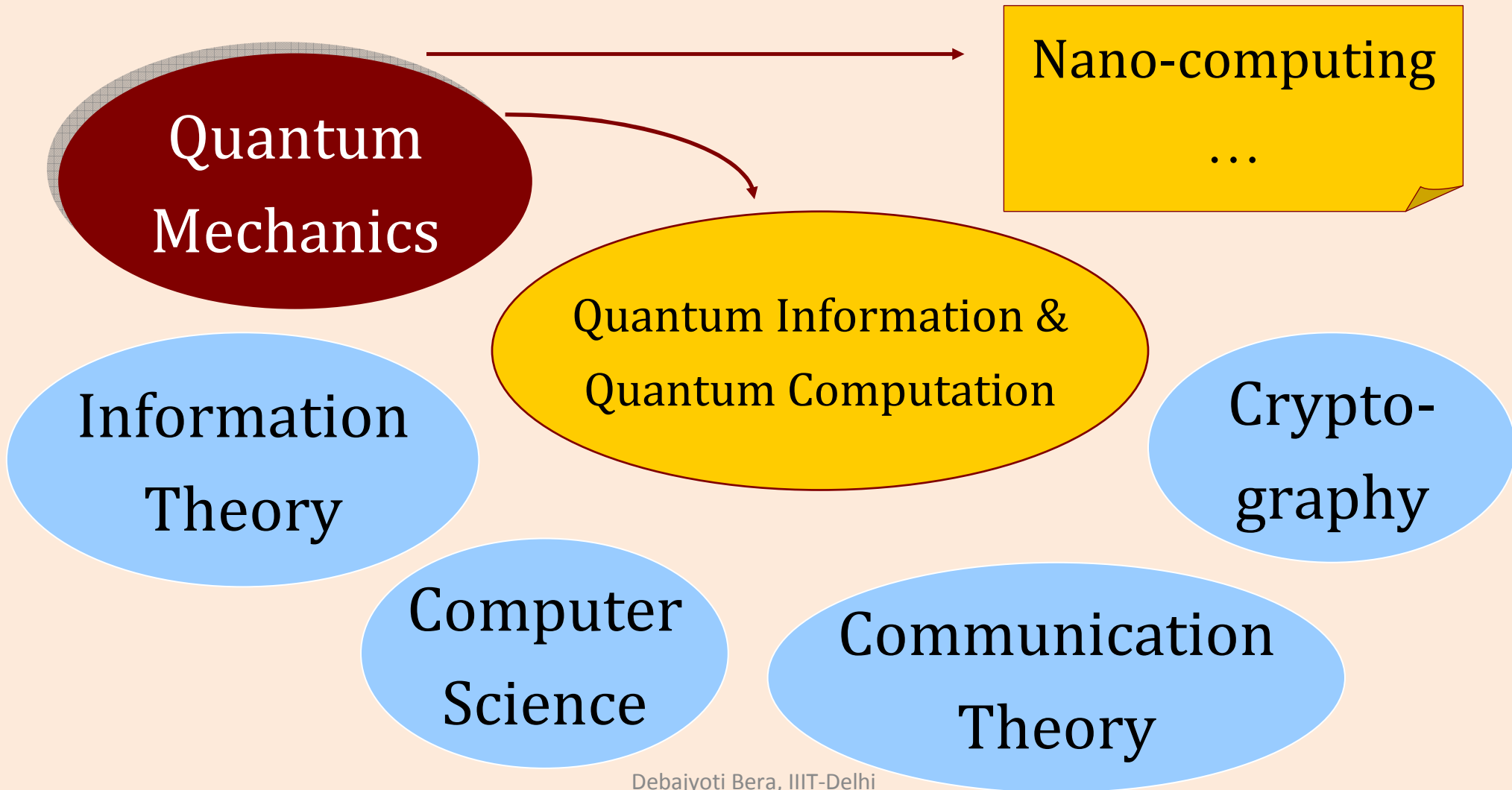


Introduction to Quantum Computing

Debajyoti Bera, IIIT-Delhi

Quantum Computing Community

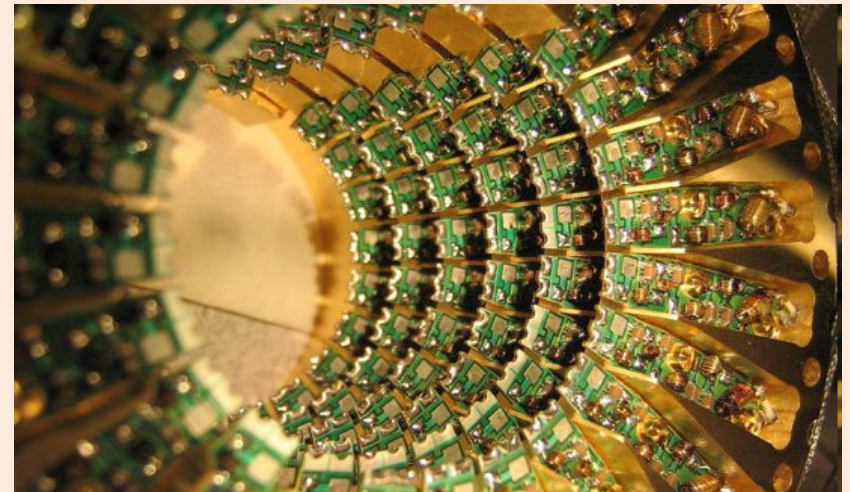


Quantum Computing for Computer Science

1. Studying different models of quantum computing
2. Design and analyse algorithms to efficiently solve problems using these models

What is Quantum Computation

Computation in which the operands and operators follow the laws of quantum mechanics

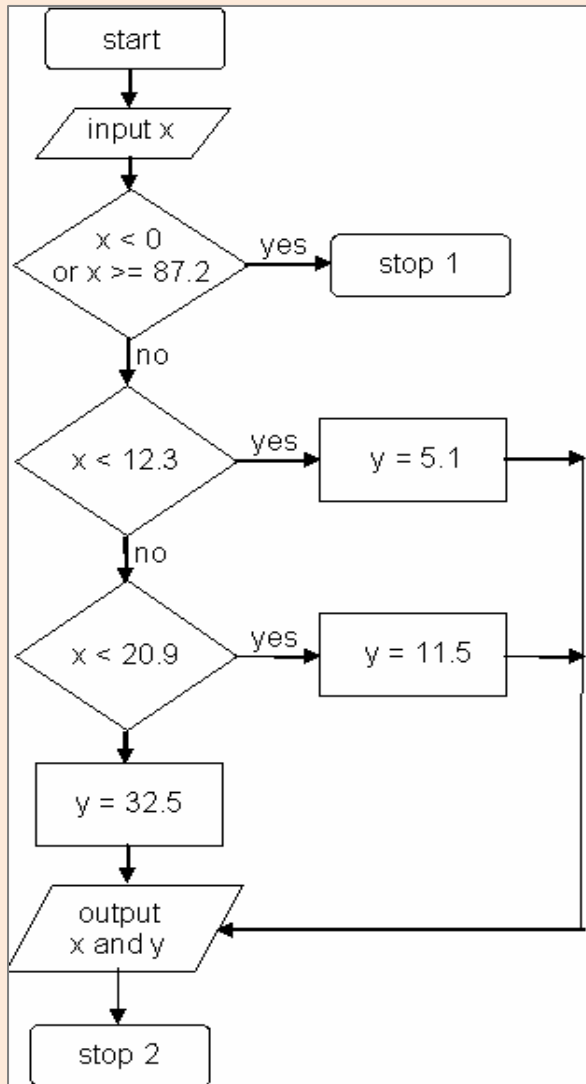


Images – (left) ©IBM, (right) © D-Wave Systems, Inc.

Overview

1. Computation
2. Quantum Mechanics
3. Quantum Computing
4. Progress & Challenge

What is Computation?



A sequence of steps,
Performed by a system
Which, given an input,
Produces output
Where, each step involves
Operation on values

Classical Computation

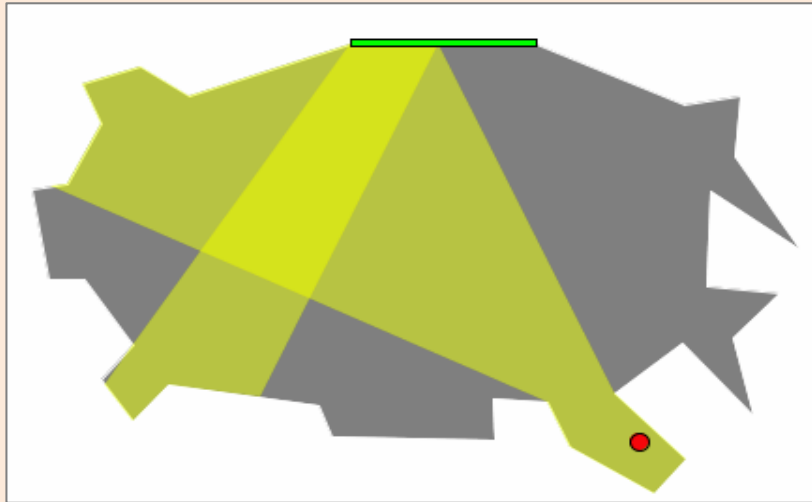
Calculation of compound interest on Rs 877/- for 4 years at the rate of 7% p.a.

(without using formula)

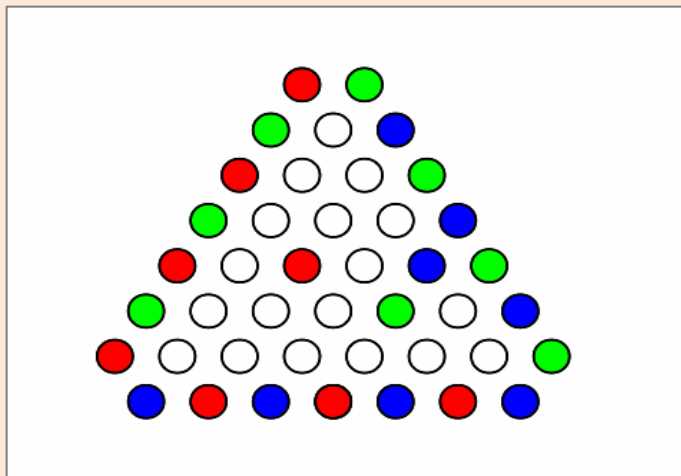
1. Compute interest after 1 year
2. Add interest to principle
3. This is the new principle
4. Compute interest after 2 years ...



Classical Computing: Examples



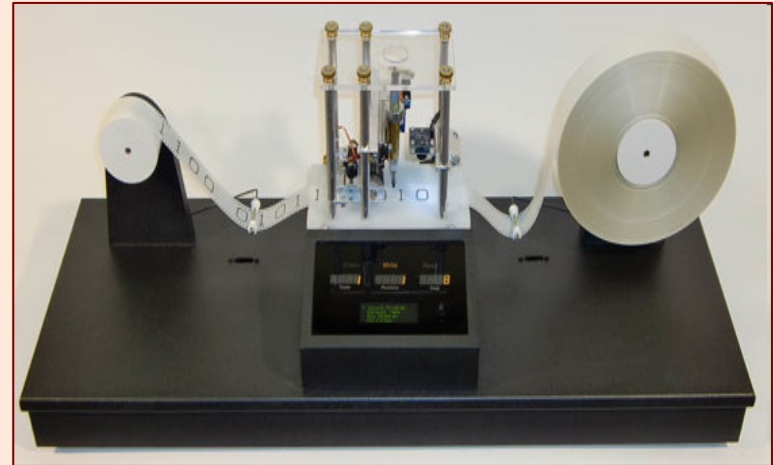
Winning a game of chess
Cheapest flight to Delhi
Finding way to home
Placement of cameras



Analysis of Computation

Models of Computation

- Boolean Circuit
- Turing Machine
- Cellular Automata
- Genetic Algorithm, Neural Network, ...



Metrics for Analysis

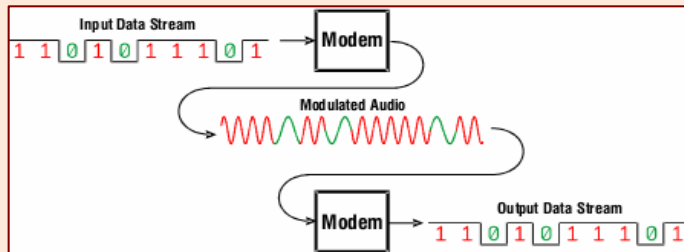
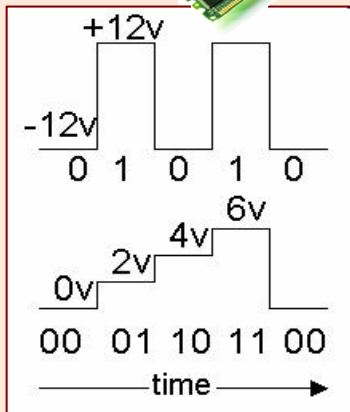
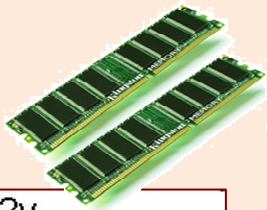
- Time to perform operations
- Space to store operands, ...

Operations & Operands

Operations
on
Operands

=

Change of state
of
“Some Thing”



Operations & Operands

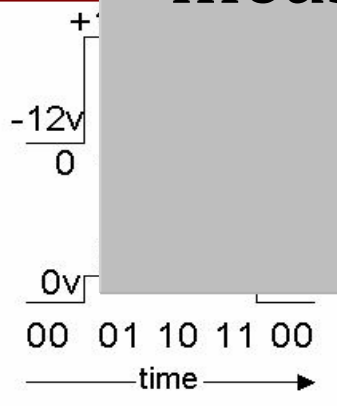
Operations

Change of state



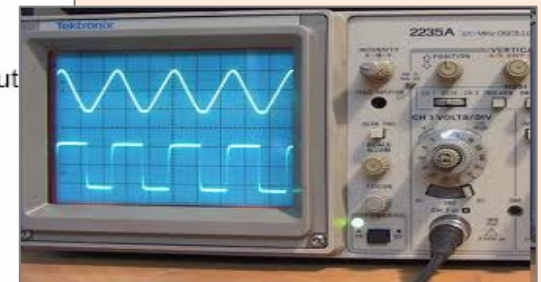
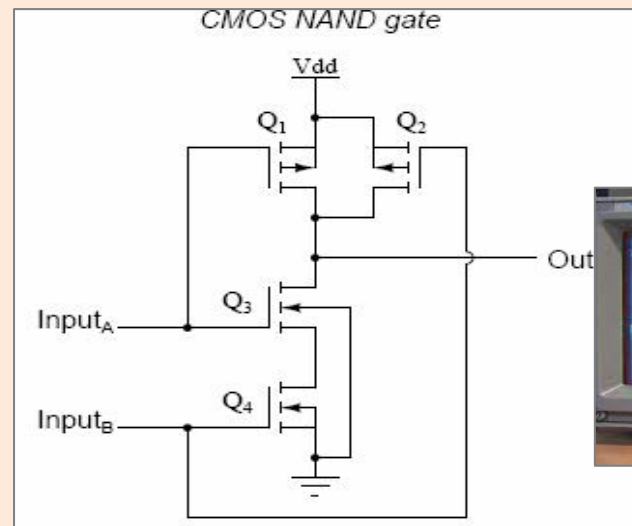
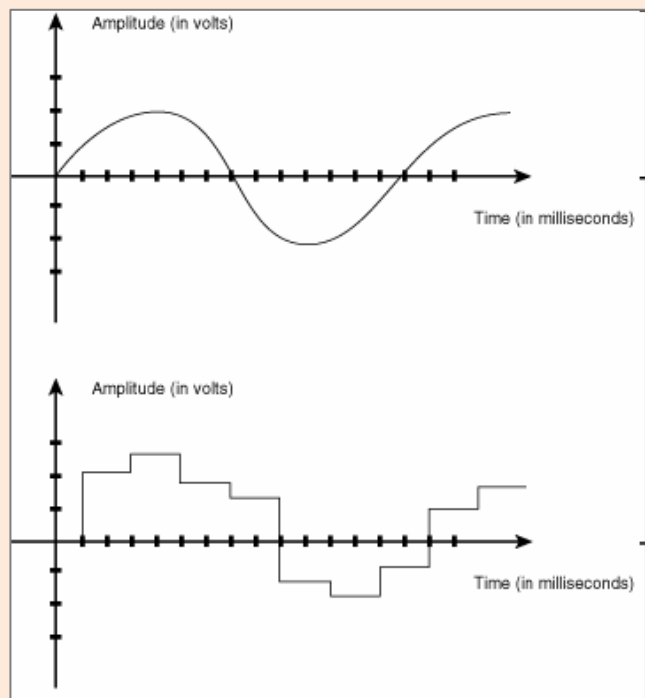
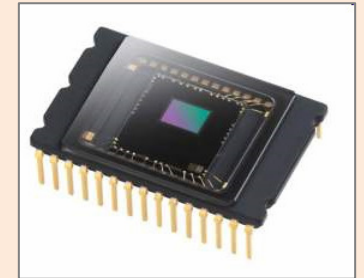
Data/Value

measurable property observable using
macroscopic methods



Classical “bits” and operations

- Bit – digital signal – 0 or 1
- Operations – Boolean functions

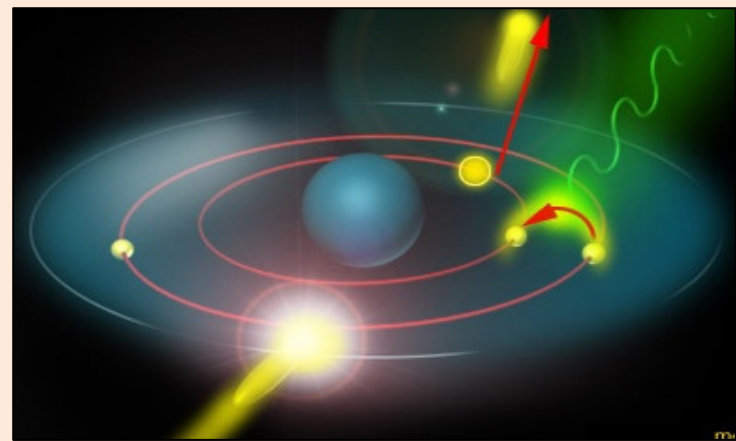
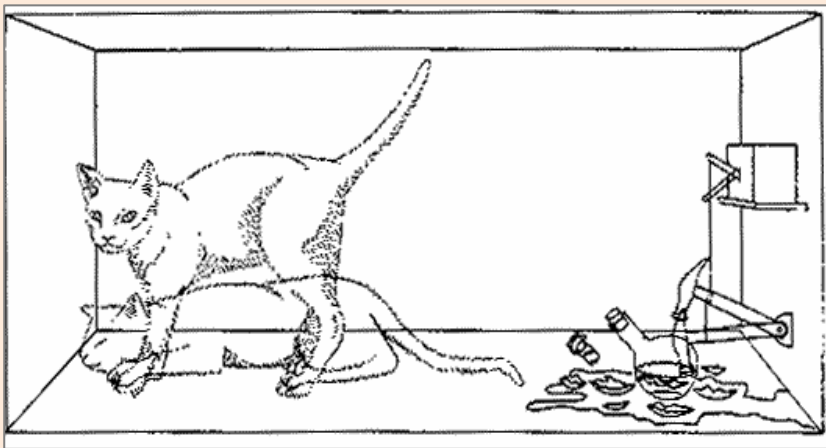


Digital circuits & logic gates

Macroscopic CMOS transistors

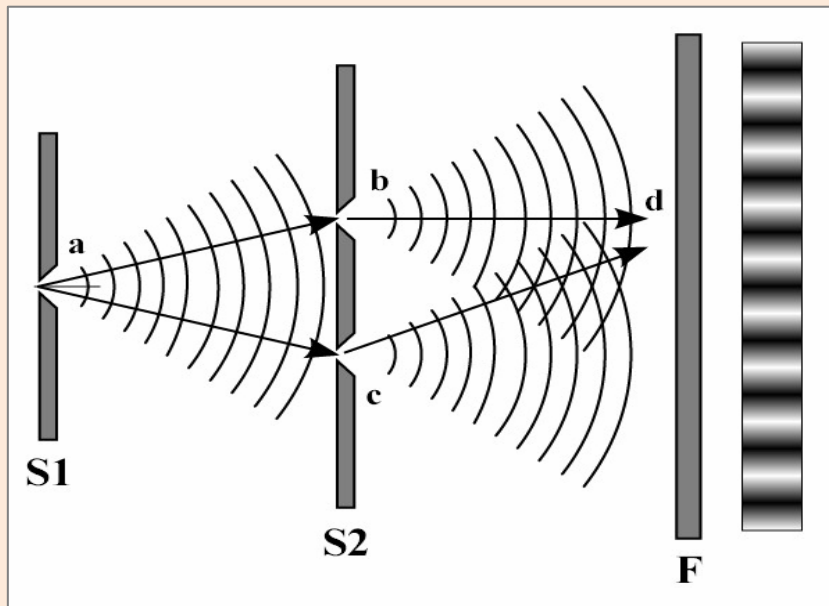
Quantum Mechanics

A proposed theory of nature (reality) that seems to be able to explain many facts about small particles which couldn't be (easily) explained using other theories.

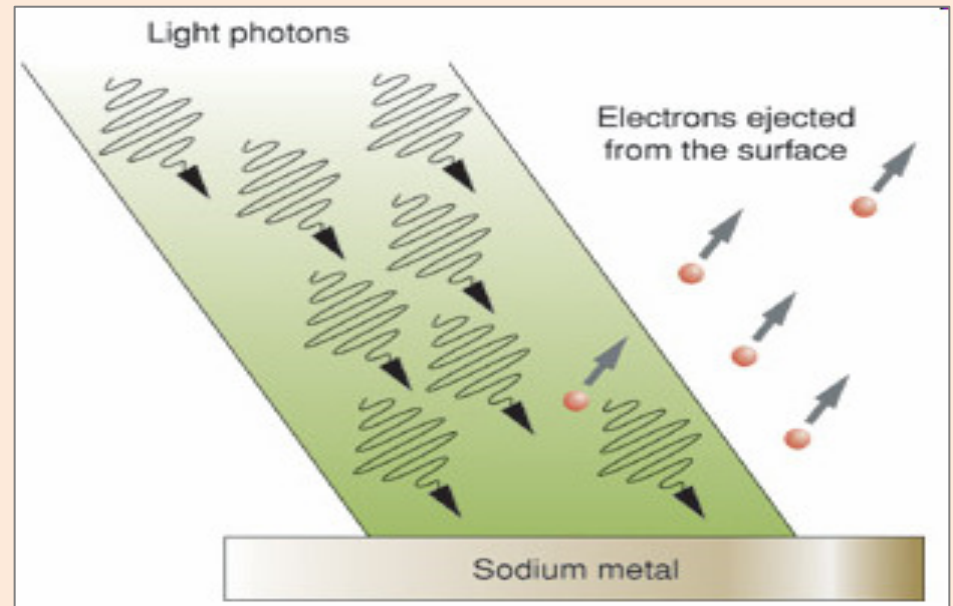


Reality of LIGHT?

1803 – light behaves like
a wave
(Double slit expt.)



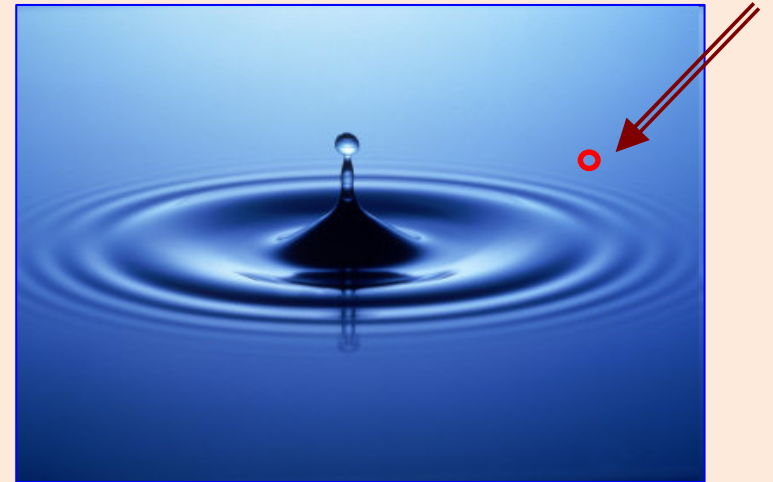
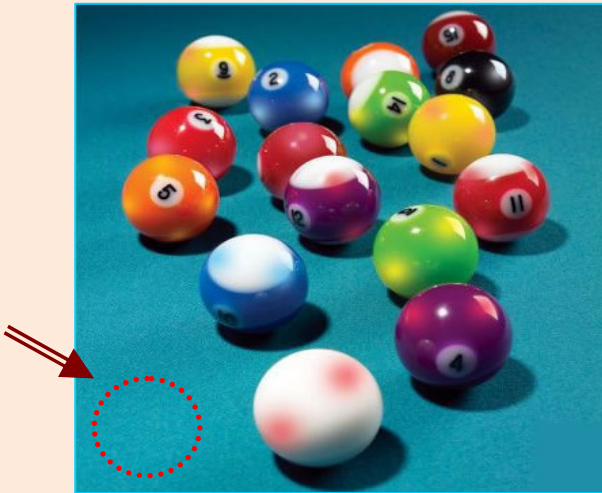
1905 – light is made of
photons
(Photoelectric effect)



Particle -vs- Wave

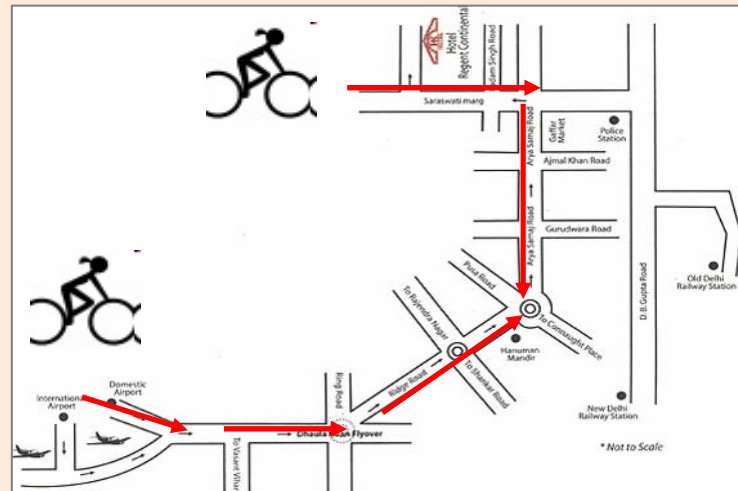
P
A
R
T
I
C
L
E

W
A
V
E

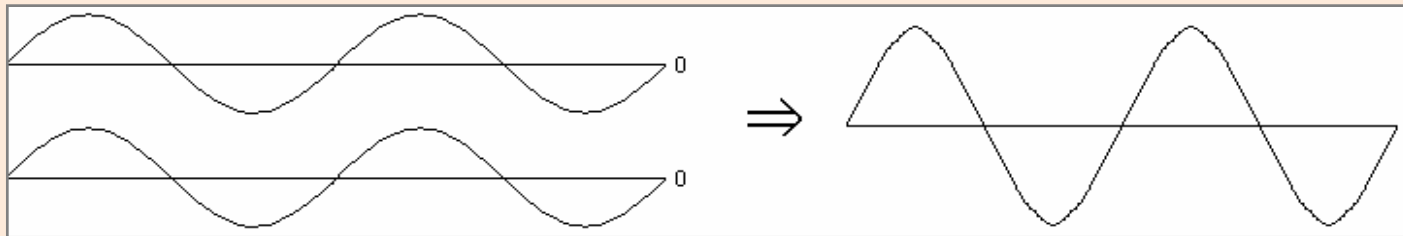


Particle -vs- Wave

PARTICLE

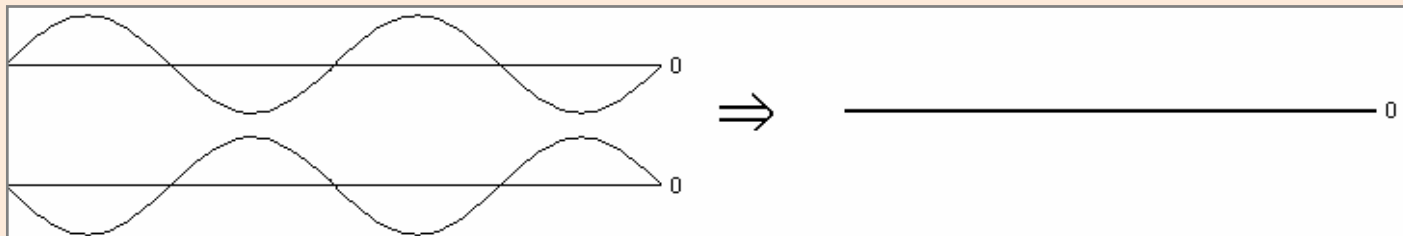


W



constructive interference

A

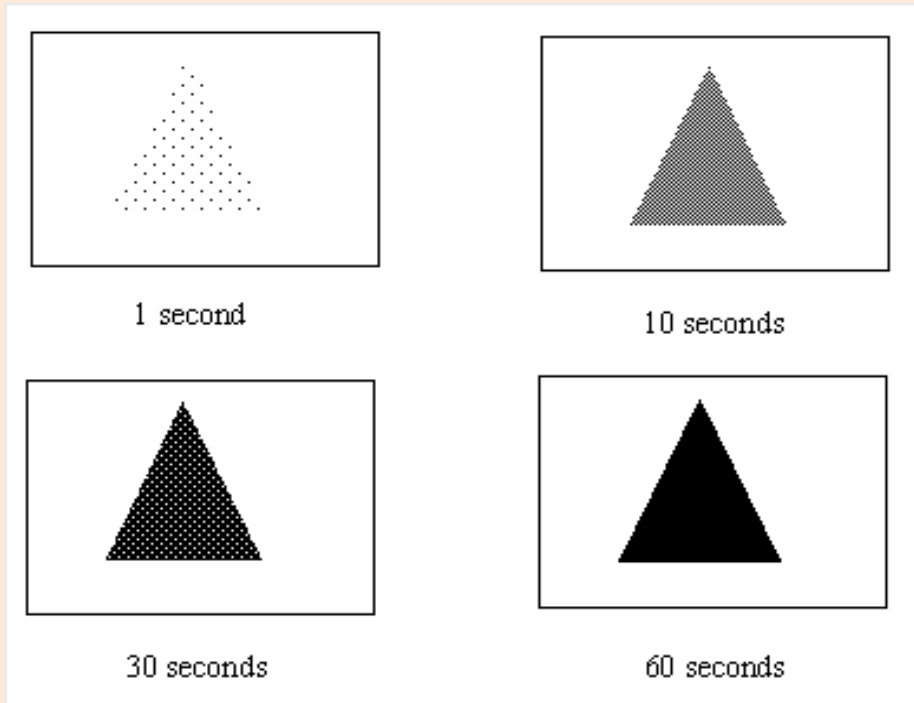


destructive interference

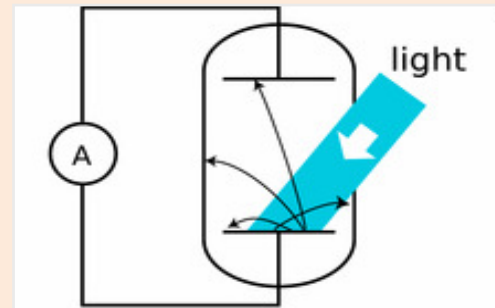
V

E

Light as Particle



Expose photographic plate to a short burst of light



Photoelectric effect

A beam of light strikes a capacitor plate inside a vacuum tube, and electrons are ejected.

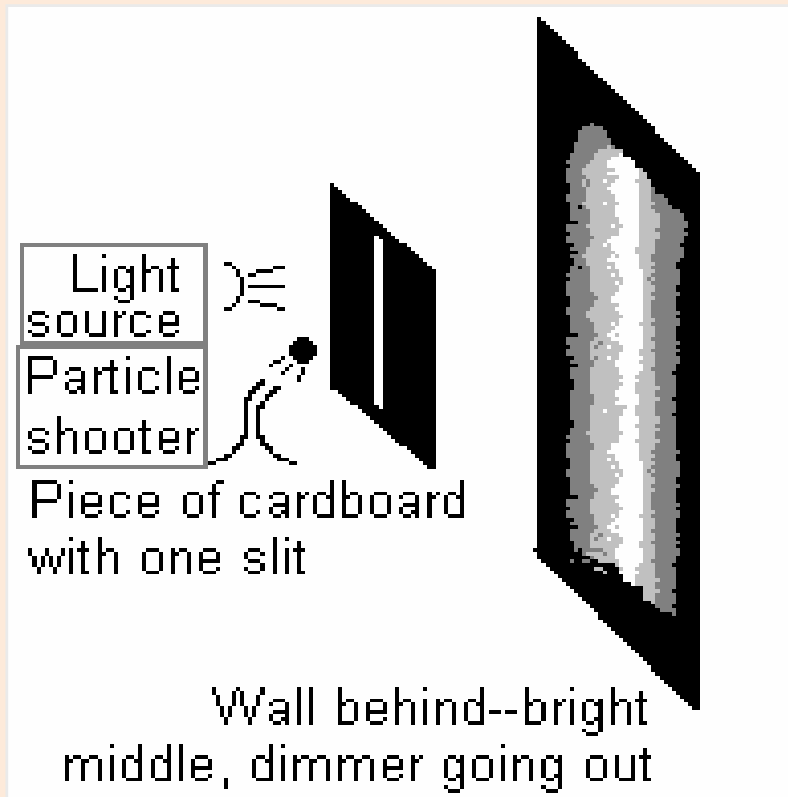
Corpuscular Model of Light – Isaac Newton

Taken from http://www.lightandmatter.com/html_books/lm/ch34/ch34.html

http://www.antonine-education.co.uk/physics_as/module_1/topic_3/topic_3_particle_model_of_light.htm

Debajyoti Bera, IIT-Delhi

Young's Double Slit Expt.

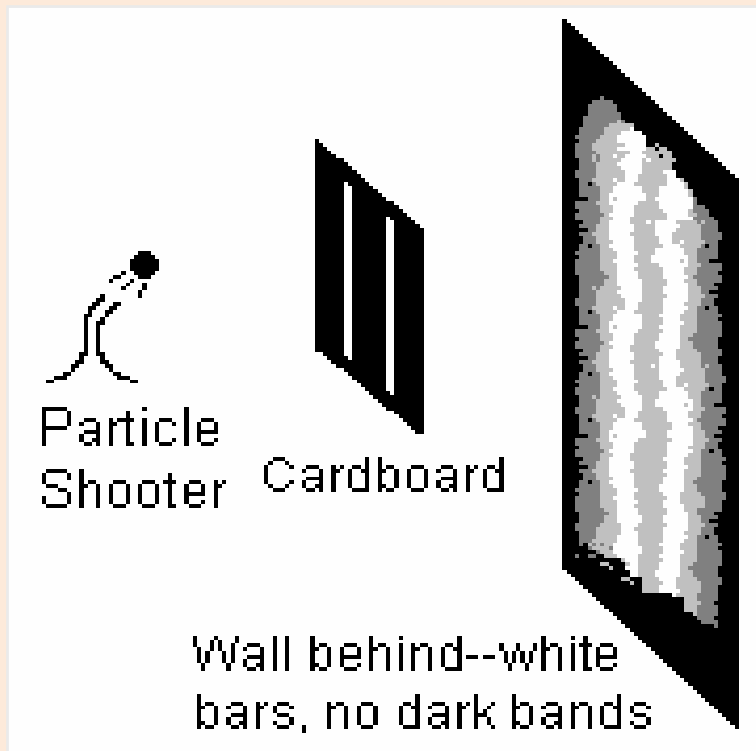


Single slit with light

Single slit with particles

- Bright band behind the slit
- Band fades towards outside

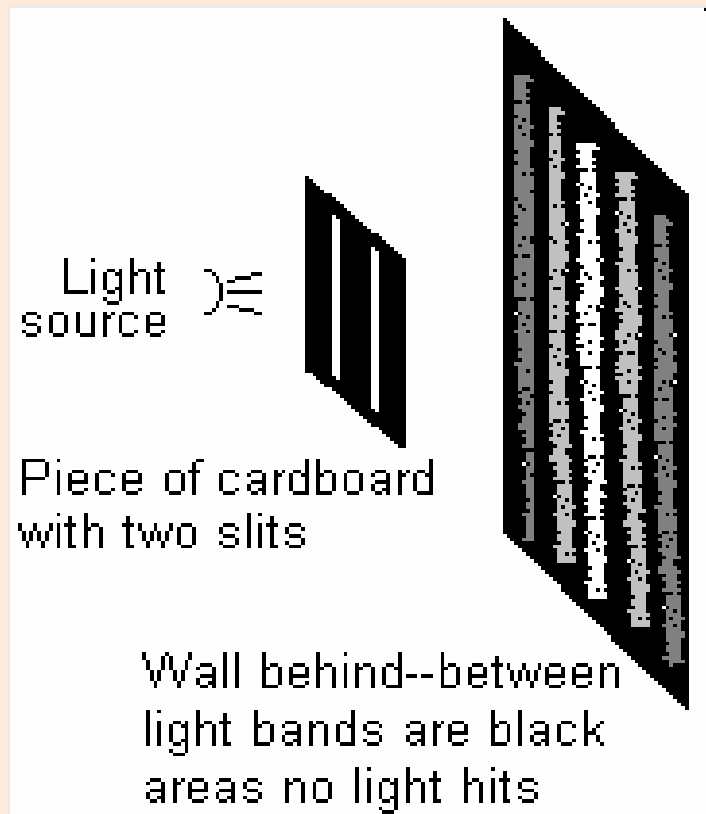
Young's Double Slit Expt.



Double slit with particles

- Two bright bands behind the slits ...
- Bands fade towards outside

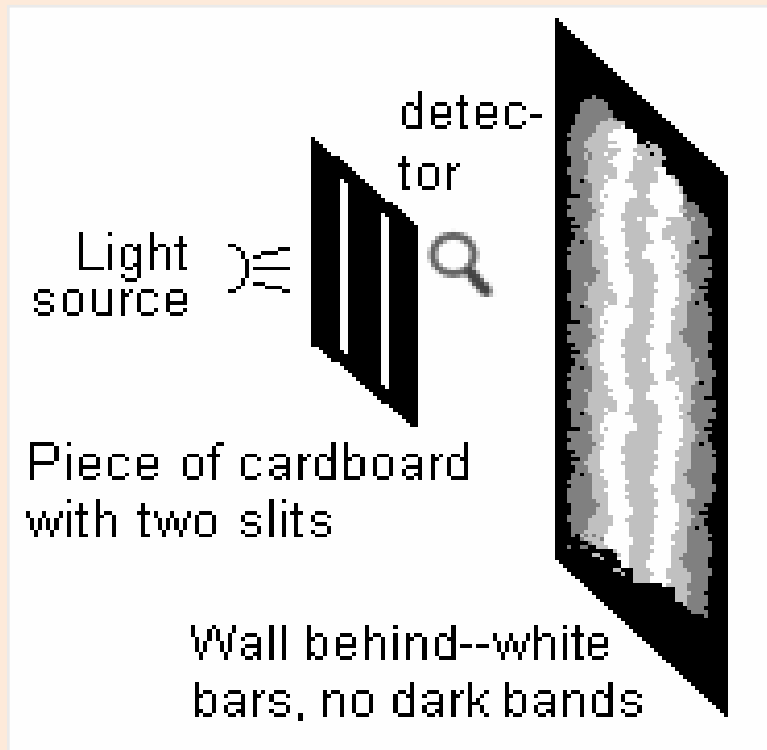
Young's Double Slit Expt.



Double slit with light

- Two bright bands behind the slits ...
- Alternate bright and dark bands towards outside

Young's Double Slit Expt.



Double slit with light +
Photon-detector at one slit

- Two bright bands behind the slits ...
- Alternate bright and dark bands towards outside

Just like particle!

Quantum Mechanical properties of Light, Electron, ...

- Both Particle & Wave
- Behaves like a particle whose “presence” follows a wave pattern (wavefunction)
 - Simultaneously present at all places
 - ... unless observed ...
 - During observation, found at any one place with “some possibility” decided by the wavefunction
- Interference & other properties of waves...



Quantum Computing Basics

Many properties follow wavefunction:

- simultaneously all possible values
- “collapses” to one value during observation

Quantum Computing

Assuming ...

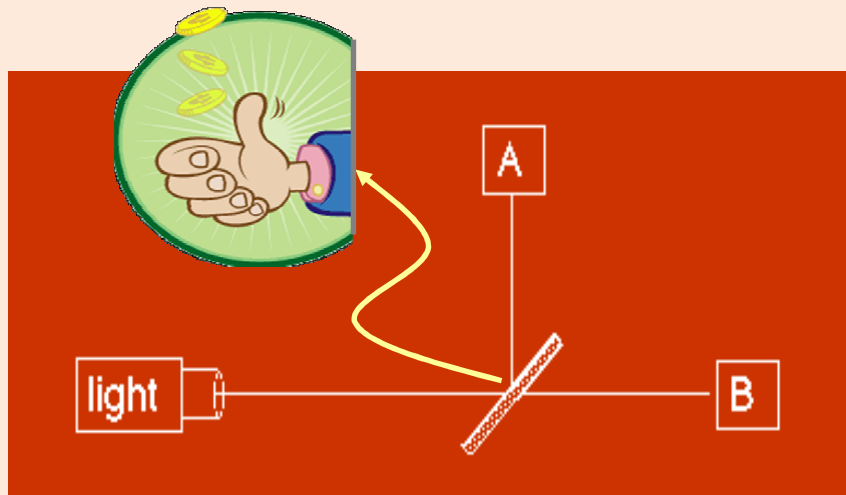
Machines which follow principles of quantum mechanics...

... Can we compute more effectively?

- Less time
- More space
- Fewer error

Quantum is better than Classical

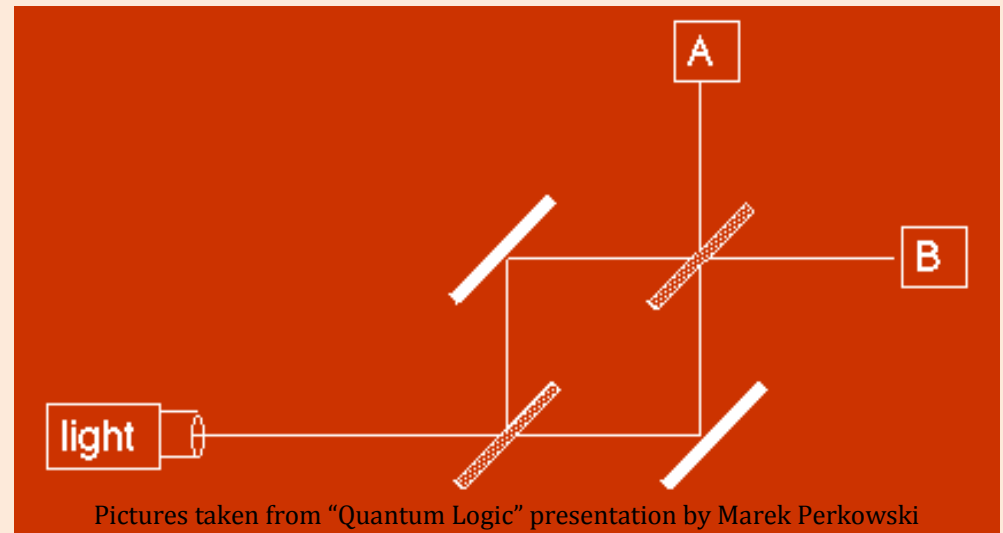
Using Photons for Data



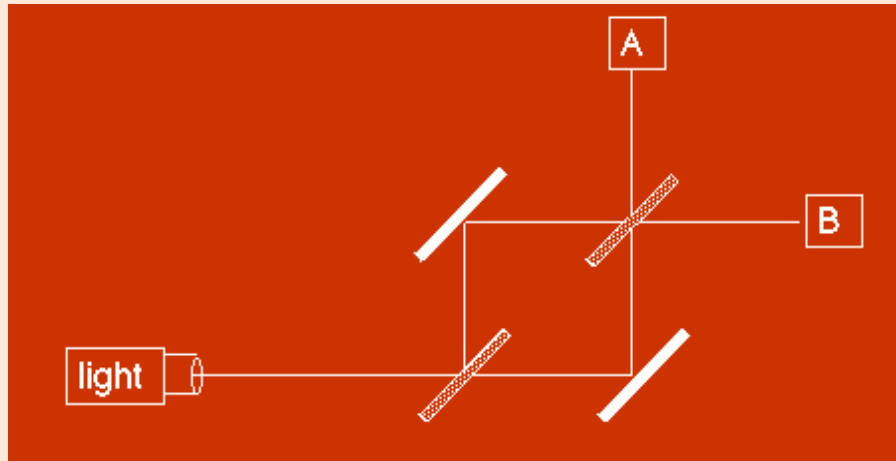
1. 50% photons leaving the light source arrive at detector A
2. Rest 50% arrive at B

All photons leaving the source arrive at A !!!!

Expt. setup: Equal path lengths, rigid mirrors, only one photon in the apparatus at a time.



Quantum Bits – “qubits”



Combined State/
Wavefunction

Individual
States / Possibilities

$$|\Psi\rangle = \alpha_1 |S_1\rangle + \alpha_2 |S_2\rangle + \alpha_3 |S_3\rangle + \dots$$

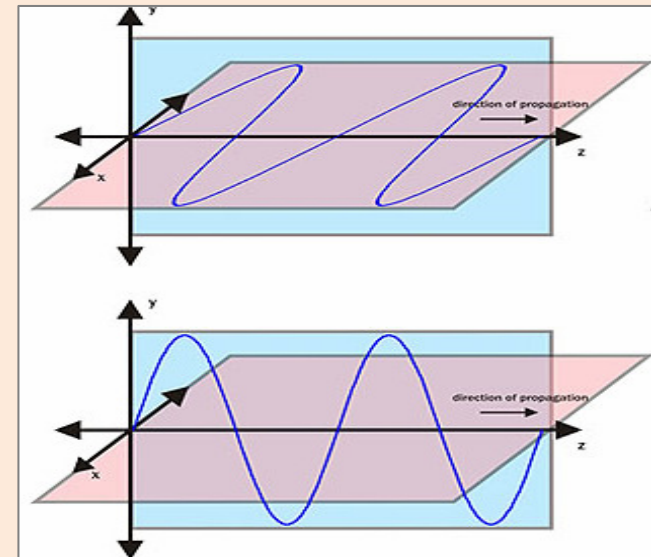
Amplitude (value of possibility)
— can be -ve (interference)

Qubits

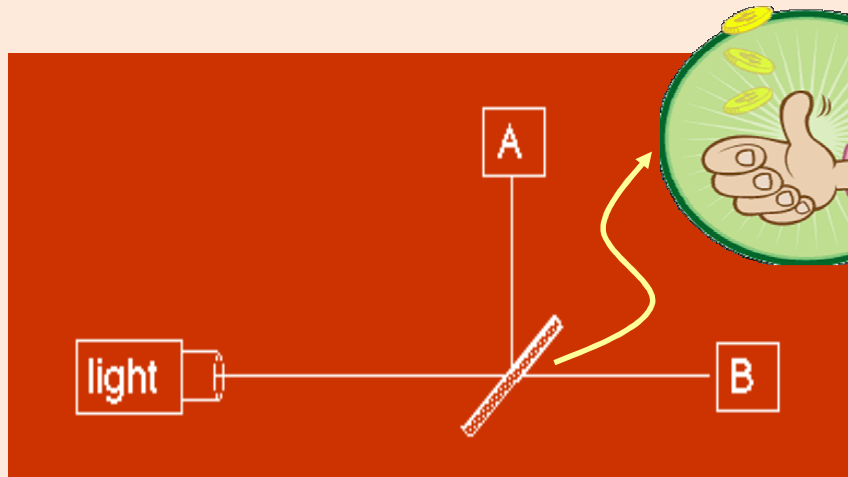
- Infrared Photon – polarisation (.1msec)
- Trapped Ion – energy levels (15sec)
- Trapped Atom – energy levels (3sec)
- Nuclear Spins – spin orientation (2-25sec)

Mathematically...

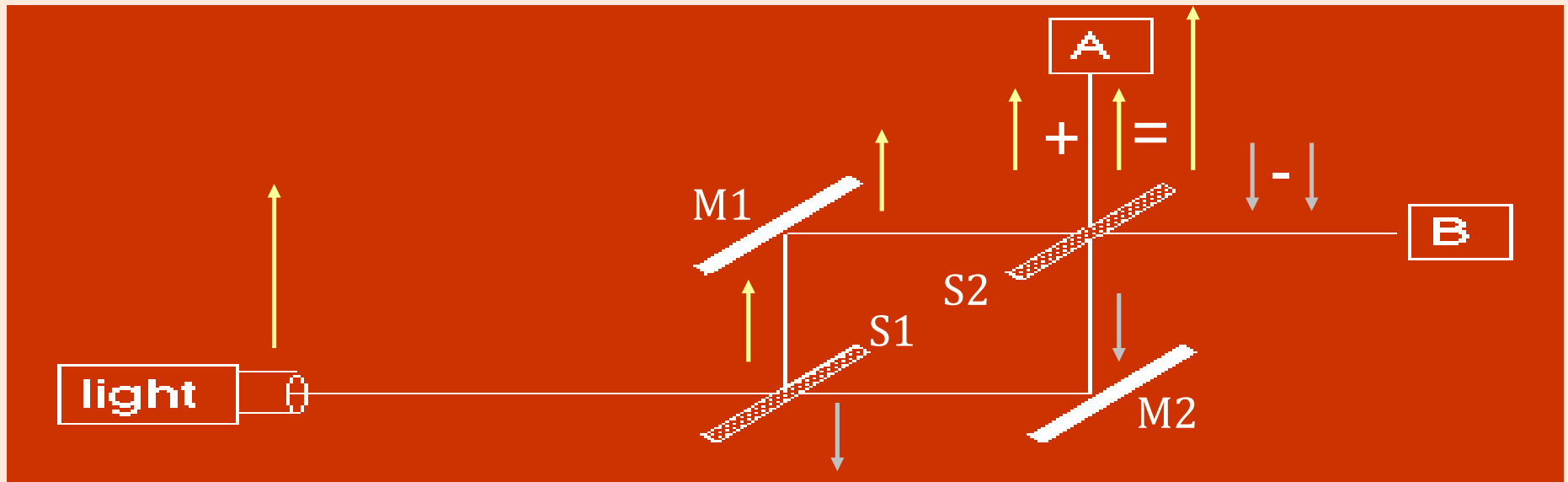
A state with k possibilities is a unit-vector in \mathbb{C}^k



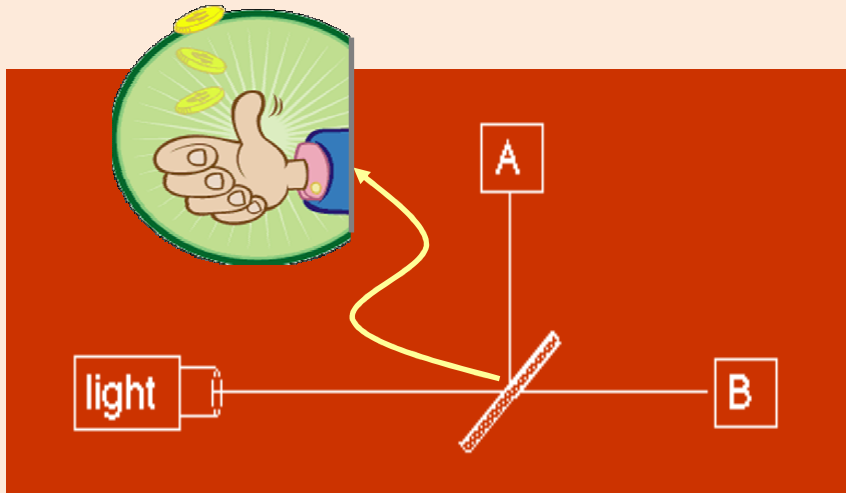
Operations on Photons



$$\begin{aligned}
 |\uparrow\rangle &\rightarrow \frac{1}{\sqrt{2}}|\uparrow\rangle + \frac{1}{\sqrt{2}}|\downarrow\rangle \\
 |\downarrow\rangle &\rightarrow \frac{1}{\sqrt{2}}|\uparrow\rangle - \frac{1}{\sqrt{2}}|\downarrow\rangle
 \end{aligned}$$



Quantum Operators



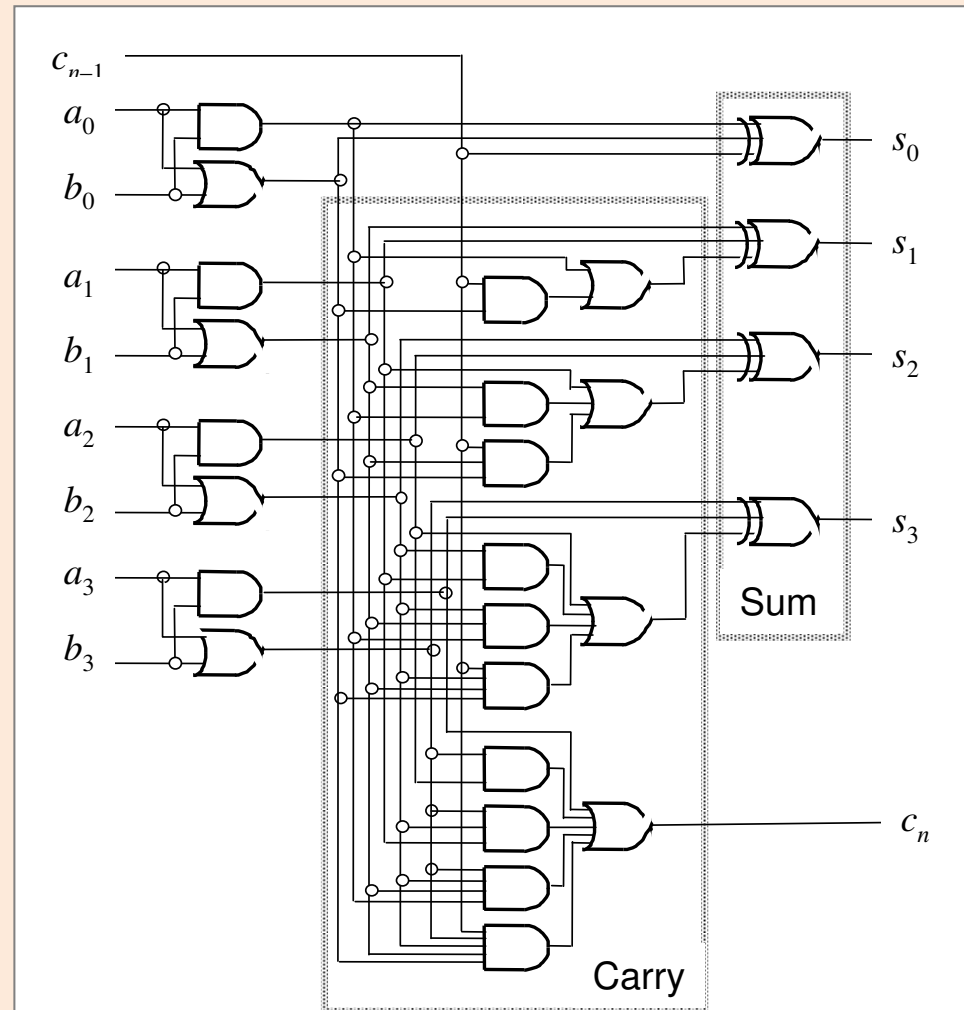
Unitary operators
(length-preserving,
over complex
numbers)

$$\begin{aligned} |\uparrow\rangle &\rightarrow \frac{1}{\sqrt{2}}|\uparrow\rangle + \frac{1}{\sqrt{2}}|\downarrow\rangle \\ |\downarrow\rangle &\rightarrow \frac{1}{\sqrt{2}}|\uparrow\rangle - \frac{1}{\sqrt{2}}|\downarrow\rangle \end{aligned}$$

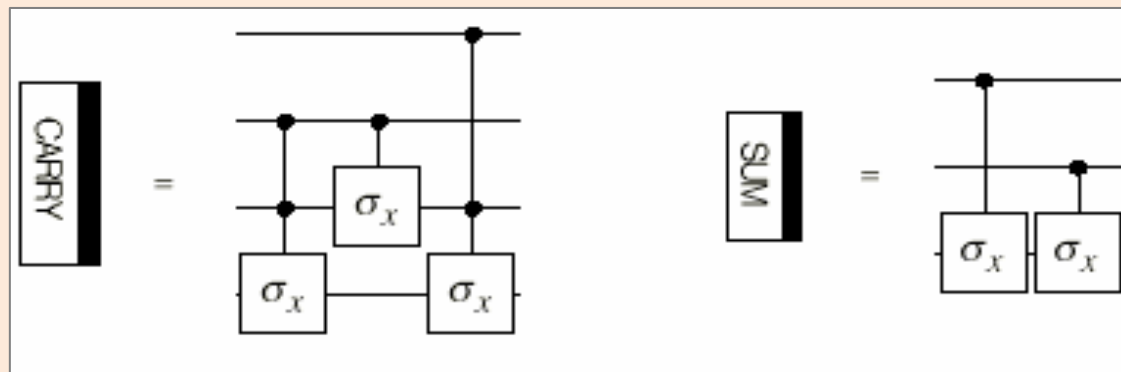
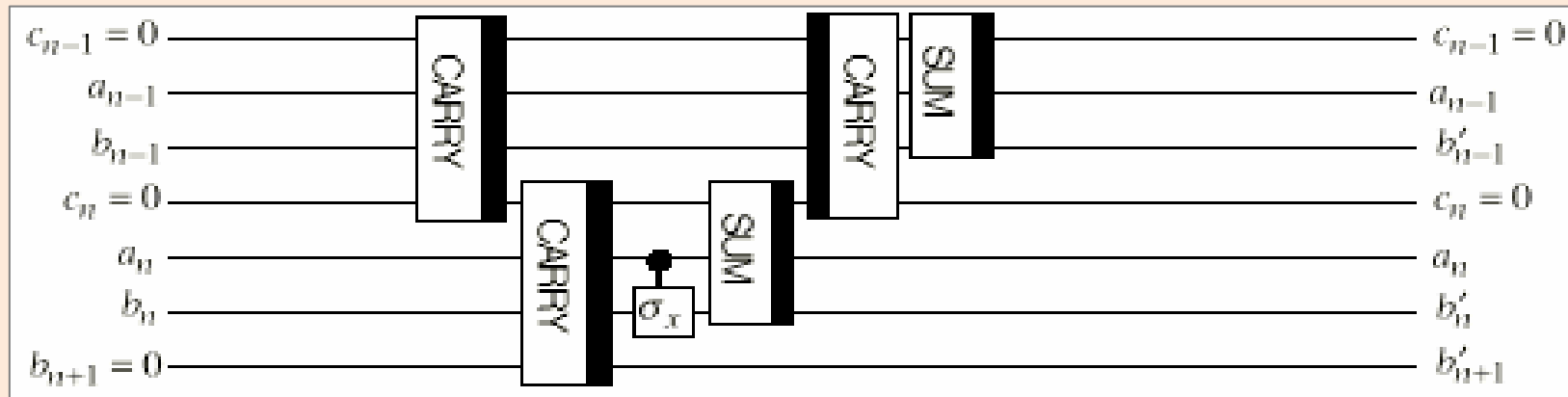
Hadamard Operator

- NMR
- Optical Lattice
- Trapped Ion QC
- Cavity QED

Classical Adder



Quantum Adder



σ_x : Pauli rotation

$$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

Unlike Classical ...

✓ **Superposition**

✓ Measurement

✓ Interference

✓ No copying

✓ Entanglement (multi qubit)

At the same time, both 0 & 1

vs.

At the same time, either 0 OR 1

Unlike Classical ...

- ✓ Superposition
- ✓ Measurement
- ✓ Interference
- ✓ No copying
- ✓ Entanglement (multi qubit)

Reality is independent of observation

VS

Reality changes after observation

Unlike Classical ...

- ✓ Superposition
- ✓ Measurement
- ✓ **Interference**
- ✓ No copying
- ✓ Entanglement (multi qubit)

Multiple occurrence increases probability

vs.

Multiple occurrence may decrease probability

Unlike Classical ...

✓ Superposition

✓ Measurement

✓ Interference

✓ **No copying**

✓ Entanglement (multi qubit)

Cannot duplicate a state (qubit)

vs.

Can create arbitrary copies of data

Unlike Classical ...

- ✓ Superposition
- ✓ Measurement
- ✓ Interference
- ✓ No copying
- ✓ Entanglement (multi qubit)

Value affected by far-off operations

vs.

Value affected by only local operations

Secret Recipe

- In quantum systems possibilities count, even if they never happen!
- Each of exponentially many possibilities can be used to perform a part of a computation at the same time.
- It may be possible to cancel out “bad” possibilities during computation.

Pitfalls!

- Gates and circuits must be reversible (lossless computation)
- During measurement, all possible computations except only one are destroyed
- Temporary copies of intermediate results cannot be made
- Interference with environment completely changes computation (decoherence)

Quantum Computing:

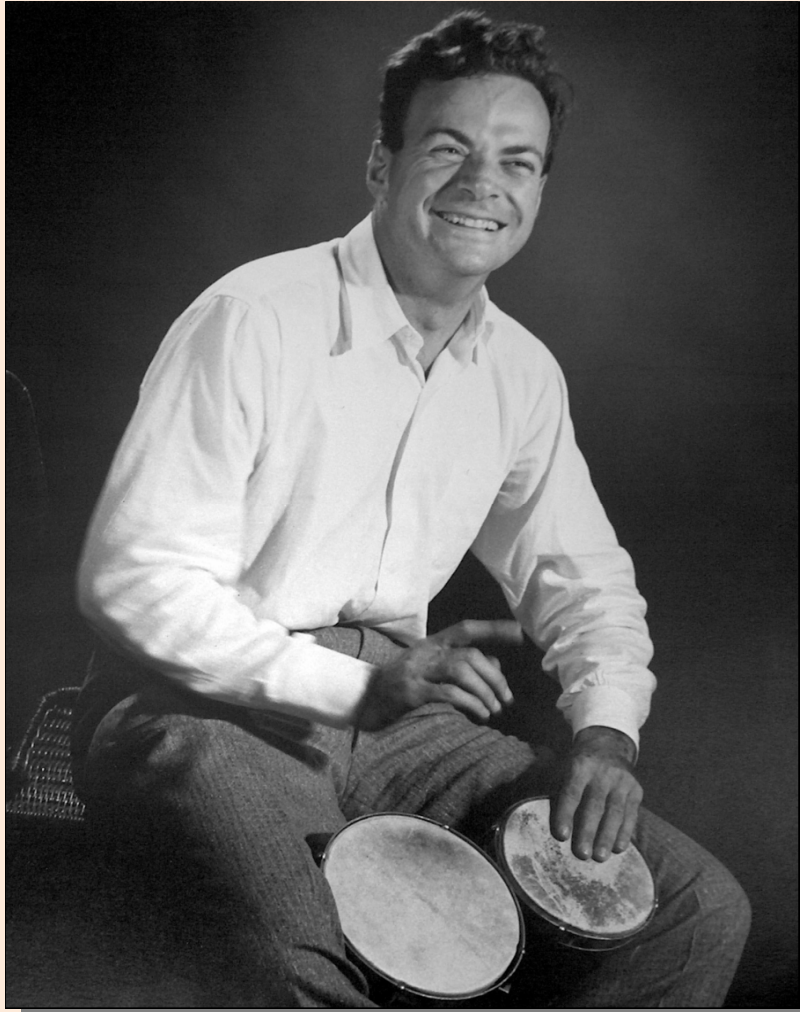
1982 ...

1982

Simulating Physics with
Computers

- *Richard Feynman*

“Nature isn't classical, dammit, and if you want to make a simulation of Nature, you'd better make it quantum mechanical, and by golly it's a wonderful problem, because it doesn't look so easy.”



... **1985** ...

Church-Turing thesis (1930-1950): Anything that can be computed (by a mechanical process) can be computed by a Turing machine.

1985

Church-Turing-Deutsch thesis: Anything that can be computed by a physical process can be computed by a universal computing device (Universal Quantum Turing Machine).

... 1993 ...

1985: Deutsch – (inefficient) universal quantum Turing machine

1993

- Bernstein-Vazirani / Yao – efficient universal quantum Turing machine
- Equivalence of quantum computing models: quantum Turing machine & quantum circuit

... 1994 – 1996 ...

1994 - Peter Shor came up with a quantum algorithm to factor very large numbers incredibly fast.

1997 - Lov Grover developed a quantum search algorithm which takes significantly lesser time to search unstructured database.

Both better than known classical algorithm!

... 1998 – 2001 ...

Experimental demonstrations

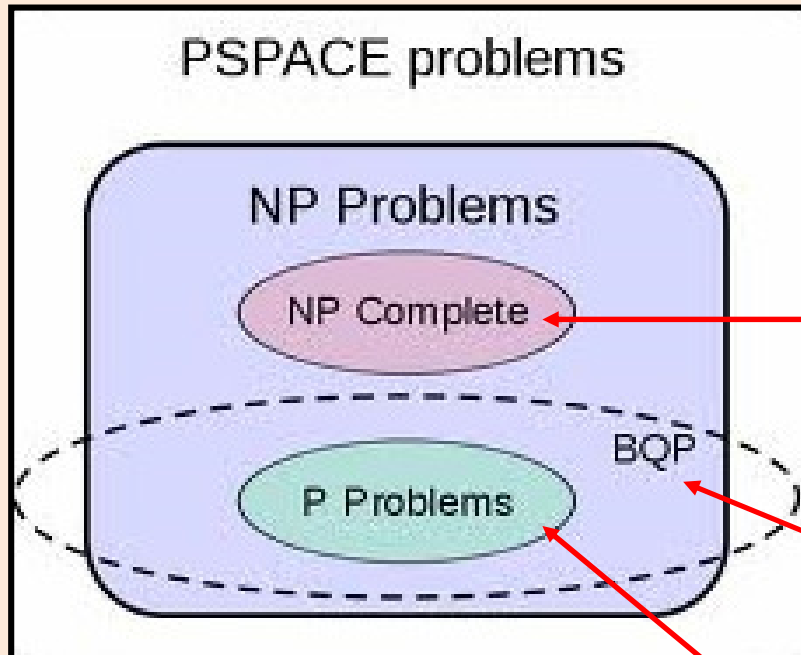
- 2-qubit NMR quantum computer to solve Deutsch's problem (Oxford University, IBM-Stanford-MIT)
- 3-qubit, 5-qubit, 7-qubit NMR computer
- Execution of Grover's algorithm on an NMR computer
- Execution of Shor's algorithm to factor 15

... 2001 – 2011 ...

Theory of Quantum Computing

- ✓ Efficient quantum circuits
 - Smaller size, lesser time, fewer faults
- ✓ Efficient quantum algorithms
 - Lesser storage, lesser time, fewer error
- ✓ Efficient quantum communication protocols
 - Lesser communication
- ✓ Also! Problems for which quantum algorithm provably cannot do significantly better than classical algorithms

Challenges (for Comp. Sc.)

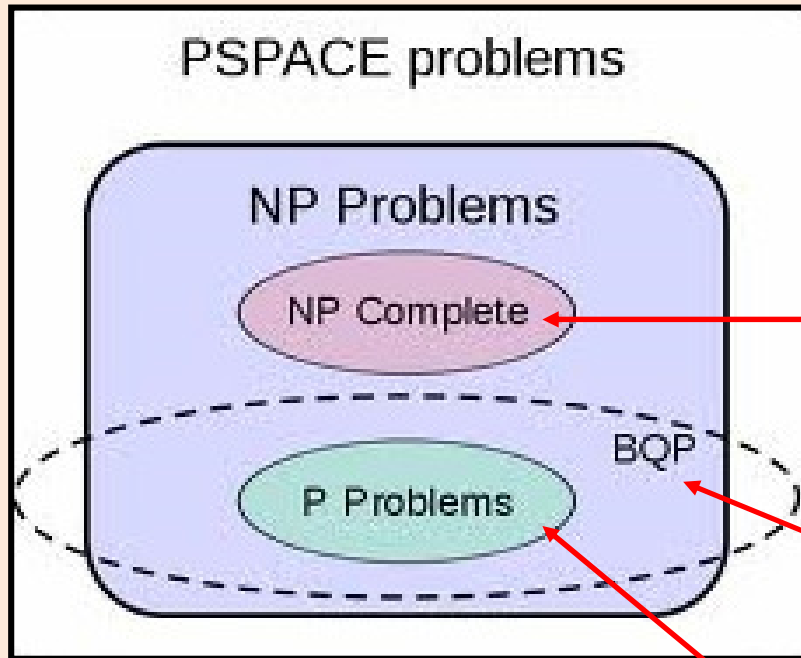


Possibly hard for classical computers
Timetable scheduling for large school

Easily solved by quantum computers
Factoring a very large number

Easily solved by classical computers
Testing if a number is prime

Challenges (for Comp. Sc.)



Possibly hard for classical computers
Timetable scheduling for large school

Easily solved by quantum computers
Factoring a very large number

- Find efficient solutions for hard problems
- Understand which problems are still hard
- Make solutions robust to errors and failures